Real-Time Scheduling Algorithms and Battery Consumption of Mobile Devices

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***Abstract*—One of the most increasing areas in application development is real time applications, as time goes by and technology develops more powerful devices the applications are now requested by users as real time applications, extended reality applications, and more complex applications such as online banking and more that requires more complex implementations every time. As much as we as users like these new applications and the new possibilities we have with them, there is always a concern regarding this kind of applications in mobile devices: the energy consumption. For this applications to run and perform as expected, a considerable amount of energy is needed, for these applications the constant communication with peers and/or main services is essential, and for that live interaction the device needs to spend more energy than a plain classic application, specifically for jobs that the processor executes periodically to keep the live interaction as expected. There are some approaches for this problem that involve designs of algorithms for scheduling these kind of jobs with the objective of saving energy, or at least spend it wisely. In this paper we discuss some of the algorithms that have been proposed to mitigate this issue and keep the user experience the best possible by using battery energy in a smart way but still guaranteeing a very good performance of real time applications.**

I. Introduction

NOWADAYS real-time applications are taking over mobile devices more than ever and, although this brings a lot of new opportunities, it brings challenges too. There is a plenty of examples of applications that includes collective, social, distributed and even virtual/augmented reality features out there and, it just a matter to take a look to a smartphone of an average user to see several of them in action. But, besides the success behind laptops and cell phones as the mobile devices, currently there are many other hardware architectures which has mobile capabilities as well and, in which the implementation of new and interactive applications have increased in recent years. Weareable technolgy and ARM architectures are good examples of this.

Thanks to hardware advances, both companies and users are pushing to provide and experience better applications on mobile devices but this still has big impact in its performance, particularly in battery conpsumption. Research groups have focused on optimizing the hardware of mobile devices, as well as their middleware increasing both the devices' uptime and the user satisfaction but the greater demand in performance for both mobile device hardware and its applications conflicts with the desire for longer battery life.

Users are craving for longer battery life, some even claim that the next big thing in technology ought be better batteries [8]. Taking as example mobile applications, a study conducted by [23] analyzed 9 millions user comments and 27,000 mobile applications under the Google Play store and demostrated that users of mobile applications are interested in enery-efficient applications and energy-inefficient applications lead to frustrated users to negative feedback and lower application ratings. Some other relevants results of the study revealed that: more than 18% of the analyzed applications have user feedback comprising comments on energy consumption problems, energy-efficiency issues negatively influence the grades users give for mobile apps in market places and that free apps do not have more energy consumption problems than payed apps.

The energy use of a typical laptop computer, smartphone and a tablet is dominated by the backlight and display, disks and CPU. They use a number of techniques to reduce the energy consumed by the disk and display, primarily by turning them off after a period of no use. Power consumed by the CPU is becoming more significant because of the type of the applications they run now: data-intensive, multimedia, games and collaborative applications that need to be in a constant sync with networks, sensors, and other devices. Dynamic voltage scaling (DVS) is a common mechanism to save CPU energy. It exploits an important characteristic or CMOS[1]-based processors: the maximun frequency scales almost linearly to the voltage, and the energy consumed per cycle is proportional to the square of the voltage. A lower frequency hence enables a lower voltage and yields a quadratic energy reduction [3]. The major goal of DVS is to reduce energy by as much as possible without degrading appplication performance. The efectiveness of DVS techniques is, therefore, dependent on the ability to predict application CPU demands – overestimating them can waste CPU and energy resources, while understimating them can degrade aplication performance [29].

A real-time operating system has a well-specified maximum time for each action that it performs to support applications with precise timing needs. Systems that can guarantee these

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[1]CMOS: Complementary metal–oxide–semiconductor

maximum times are called hard real-time systems. Those that meet these times most of the time are called soft real-time systems. Deploying an airbag in response to a sensor being actuated is a case where you would want a hard real-time system. On-line transaction systems, airline reservation systems and decoding video frames are examples of where a soft real-time system can be used.

In this paper, we introduce a set or real-time scheduling algorithms for hard real-time systems have been proposed to improve energy-saving for mobile devices. The rest of the paper is organized as follows. The paper begins pointing the differences between hard real-time and soft real-time systems in Section II. Then, we provide an introduction to real-time task scheduling algorithms in Section III. We focus our attention in *earliest deadline first* and *rate monotonic* algorithms because they have been proven to be the most popular algorithms for hard real-time systems [14]. In Section IV the basics of DVS algorithms are presented. Section III presents several variations of hard real-time and DVS algorithms that have been proposed that helps to improve battery performace. Results on Section VI measure how these algorithms behave under certain conditions. The paper is concluded in Section VIII.

II. Hard Real-Time versus Soft Real-Time Systems

The following are the major differences between hard and soft real-time systems according to [9].

a) Response time requirements: on hard real-time systems are in the order of milliseconds or less and can result in a catastrophe if not met. In contrast, the response time requirements of soft real-time systems are higher and not very strict.

b) Peak-load performance: in a hard real-time system, must be predictable and should not violate the predefined deadlines. In a soft real-time system, a degraded operation in a rarely occurring peak load can be tolerated.

c) Safety: a hard real-time system must remain synchronous with the state of the environment in all cases. On the other hand soft real-time systems will slow down their response time if the load is very high. Hard real-time systems are often safety critical.

d) Size of data files: hard real-time systems have small data files and real-time databases. Temporal accuracy is often the concern here. Soft real-time systems for example, on-line reservation systems have larger databases and require long-term integrity of real-time systems. If an error occurs in a soft real-time system, the computation is rolled back to a previously established checkpoint to initiate a recovery action. In hard real-time systems, roll-back/recovery is of limited use.

