

• [Tavas 2 Sadas] Codeforces lucky Number problem

- a lucky no is one which consists of only 4s and 7s.
- given a lucky no; calculate its index in the lucky no series.

eg series =

1	4	2 ¹	7	444	13	774
2	7		8	447	14	777
3	44	2 ²	9	474	2 ³	
4	47		10	477		
5	74		11	744		
6	77	12	747			

My approach -

• No. of ① digit numbers = 2¹

4 : ② digit numbers = 2²

4 : ③ digit numbers = 2³

so on

- if a number of digits 4 is given, then ~~minimum~~ index all these 1-digit, 2-digit and 3 digit numbers must be there.

because indexing starts from ① =

so, initially index = 2¹ + 2² + 2³ = 14

as i know

index of 1st digit number

1 1 1 1
8 4 2 2
→ ①

- example - (474) 2^4
initially index = $2^3 - 1 = 8 - 1 = 7$

- Then, update the index of the n-digit no among all n-digit numbers.

adding 1 initially compensates here

0	444	→	000	
1	447	→	001	
2	474	→	010	(2) 7 → 1
3	477	→	011	4 → 0
4	744	→	100	
5	747	→	101	
6	774	→	110	
7	777	→	111	

so index = $7 + 2 = 9$ // correct

example - 774
initially - index = $2^3 - 1 = 7$

$$774 \Rightarrow 110 \Rightarrow 6$$

$$7 + 6 = 13$$

Tip - ~~start~~ keep on getting the digits of the number from back and generate power of the index of digit

$$\text{index} = \begin{array}{ccc} 4 & 7 & 4 \\ 2 & 1 & 0 \end{array} \quad (2^1)$$

$$\begin{array}{r} 4747 \\ 3210 \end{array} \Rightarrow \text{index} = (2^4) + 2^0 + 2^2 = 15 + 1 + 4 = 20$$