

Only lines of gcode with an X or Y need to be modified, all others can be ignored

Final format for a line should be G(x) X(x) Y(x) A(x) B(x) then possibly also Z(x) C(x) F(x)

Starting Points :  $X_0 = 0$  ,  $Y_0 = 0$  ,  $A_0 = 0$  ,  $B_0 = 0$  (The subscripts are just for identification purposes and will not be included in the final gcode)

Every  $X_n$  ,  $Y_n$  point will have a corresponding  $A_n$  ,  $B_n$  point, this means that every  $X_n$  ,  $Y_n$  to  $X_{n+1}$  ,  $Y_{n+1}$  line segment will also have a corresponding  $A_n$  ,  $B_n$  to  $A_{n+1}$  ,  $B_{n+1}$  line segment.

Any code starting points are just ideas and can be disregarded if there is a better way.

Current max straight line distance allowed between any  $X_n$  ,  $Y_n$  point and its corresponding  $A_n$  ,  $B_n$  point is 100mm. Anything less than this will be considered “close” and anything greater than this will be called “far”. The same goes for the distance from a current  $A_n$  ,  $B_n$  point to a future  $X_{n+m}$  ,  $Y_{n+m}$  point. Greater than 100mm will be “far” and less than 100mm will be “close”.

There are four main situations of moves for X and Y which will need to be accounted for:

1.  $A_n$  ,  $B_n$  to  $X_{n+1}$  ,  $Y_{n+1}$  > 100mm &  $X_{n+1}$  ,  $Y_{n+1}$  to  $X_{n+2}$  ,  $Y_{n+2}$  > 100mm
2.  $A_n$  ,  $B_n$  to  $X_{n+1}$  ,  $Y_{n+1}$  > 100mm &  $X_{n+1}$  ,  $Y_{n+1}$  to  $X_{n+2}$  ,  $Y_{n+2}$  < 100mm
3.  $A_n$  ,  $B_n$  to  $X_{n+1}$  ,  $Y_{n+1}$  < 100mm &  $X_{n+1}$  ,  $Y_{n+1}$  to  $X_{n+2}$  ,  $Y_{n+2}$  < 100mm  
&  $X_m$  ,  $Y_m$  to  $X_{m+1}$  ,  $Y_{m+1}$  < 100mm
4.  $A_n$  ,  $B_n$  to  $X_{n+1}$  ,  $Y_{n+1}$  < 100mm &  $X_{n+1}$  ,  $Y_{n+1}$  to  $X_{n+2}$  ,  $Y_{n+2}$  < 100mm  
&  $X_m$  ,  $Y_m$  to  $X_{m+1}$  ,  $Y_{m+1}$  > 100mm

For #1: “Cutting the corner” - Bisect the angle between the lines from  $X_n, Y_n$  to  $X_{n+1}, Y_{n+1}$  and  $X_{n+1}, Y_{n+1}$  to  $X_{n+2}, Y_{n+2}$ .  $A_{n+1}, B_{n+1}$  will then be placed 100mm from  $X_{n+1}, Y_{n+1}$  along the bisecting line.

Code starting point:

- from sympy.geometry import Point, Circle, Triangle
- p1, p2, p3 = Point( $X_n, Y_n$ ), Point( $X_{n+1}, Y_{n+1}$ ), Point( $X_{n+2}, Y_{n+2}$ )
- t = Triangle(p1, p2, p3)
- r = 100
- c = Circle(p2, r)
- p4 = c.intersection(t.bisectors())[p2]

$$p4 = A_{n+1}, B_{n+1}$$

For #2: Same as #1 but instead of  $A_{n+1}, B_{n+1}$  being 100mm from  $X_{n+1}, Y_{n+1}$  along the bisecting line it will need to be half the distance from  $X_{n+1}, Y_{n+1}$  to  $X_{n+2}, Y_{n+2}$  along the bisecting line.

