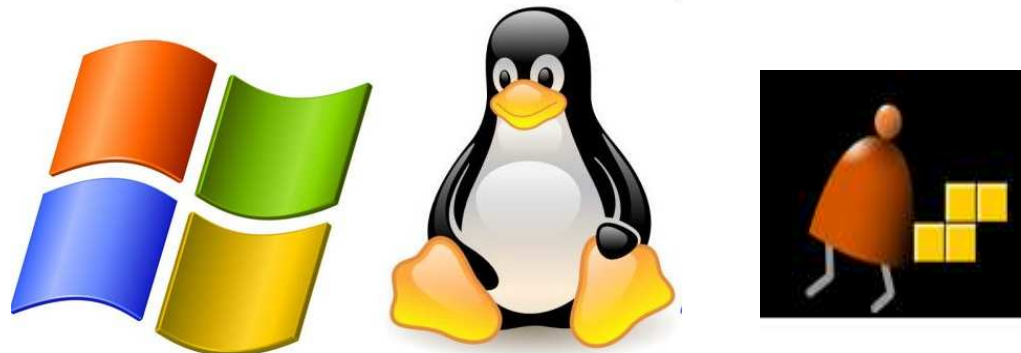


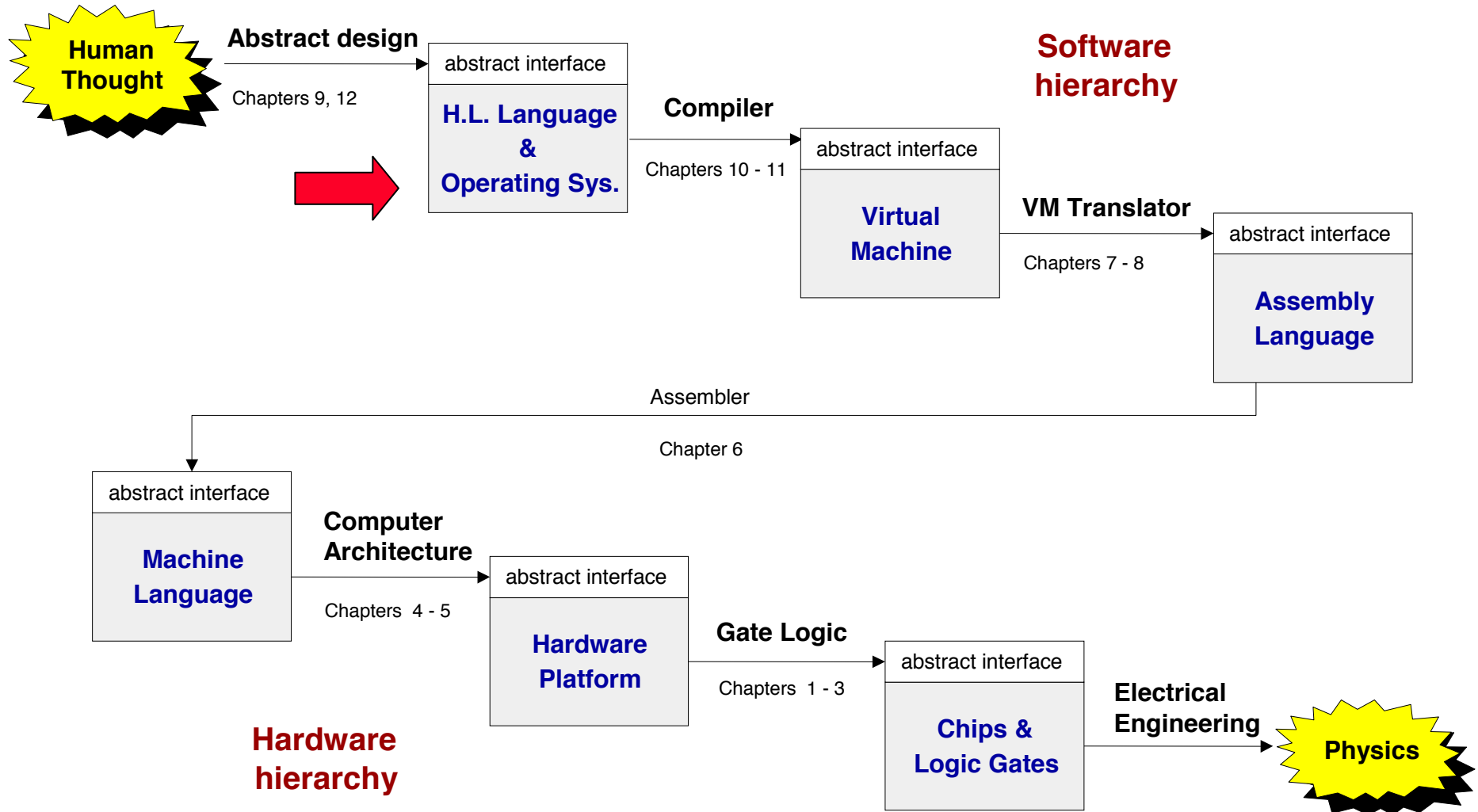
Operating Systems



Building a Modern Computer From First Principles

www.nand2tetris.org

Where we are at:



Jack revisited

```
/** Computes the average of a sequence of integers. */
class Main {
  function void main() {
    var Array a;
    var int length;
    var int i, sum;

    let length = Keyboard.readInt("How many numbers? ");
    let a = Array.new(length); // Constructs the array
    let i = 0;

    while (i < length) {
      let a[i] = Keyboard.readInt("Enter the next number: ");
      let sum = sum + a[i];
      let i = i + 1;
    }

    do Output.printString("The average is: ");
    do Output.printInt(sum / length);
    do Output.println();
    return;
  }
}
```

Jack revisited

```
/** Computes the average of a sequence of integers. */
class Main {
  function void main() {
    var Array a;
    var int length;
    var int i, sum;

    let length = Keyboard.readInt("How many numbers? ");
    let a = Array.new(length); // Constructs the array
    let i = 0;

    while (i < length) {
      let a[i] = Keyboard.readInt("Enter the next number: ");
      let sum = sum + a[i];
      let i = i + 1;
    }

    do Output.printString("The average is: ");
    do Output.printInt(sum / length);
    do Output.println();
    return;
  }
}
```

Typical OS functions

Language extensions / standard library

- Mathematical operations
(**abs**, **sqrt**, ...)
- Abstract data types
(**String**, **Date**, ...)
- Output functions
(**printChar**, **printString** ...)
- Input functions
(**readChar**, **readLine** ...)
- Graphics functions
(**drawPixel**, **drawCircle**, ...)
- And more ...

System-oriented services

- Memory management
(objects, arrays, ...)
- I/O device drivers
- Mass storage
- File system
- Multi-tasking
- UI management (shell / windows)
- Security
- Communications
- And more ...

The Jack OS

- **Math:** Provides basic mathematical operations;
- **String:** Implements the **String** type and string-related operations;
- **Array:** Implements the **Array** type and array-related operations;
- **Output:** Handles text output to the screen;
- **Screen:** Handles graphic output to the screen;
- **Keyboard:** Handles user input from the keyboard;
- **Memory:** Handles memory operations;
- **Sys:** Provides some execution-related services.

