Solving the Monty Hall Problem in R

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The Monty Hall problem

This classic probability puzzle is based loosely on Monty Hall's game show *Let's Make a Deal*. The problem as we know it now was made famous in 1990 as a reader's question to Marilyn vos Savant (of *Parade* magazine's "Ask Marilyn"). The reader framed the problem this way:

Suppose you're on a game show, and you're given the choice of three doors: Behind one door is a car; behind the others, goats. You pick a door, say No. 1, and the host, who knows what's behind the doors, opens another door, say No. 3, revealing a goat. He then says to you, "Do you want to pick door No. 2?" Is it to your advantage to switch your choice?

Marilyn's answer was simple: switch. Switching doubles the probability of winning the car: Pr[car|switch] = 0.666; Pr[car|stay] = 0.333. Her answer was not popular. The magazine received more than 10,000 letters insisting that vos Savant was wrong and a total fool for suggesting that the contestant switch. Marilyn's follow-up explanations and formal proofs were not enough to satisfy the most serious doubters. Notably, mathematician Paul Erös rejected Marilyn's answer until he was shown a computer simulation.

Your challenge

Write and execute a computer simulation to convince Marilyn's most skeptical readers that switching doors is the best solution to the Monty Hall problem. Code the routine using the R language. Then use R Markdown to communicate your findings by answering the questions below.

- 1. How did you program your simulation? Paste your well formatted code into your answers.
- 2. Present a table showing the number of simulated games won by the contestant who chose to switch and the number won by the contestant who stayed.
- 3. Now present the results graphically (e.g., with a bar chart).
- 4. Are your findings consistent with Marilyn's arguments? Is it better to switch? Explain.

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