Code starting point:

- from sympy.geometry import Point, Circle, Triangle, Line
- p1, p2, p3 = Point( $X_n, Y_n$ ), Point( $X_{n+1}, Y_{n+1}$ ), Point( $X_{n+2}, Y_{n+2}$ )
- t = Triangle(p1, p2, p3)
- l = Segment(p2, p3)
- r = (l.length)/2
- c = Circle(p2, r)
- p4 = c.intersection(t.bisectors())[p2]

$$p4 = A_{n+1}, B_{n+1}$$

For #3: When  $X_{n+1}, Y_{n+1}$  is close to  $A_n, B_n$  then the distance from  $A_n, B_n$  to all the following  $X, Y$  points will need to be calculated until one is found to be more than 100mm away. Call this point  $X_{m+1}, Y_{m+1}$  with the last point still within 100mm now called  $X_m, Y_m$ . The total distance traveled by the  $X, Y$  system will need to be calculated and added up between points  $X_n, Y_n$  and  $X_m, Y_m$ . Call this distance  $\Delta XY$  for now. If the distance from  $X_m, Y_m$  to  $X_{m+1}, Y_{m+1}$  is also less than 100mm then the midpoint between  $X_m, Y_m$  and  $X_{m-1}, Y_{m-1}$  will need to be calculated. Call this point  $A_m, B_m$ . The distance,  $\Delta AB$ , of the line from  $A_n, B_n$  to  $A_m, B_m$  will then need to be calculated. Next  $\Delta XY$  will need to be divided by  $\Delta AB$  to get the distance scaling factor. The length of the line segment from  $X_n, Y_n$  to  $X_{n+1}, Y_{n+1}$  will then be divided by this scaling factor to determine the length of line from  $A_n, B_n$  to  $A_{n+1}, B_{n+1}$  with  $A_{n+1}, B_{n+1}$  being placed that distance from  $A_n, B_n$  along the line to  $A_m, B_m$  which was determined earlier. At this point  $A_{n+1}, B_{n+1}$  and  $X_{n+1}, Y_{n+1}$  will now become the new  $A_n, B_n$  and  $X_n, Y_n$  and this whole process will be run again from the new starting points until reaching a point where  $X_{m+1}, Y_{m+1}$  is more than 100mm from  $X_m, Y_m$ .

Code starting point:

- Loop checking distance from  $A_n, B_n$  to  $X_{n+1}, Y_{n+1}$  is less than 100mm. This loop can also sum the  $X, Y$  distance traveled as it checks each point in order. Should probably also save the distance from  $X_n, Y_n$  to  $X_{n+1}, Y_{n+1}$  as its own variable since that number will be needed later.
- Once  $X_{m+1}, Y_{m+1}$  is found,  $A_m, B_m$  can be determined by finding the midpoint from  $X_m, Y_m$  and  $X_{m-1}, Y_{m-1}$  using:
  - from sympy.geometry import Point
  - p1, p2 = Point( $X_{m-1}, Y_{m-1}$ ), Point( $X_m, Y_m$ )

- $p1.midpoint(p2)$
- Divide the total  $X, Y$  by the segment from  $A_n, B_n$  to  $A_m, B_m$  then use that product to divide the segment from  $X_n, Y_n$  to  $X_{n+1}, Y_{n+1}$
- That length can then be used as the radius for a circle at point  $A_n, B_n$  and then intersected with the line from  $A_n, B_n$  to  $A_m, B_m$  to find  $A_{n+1}, B_{n+1}$

For #4: Everything about this one will be the same as #3 except that  $A_m, B_m$  will be placed at the “cutting the corner” location between  $X_m, Y_m$  and  $X_{m+1}, Y_{m+1}$ . The loop will then continue until  $A_{n+1}, B_{n+1}$  coincides with point  $A_m, B_m$ . This should result in either a #1 or #2 type of movement case.

All new  $A_{n+1}, B_{n+1}$  points will need to be checked to make sure they are still within 100mm of their corresponding  $X_{n+1}, Y_{n+1}$  point. If they are more than 100mm away then they will need to be moved along a straight line to 100mm away from  $X_{n+1}, Y_{n+1}$ . This would probably involve using the .intersection function of a 100mm radius circle centered at  $X_{n+1}, Y_{n+1}$  intersecting a line from  $X_{n+1}, Y_{n+1}$  to the current  $A_{n+1}, B_{n+1}$  to give the new  $A_{n+1}, B_{n+1}$  point.