Jack OS API

```
class Math {  
  Class String {  
    Class Array {  
      class Output {  
        Class Screen {  
          class Memory {  
            Class Keyboard {  
              Class Sys {  
                function void halt():  
                function void error(int errorCode)  
                function void wait(int duration)  
              }  
            }  
          }  
        }  
      }  
    }  
  }  
}
```

A typical OS:

- ❑ Is modular and scalable
- ❑ Empowers programmers (language extensions)
- ❑ Empowers users (file system, GUI, ...)
- ❑ Closes gaps between software and hardware
- ❑ Runs in “protected mode”
- ❑ Typically written in some high level language
- ❑ Typically grows gradually, assuming more and more functions
- ❑ Must be efficient.

Efficiency

We have to implement various operations on n -bit binary numbers ($n = 16, 32, 64, \dots$).

For example, consider *multiplication*

■ Naïve algorithm: to multiply $x*y$: { for $i = 1 \dots y$ do $sum = sum + x$ }

Run-time is proportional to y

In a 64-bit system, y can be as large as 2^{64} .

Multiplications can take years to complete

■ Algorithms that operate on n -bit inputs can be either:

- Naïve: run-time is proportional to the value of the n -bit inputs
- Good: run-time is proportional to n , the input's size.

Example I: multiplication

The "steps"

$$\begin{array}{r}
 1\ 0\ 1\ 1 = 1\ 1 \\
 1\ 0\ 1 = 5 \\
 \hline
 1\ 0\ 1\ 1 \\
 0\ 0\ 0\ 0 \\
 1\ 0\ 1\ 1 \\
 \hline
 1\ 1\ 0\ 1\ 1\ 1 = 5\ 5
 \end{array}$$

The algorithm explained (first 4 of 16 iteration)

x:	0	0	0	1	0	1	1	
y:	0	0	0	0	1	0	1	j^{th} bit of y
	0	0	0	1	0	1	1	1
	0	0	1	0	1	1	0	0
	0	1	0	1	1	0	0	1
	1	0	1	1	0	0	0	0
x·y:	0	1	1	0	1	1	1	sum

multiply(x, y):

// Where $x, y \geq 0$

sum = 0

shiftedX = *x*

for $j = 0 \dots (n-1)$ do

 if (j -th bit of *y*) = 1 then

sum = *sum* + *shiftedX*

shiftedX = *shiftedX* * 2

- Run-time: proportional to n
- Can be implemented in SW or HW
- Division: similar idea.

Example II: square root

The square root function has two convenient properties:

- It's inverse function is computed easily
- Monotonically increasing

Functions that have these two properties can be computed by binary search:

```
sqrt(x):
```

```
// Compute the integer part of  $y = \sqrt{x}$ . Strategy:  
// Find an integer  $y$  such that  $y^2 \leq x < (y+1)^2$  (for  $0 \leq x < 2^n$ )  
// By performing a binary search in the range  $0 \dots 2^{n/2} - 1$ .  
y = 0  
for j = n/2 - 1 ... 0 do  
    if  $(y + 2^j)^2 \leq x$  then  $y = y + 2^j$   
return y
```

Number of loop iterations is bounded by $n/2$, thus the run-time is $O(n)$.

Math operations (in the Jack OS)

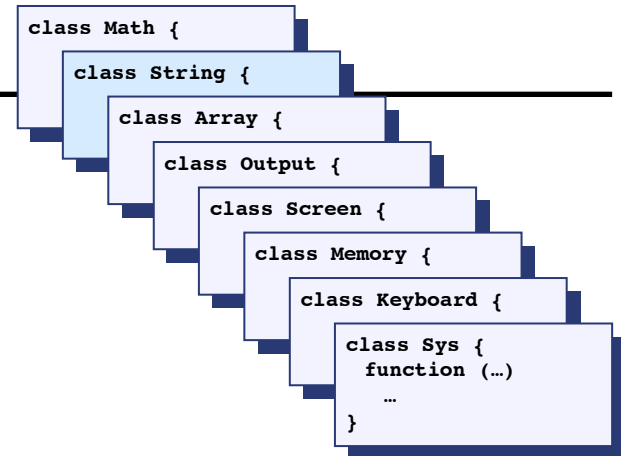
```
class Math {  
  
    function void init()  
  
    function int abs(int x)  
  
    ✓ function int multiply(int x, int y)  
    ✓ function int divide(int x, int y)  
  
    function int min(int x, int y)  
  
    function int max(int x, int y)  
  
    ✓ function int sqrt(int x)  
  
}
```

```
class Math {  
    class String {  
        class Array {  
            class Output {  
                class Screen {  
                    class Memory {  
                        class Keyboard {  
                            class Sys {  
                                function (...)  
                                ...  
                            }  
                        }  
                    }  
                }  
            }  
        }  
    }  
}
```

The remaining functions are simple to implement.

String processing (in the Jack OS)

```
Class String {  
  
    constructor String new(int maxLength)  
  
    method void    dispose()  
  
    method int     length()  
  
    method char    charAt(int j)  
  
    method void    setCharAt(int j, char c)  
  
    method String  appendChar(char c)  
  
    method void    eraseLastChar()  
  
    method int      intValue()  
  
    method void      setInt(int j)  
  
    function char  backSpace()  
  
    function char  doubleQuote()  
  
    function char  newLine()  
  
}
```



Single digit ASCII conversions

Character: '0' '1' '2' '3' '4' '5' '6' '7' '8' '9'

ASCII code: 48 49 50 51 52 53 54 55 56 57

- $\text{asciiCode}(\text{digit}) == \text{digit} + 48$
- $\text{digit}(\text{asciiCode}) == \text{asciiCode} - 48$

Converting a number to a string

- SingleDigit-to-character conversions: done
- Number-to-string conversions:

```
// Convert a non-negative number to a string
```

```
int2String(n):
```

```
    lastDigit = n % 10
```

```
    c = character representing lastDigit
```

```
    if n < 10
```

```
        return c (as a string)
```

```
    else
```

```
        return int2String(n / 10).append(c)
```

```
// Convert a string to a non-negative number
```

```
string2Int(s):
```

```
    v = 0
```

```
    for i = 1 ... length of s do
```

```
        d = integer value of the digit s[i]
```

```
        v = v * 10 + d
```

```
    return v
```

```
    // (Assuming that s[1] is the most
```

```
    // significant digit character of s.)
```

Memory management (in the Jack OS)

```
class Math {  
  class String {  
    class Array {  
      class Output {  
        class Screen {  
          class Memory {  
            class Keyboard {  
              class Sys {  
                function (...)  
                ...  
              }  
            }  
          }  
        }  
      }  
    }  
  }  
}
```

```
class Memory {  
  function int peek(int address)  
  
  function void poke(int address, int value)  
  
  function Array alloc(int size)  
  
  function void deAlloc(Array o)  
  
}
```


Memory management (naive)

- When a program constructs (deconstructs) an object, the OS has to allocate (de-allocate) a RAM block on the heap:
 - **alloc(size)**: returns a reference to a free RAM block of size **size**
 - **deAlloc(object)**: recycles the RAM block that **object** refers to

Initialization: *free = heapBase*

// Allocate a memory block of size words.

alloc(size):

pointer = free

free = free + size

return pointer

// De-allocate the memory space of a given object.

deAlloc(object):

do nothing

- The data structure that this algorithm manages is a single pointer: **free**.

Memory management (improved)

Initialization:

```
freeList = heapBase  
freeList.length = heapLength  
freeList.next = null
```

// Allocate a memory space of *size* words.

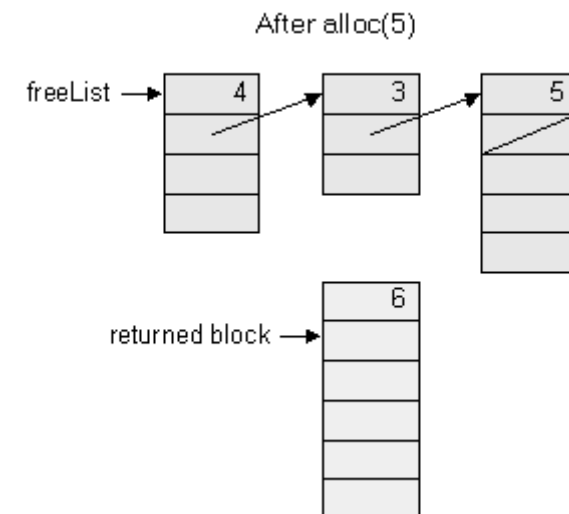
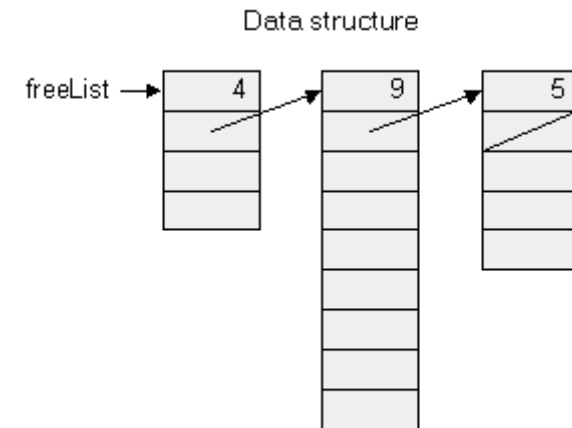
alloc(size):

```
Search freeList using best-fit or first-fit heuristics  
  to obtain a segment with segment.length > size  
If no such segment is found, return failure  
  (or attempt defragmentation)  
block = needed part of the found segment  
  (or all of it, if the segment remainder is too small)  
Update freeList to reflect the allocation  
block[-1] = size + 1 // Remember block size, for de-allocation  
Return block
```

// Deallocate a decommissioned *object*.

deAlloc(object):

```
segment = object - 1  
segment.length = object[-1]  
Insert segment into the freeList
```



Peek and poke

```
class Memory {  
    function int peek(int address)  
  
    function void poke(int address, int value)  
  
    function Array alloc(int size)  
  
    function void deAlloc(Array o)  
  
}
```

- Implementation: based on our ability to exploit exotic casting in Jack:

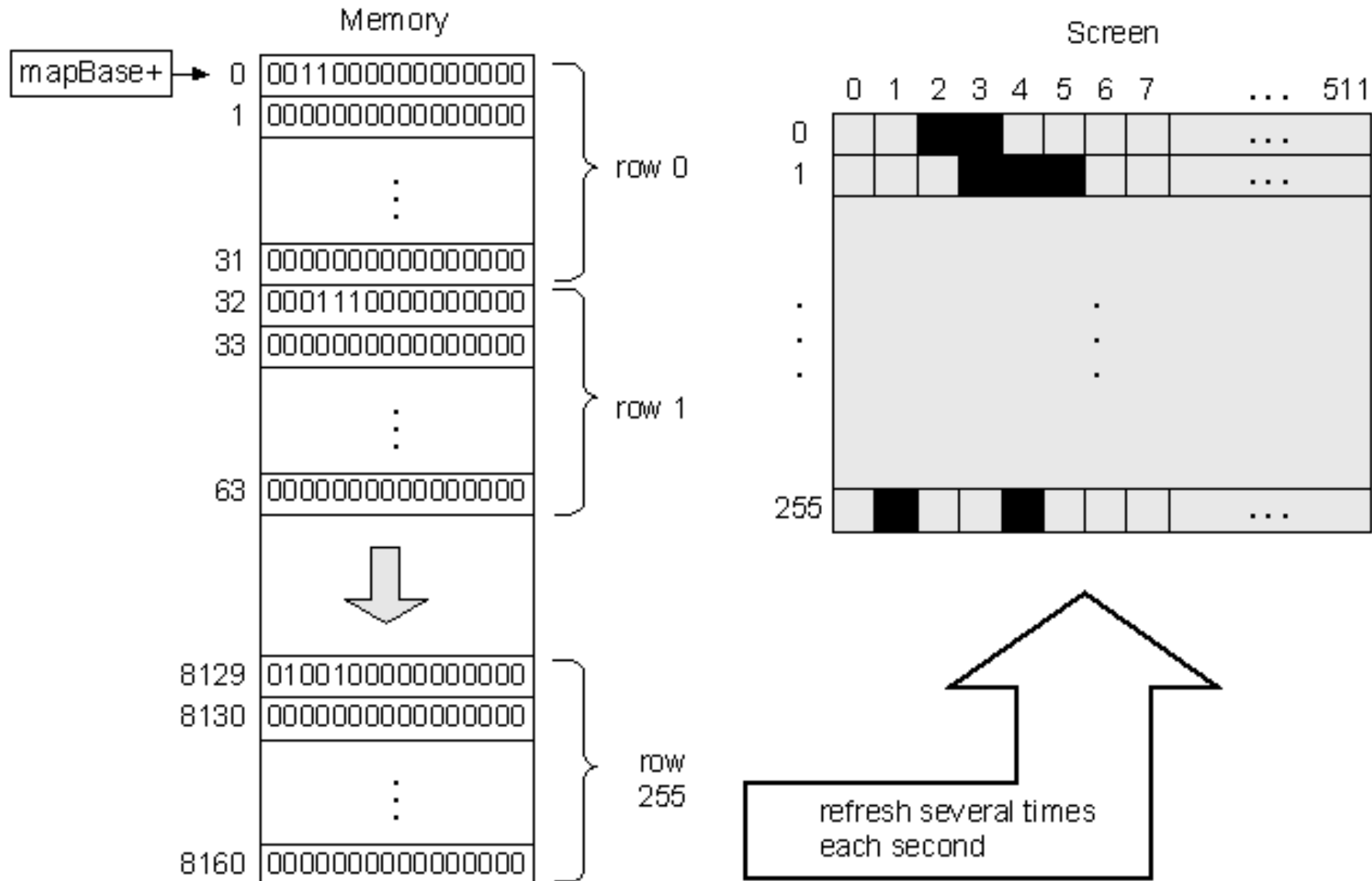
```
// To create a Jack-level "proxy" of the RAM:  
var Array memory;  
let memory = 0;  
// From this point on we can use code like:  
let x = memory[j] // Where j is any RAM address  
let memory[j] = y // Where j is any RAM address
```

Graphics primitives (in the Jack OS)

```
class Math {  
  ...  
}  
class String {  
  ...  
}  
class Array {  
  ...  
}  
class Output {  
  ...  
}  
class Screen {  
  ...  
}  
class Memory {  
  ...  
}  
class Keyboard {  
  ...  
}  
class Sys {  
  function (...)  
  ...  
}
```

```
Class Screen {  
  
  function void clearScreen()  
  
  function void setColor(boolean b)  
  
  function void drawPixel(int x, int y)  
  
  function void drawLine(int x1, int y1, int x2, int y2)  
  
  function void drawRectangle(int x1, int y1, int x2, int y2)  
  
  function void drawCircle(int x, int y, int r)  
  
}
```

Memory-mapped screen



Pixel drawing

```
drawPixel (x, y):
```

```
// Hardware-specific.
```

```
// Assuming a memory mapped screen:
```

```
Write a predetermined value in the RAM  
location corresponding to screen location (x, y).
```

■ Implementation: using `poke(address,value)`

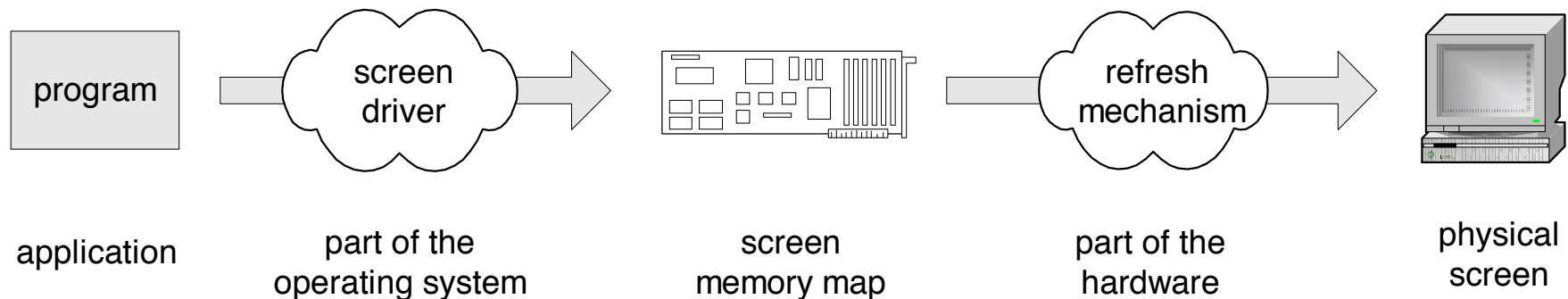
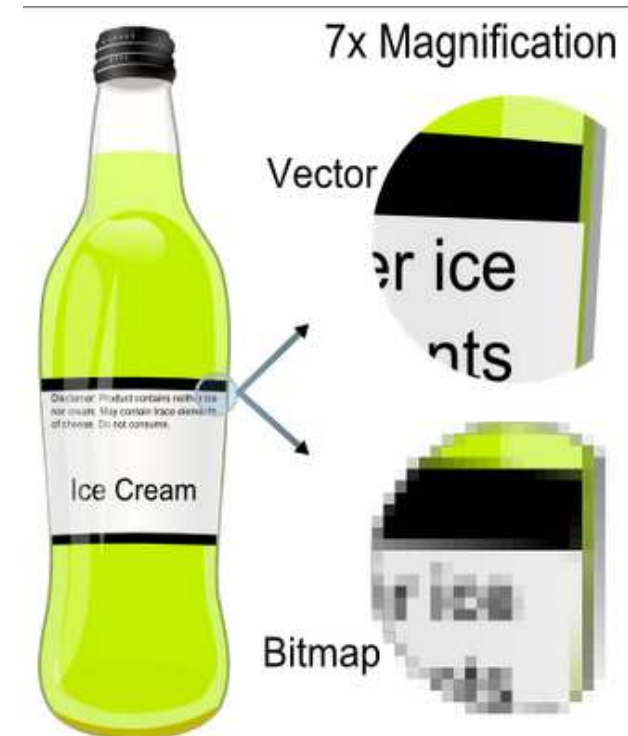
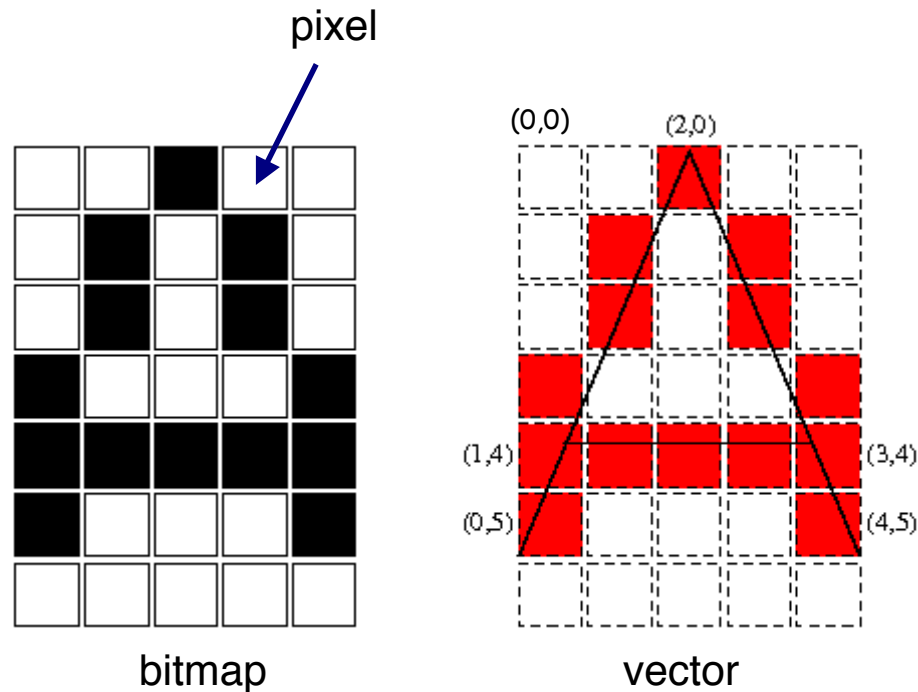
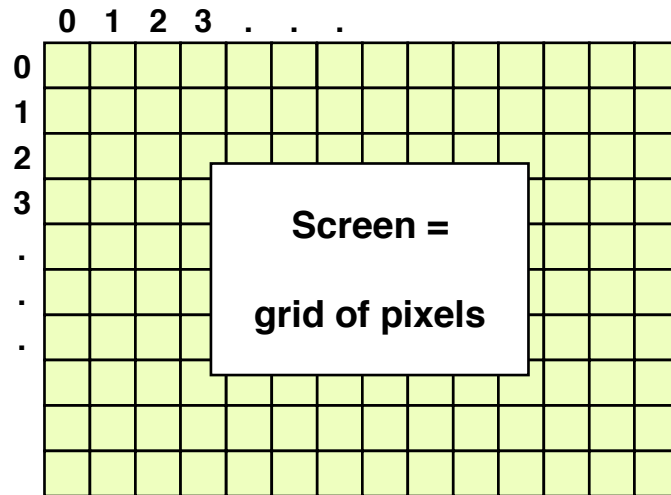


Image representation: bitmap versus vector graphics



- Bitmap file: 00100, 01010, 01010, 10001, 11111, 10001, 00000, . . .
- Vector graphics file: `drawLine(2,0,0,5)`, `drawLine(2,0,4,5)`, `drawLine(1,4,3,4)`
- Pros and cons of each method.

Vector graphics: basic operations



`drawPixel(x,y)` (Primitive operation)



`drawLine(x1,y1,x2,y2)`



`drawCircle(x,y,r)`

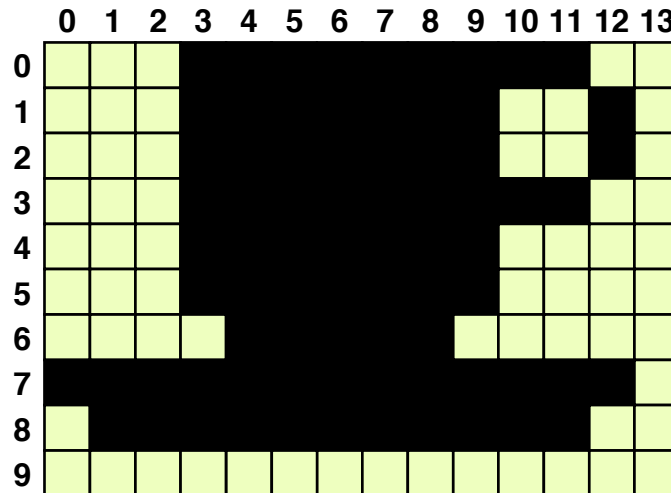


`drawRectangle(x1,y1,x2,y2)`



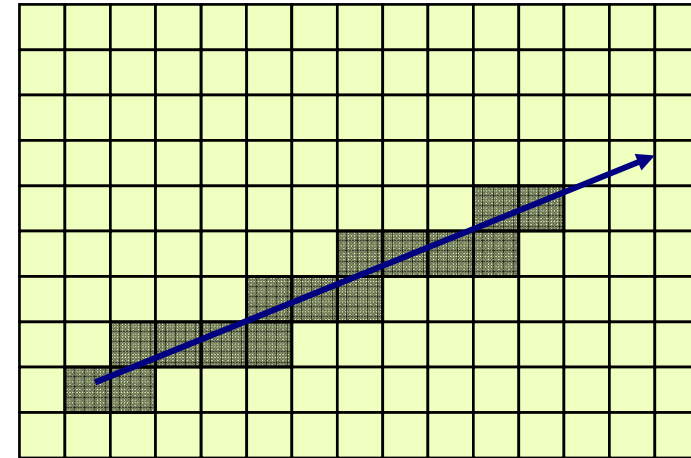
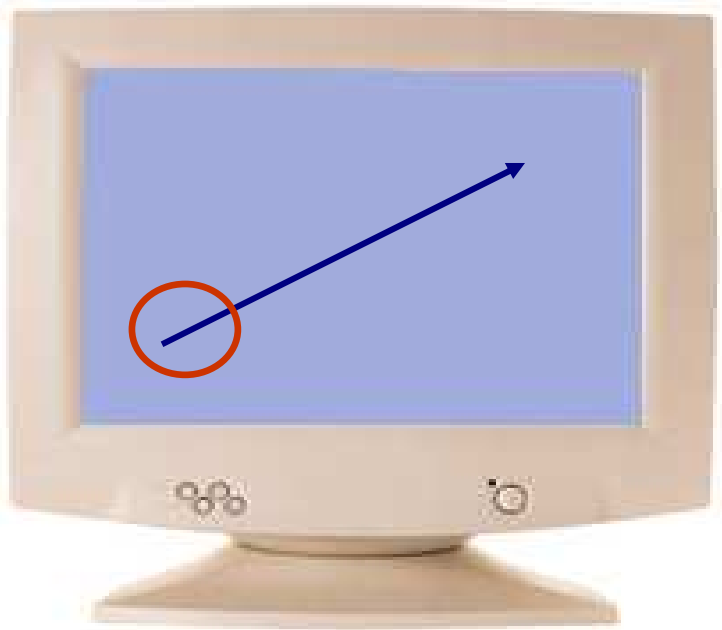
`drawTriangle(x1,y1,x2,y2,x3,y3)`

etc. (a few more similar operations)



```
drawLine(0,3,0,11)
drawRectangle(1,3,5,9)
drawLine(1,12,2,12)
drawLine(3,10,3,11)
drawLine(6,4,6,9)
drawLine(7,0,7,12)
drawLine(8,1,8,12)
```


How to draw a line?

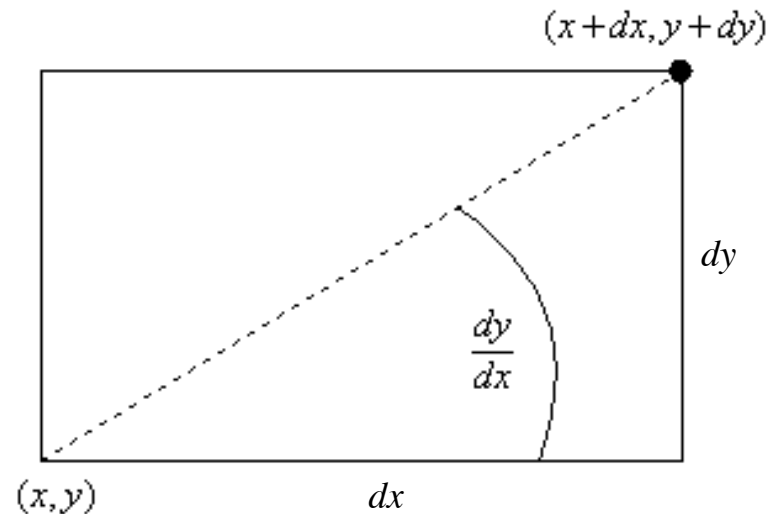


`drawLine(x1,y1,x2,y2)`

- Basic idea: `drawLine` is implemented through a sequence of `drawPixel` operations
- Challenge 1: which pixels should be drawn ?
- Challenge 2: how to draw the line *fast*?
- Simplifying assumption: the line that we are asked to draw goes north-east.

Line Drawing

- Given: `drawLine(x1,y1,x2,y2)`
- Notation: $x=x1$, $y=y1$, $dx=x2-x1$, $dy=y2-y1$
- Using the new notation:
We are asked to draw a line
between (x,y) and $(x+dx,y+dy)$



```
set (a,b) = (0,0)
```

```
while there is more work to do
```

```
    drawPixel(x+a,y+b)
```

```
    decide if you want to go right, or up
```

```
    if you decide to go right, set a=a+1;
```

```
    if you decide to go up, set b=b+1
```



```
set (a,b) = (0,0)
```

```
while (a ≤ dx) and (b ≤ dy)
```

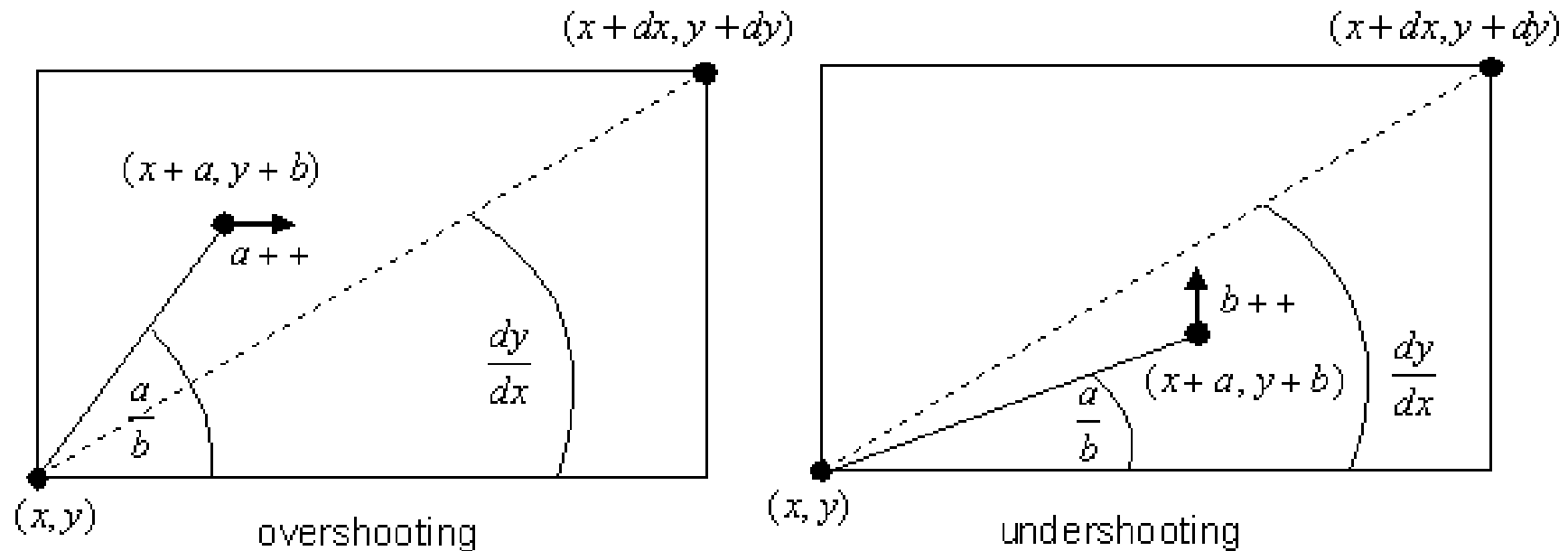
```
    drawPixel(x+a,y+b)
```

```
    decide if you want to go right, or up
```

```
    if you decide to go right, set a=a+1;
```

```
    if you decide to go up, set b=b+1
```

Line Drawing algorithm



drawLine(x,y,x+dx,y+dy)

set (a,b) = (0,0)

while (a ≤ dx) and (b ≤ dy)

drawPixel(x+a,y+b)

decide if you want to go right, or up

if you decide to go right, set a=a+1;

if you decide to go up, set b=b+1



drawLine(x,y,x+dx,y+dy)

set (a,b) = (0,0)

while (a ≤ dx) and (b ≤ dy)

drawPixel(x+a,y+b)

Oy
Vey

if $b/a > dy/dx$ set a=a+1
else set b=b+1

Line Drawing algorithm, optimized

```
drawLine(x,y,x+dx,y+dy)  
set (a,b) = (0,0)  
while (a ≤ dx) and (b ≤ dy)  
    drawPixel(x+a,y+b)  
    if  $b/a > dy/dx$  set a=a+1  
    else           set b=b+1
```



```
drawLine(x,y,x+dx,y+dy)  
set (a,b) = (0,0), diff = 0  
while (a ≤ dx) and (b ≤ dy)  
    drawPixel(x+a,y+b)  
    if diff < 0 set a=a+1, diff = diff + dx  
    else       set b=b+1, diff = diff - dy
```

Motivation

- When you draw polygons, e.g. in animation or video, you need to draw millions of lines
- Therefore, drawLine must be ultra fast
- Division is a very slow operation
- Addition is ultra fast (hardware based)

$b/a > dy/dx$ is the same as $a*dy < b*dx$

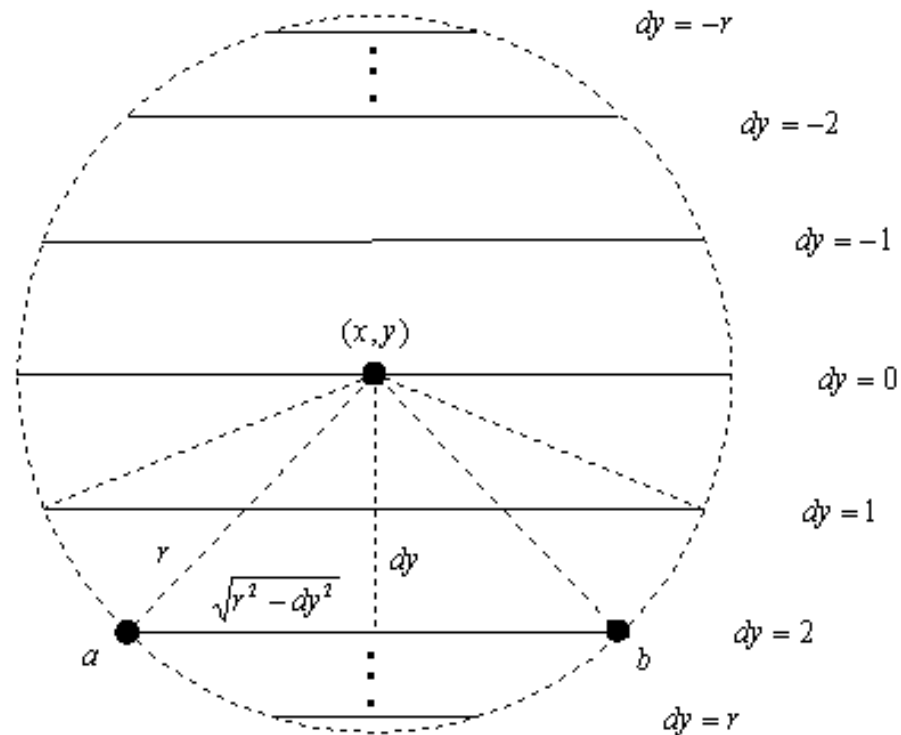
Define $diff = a*dy - b*dx$

Let's take a close look at this diff:

1. $b/a > dy/dx$ is the same as $diff < 0$
2. When we set $(a,b)=(0,0)$, $diff = 0$
3. When we set $a=a+1$, $diff$ goes up by dy
4. When we set $b=b+1$, $diff$ goes down by dx

Circle drawing

The screen origin (0,0) is at the top left.



$$\text{point } a = (x - \sqrt{r^2 - dy^2}, y + dy)$$

$$\text{point } b = (x + \sqrt{r^2 - dy^2}, y + dy)$$

drawCircle(x, y, r):

for each $dy \in -r \dots r$ do

drawLine from $(x - \sqrt{r^2 - dy^2}, y + dy)$ to $(x + \sqrt{r^2 - dy^2}, y + dy)$

An anecdote about efficiency and design

... Jobs obsessed about the look of what would appear on the screen. One day Bill Atkinson burst into his office all excited. He had just come up with a brilliant algorithm that could draw circles onscreen quickly. The math for making circles usually required calculating square roots, which the Motorola 68000 microprocessor didn't support. But Atkinson did a workaround based on the fact that the sum of a sequence of odd numbers produces a sequence of perfect squares (e.g. $1 + 3 = 4$, $1 + 3 + 5 = 9$, etc.)

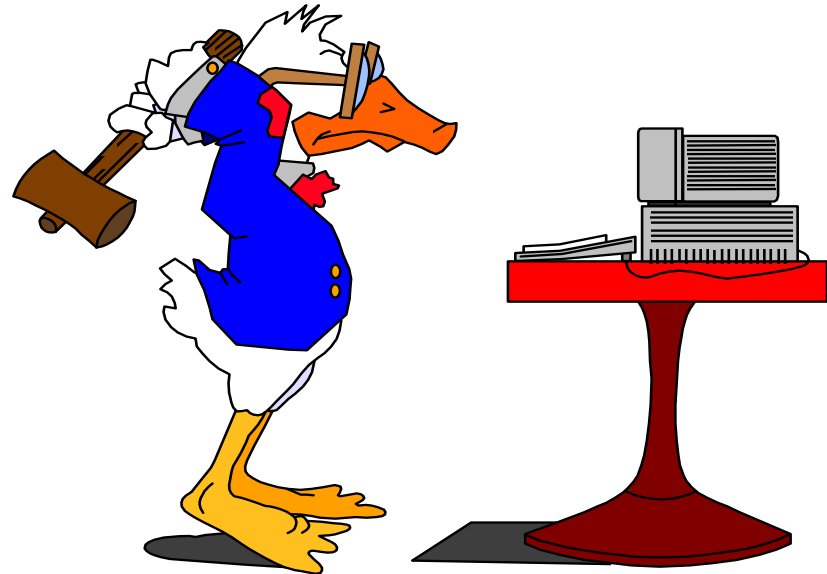
When Atkinson fired up his demo, everyone was impressed except Jobs. "Well, circles are nice," he said, "but how about drawing rectangles with rounded corners?"

(*Steve Jobs*, by Walter Isaacson, 2012)



To sum up (vector graphics)...

- To do vector graphics (e.g. display a PPT file), you have to draw polygons
- To draw polygons, you need to draw lines
- To draw lines, you need to divide
- Division can be re-expressed as multiplication
- Multiplication can be reduced to addition
- Addition is easy.



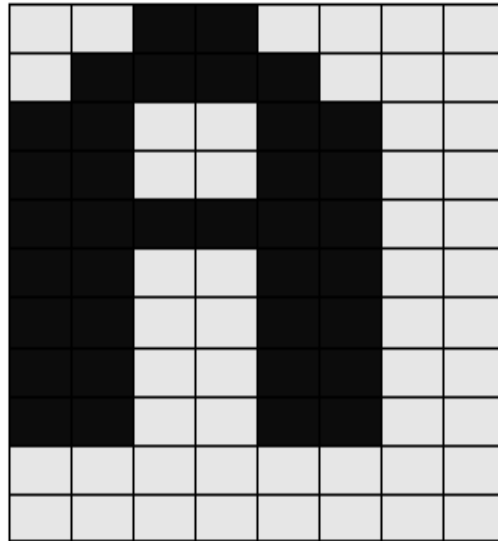
Character output primitives (in the Jack OS)

```
class Output {  
  
    function void moveCursor(int i, int j)  
  
    function void printChar(char c)  
  
    function void printString(String s)  
  
    function void printInt(int i)  
  
    function void println()  
  
    function void backSpace()  
  
}
```

```
class Math {  
    class String {  
        class Array {  
            class Output {  
                class Screen {  
                    class Memory {  
                        class Keyboard {  
                            class Sys {  
                                function (...)  
                                ...  
                            }  
                        }  
                    }  
                }  
            }  
        }  
    }  
}
```


Character output

- Given display: a physical screen, say 256 rows by 512 columns
- We can allocate an 11 by 8 grid for each character
- Hence, our output package should manage a 23 lines by 64 characters screen
- Font: each displayable character must have an agreed-upon bitmap
- In addition, we have to manage a "cursor".



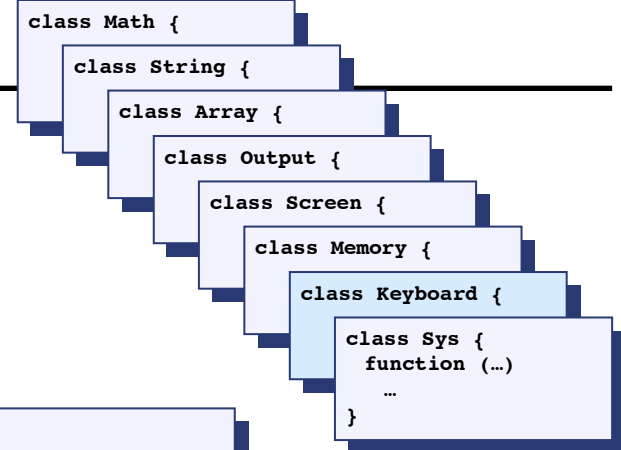
Font implementation (in the Jack OS)

```
class Output {
  static Array charMaps;
  function void initMap() {
    let charMaps = Array.new(127);
    // Assign a bitmap for each character
    do Output.create(32,0,0,0,0,0,0,0,0,0,0,0); // space
    do Output.create(33,12,30,30,30,12,12,0,12,12,0,0); // !
    do Output.create(34,54,54,20,0,0,0,0,0,0,0,0); // "
    do Output.create(35,0,18,18,63,18,18,63,18,18,0,0); // #
    ...
    do Output.create(48,12,30,51,51,51,51,51,30,12,0,0); // 0
    do Output.create(49,12,14,15,12,12,12,12,12,63,0,0); // 1
    do Output.create(50,30,51,48,24,12,6,3,51,63,0,0); // 2
    . . .
    do Output.create(65,0,0,0,0,0,0,0,0,0,0,0); // A ** TO BE FILLED **
    do Output.create(66,31,51,51,51,31,51,51,51,31,0,0); // B
    do Output.create(67,28,54,35,3,3,3,35,54,28,0,0); // C
    . . .
    return;
  }
}

// Creates a character map array
function void create(int index, int a, int b, int c, int d, int e,
                    int f, int g, int h, int i, int j, int k) {

  var Array map;
  let map = Array.new(11);
  let charMaps[index] = map;
  let map[0] = a;
  let map[1] = b;
  let map[2] = c;
  ...
  let map[10] = k;
  return; }
```

Keyboard primitives (in the Jack OS)



```
Class Keyboard {  
  
  function char keyPressed()  
  
  function char readChar()  
  
  function String readLine(String message)  
  
  function int readInt(String message)  
  
}
```

Keyboard input

```
keyPressed():
```

```
// Depends on the specifics of the keyboard interface  
if a key is presently pressed on the keyboard  
    return the ASCII value of the key  
else  
    return 0
```

- If the RAM address of the keyboard's memory map is known, the above logic can be implemented using a peek function
- Problem I: the elapsed time between a "key press" and key release" events is unpredictable
- Problem II: when pressing a key, the user should get some visible feedback (cursor, echo, ...).

A historic moment remembered

... Wozniak began writing the software that would get the microprocessor to display images on the screen. After a couple of month he was ready to test it. “I typed a few keys on the keyboard and I was shocked! The letters were displayed on the screen.”

It was Sunday, June 29, 1975, a milestone for the personal computer. “It was the first time in history,” Wozniak later said, “anyone had typed a character on a keyboard and seen it show up on their own computer’s screen right in front of them”

(*Steve Jobs*, by Walter Isaacson, 2012)



Keyboard input (cont.)

readChar():

```
// Read and echo a single character
display the cursor
while no key is pressed on the keyboard
    do nothing // wait till the user presses a key
c = code of currently pressed key
while a key is pressed
    do nothing // wait for the user to let go
print c at the current cursor location
move the cursor one position to the right
return c
```

readLine():

```
// Read and echo a "line" (until newline)
s = empty string
repeat
    c = readChar()
    if c = newline character
        print newline
        return s
    else if c = backspace character
        remove last character from s
        move the cursor 1 position back
    else
        s = s.append(c)
return s
```

Jack OS recap

Project 12:

Build it.

```
class Math {
```

```
  Class String {
```

```
    Class Array {
```

```
      class Output {
```

```
        Class Screen {
```

```
      }
```

```
        class Memory {
```

```
          Class Keyboard {
```

```
            Class Sys {
```

```
              function void halt():
```

```
              function void error(int errorCode)
```

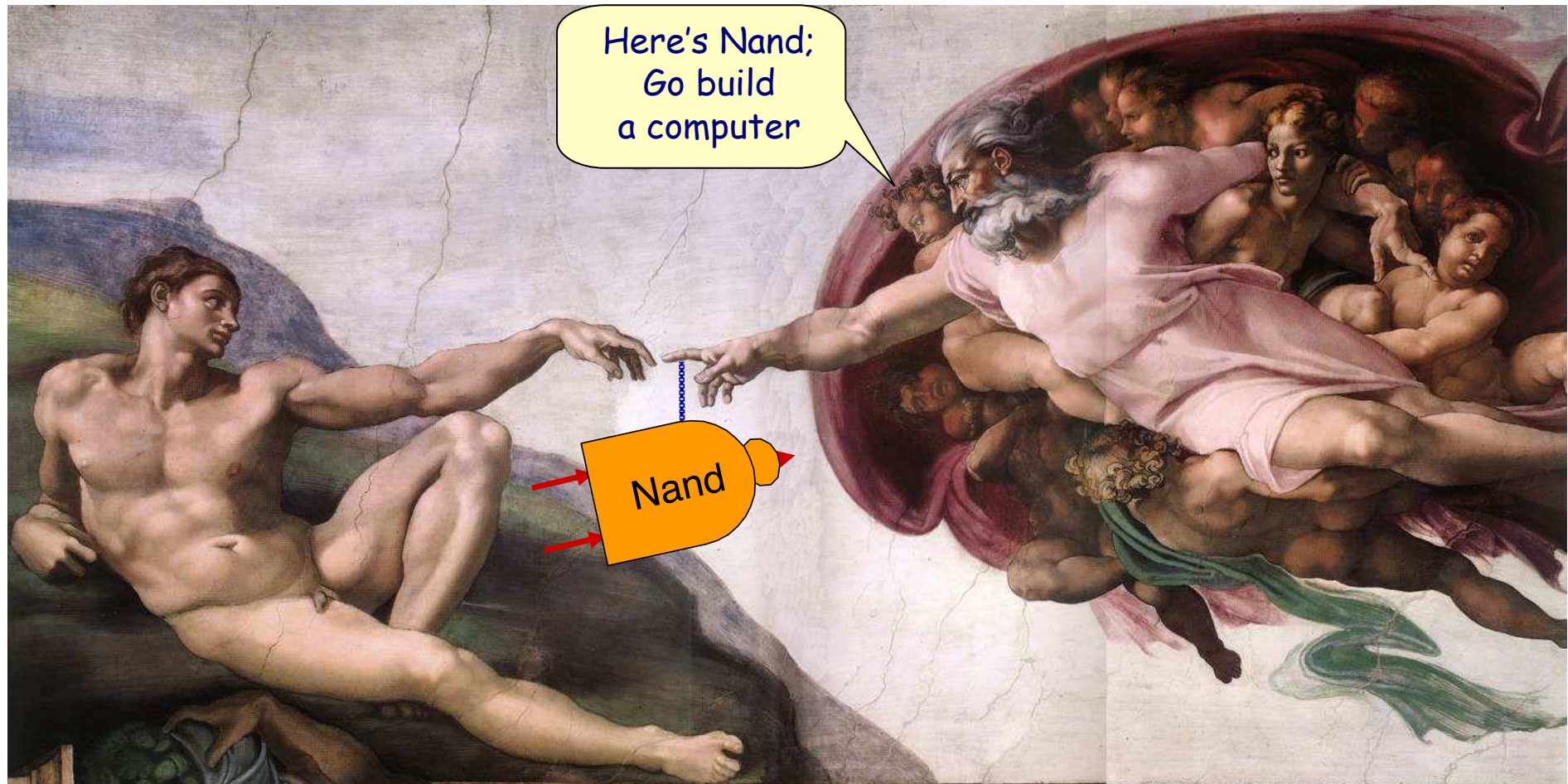
```
              function void wait(int duration)
```

```
            }
```

- Implementation: just like GNU Unix and Linux were built:
- Start with an existing system, and gradually replace it with a new system, one library at a time.

Perspective

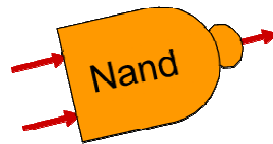
- What we presented can be described as a:
 - mini OS
 - Standard library
- Many classical OS functions are missing
- No separation between user mode and OS mode
- Some algorithms (e.g. multiplication and division) are standard
- Other algorithms (e.g. line- and circle-drawing) can be accelerated with special hardware
- And, by the way, we've just finished building the computer.



In CS, God gave us Nand
Everything else was done by humans.

Some Final notes

- CS is a science
- What is science?
- Reductionism
- Life science: From Aristo (millions of rules) to Darwin (3 rules) to Watson and Crick (1 rule)
- Computer science: We *knew* in advance that we could build a computer from almost nothing. In this course we actually did it.
- Key lessons:
 - Elegance
 - Clarity
 - Simplicity
 - Playfulness.



a	b	Out
0	0	1
0	1	1
1	0	1
1	1	0