III. Real-Time Task Scheduling Algorithms

Several schemes of classification of real-time task scheduling algorithms exist. A scheme in [16] classifies the real-time task scheduling algorithms based on how the scheduling points (the points on time line at which the scheduler makes decisions regarding which task is to be run next) are defined. According to this classification scheme, the three main types of schedulers are: clock-driven, event-driven, and hybrid. The clock-driven schedulers are those in which the scheduling points are determined by the interrupts received from a clock. In the event-driven ones, the scheduling points are defined by certain events which precludes clock interrupts. The hybrid ones use both clock interrupts as well as event occurrences to define their scheduling points.

Important examples of event-driven schedulers are Earliest Deadline First (EDF) and Rate Monotonic analysis (RM). Event-driven schedulers are more sophisticated and usually more proficient and flexible than clock-driven schedulers. These are more proficient because they can feasibly schedule some task sets which clock-driven schedulers can not. These are more flexible because they can feasibly schedule sporadic and aperiodic tasks in addition to periodic tasks, whereas clock-driven schedulers can satisfactorily handle only periodic tasks [16]. Event-driven scheduling of real-time tasks was a subject of intense research during early 1970s, leading to the publication of a large number of research results, of which the following two popular algorithms are the essence of all EDF and RM [14].

A. Earliest Dealine First (EDF)

Every process tells the operating system scheduler its absolute time deadline. The scheduling algorithm simply allows the process that is in the greatest danger of missing its deadline to run first. Generally, this means that one process will run to completion if it has an earlier deadline than another. The only time a process would be preempted would be when a new process with an even shorter deadline becomes ready to run. To determine whether all the scheduled processes are capable of having their deadlines met, the following condition must hold:

$$\sum_{i=1}^{n} \frac{C_i}{P_1} \leq 1$$

This simply tells us sum of all the percentages of CPU time used per process has to be less than or equal to 100%.

B. Rate Monotonic (RM)

Rate monotonic analysis is a technique for assigning static priorities to periodic processes. As such, it is not a scheduler but a mechanism for governing the behavior of a preemptive priority scheduler. A conventional priority scheduler is used with this system, where the highest priority ready process will always get scheduled, preempting any lower priority processes.

A scheduler that is aware of rate monotonic scheduling would be provided with process timing parameters (period of execution) when the process is created and compute a suitable priority for the process. Most schedulers that support priority scheduling (e.g., Windows, Linux, Solaris, FreeBSD, NetBSD) do not perform rate monotonic analysis but only allow fixed priorities, so it is up to the user to assign proper priority levels for all real-time processes on the system. To do this properly, the user must be aware of all the real-time processes that will be running at any given time and each process' frequency of

execution ($1/T$, where T is the period). To determine whether all scheduled processes can have their real-time demands met, the system has to also know each process' compute needs per period (C) and check that the following condition holds:

$$\sum_{i=1}^{n} \frac{C_i}{P_1} < \ln 2$$

To assign a rate monotonic priority, one simply uses the frequency information for each process. If a process is an aperiodic process, the worst-case (fastest) frequency should be used. The highest frequency (smallest period) process gets the highest priority and successively lower frequency processes get lower priorities.

Scheduling is performed by a simple priority scheduler. At each quantum, the highest priority ready process gets to run. Processes at the same priority level run round-robin.

IV. DVS Algorithms

There are two kinds of voltage scheduling approaches for hard real-time systems depdending on the voltage scaling granularity: intra-task DVS and inter-task DVS. The intra-task DVS algorithms adjust the voltage within an individual task boundary, while the inter-task DVS algorithms determine the voltage on a task-by-task basis at each scheduling point. The main difference between them is whether the slack times are used for the current task or for the tasks that follow. Inter-task DVS algorithms distribute the slack times from the current task for the following tasks, while intra-task DVS algorithms use the slack times from the current task for the current task itself.

A. Intra-task DVS algorithms

In scheduling hard real-time tasks, in order to guarantee the timing constraint of each task, the execution times of tasks are usually assumed to be the worst case execution times (WCETs). However, since a task has many possible execution paths, there are large execution time variations among them. So, when the execution path taken at run time is not the worst case execution path (WCEP), the task may complete its execution before its WCET, resulting in a slack time. In that case, intra-task DVS exploits such slack times and adjusts the processor speed. Intra-task DVS algorithms can be classified into two types depending on how to estimate slack times and how to adjust speeds.

1) Path-based method: the voltage and clock speed are determined based on a predicted reference execution path, such as WCEP. For example, when the actual execution deviates from the predicted reference execution path, the clock speed is adjusted. If the new path takes significantly longer to complete its execution than the reference path, the clock speed is raised to meet the deadline constraint. On the other hand, if the new path can finish its execution earlier than the reference path, the clock speed is lowered to reduce the energy consumption. Program locations for possible speed scaling are identified using static program analysis [25] or execution time profiling [13].

2) Stochastic method: based on the idea that it is better to start the execution at a low speed and accelerate the execution later when needed than to start with a high speed and reduce the speed later when slack time is found. By starting at a low speed, if the task finishes earlier than its WCET, it does not need to execute at a high speed. Theoretically, if the probability density function of execution times of a task is known *a priori*, the optimal speed schedule can be computed [5]. Under the stochastic method, the clock speed is raised at specific time instances, regardless of the execution paths taken. The stochastic intra-task DVS may not utilize all the potential slack times.

B. Inter-task DVS algorithms

Inter-task DVS algorithms exploit the "run-calculate-assign-run" strategy to determine the supply voltage, which can be summarized as follows: (1) run a current task, (2) when the task is completed, calculate the maximum allowable execution time for the next task, (3) assign the supply voltage for the next task, and (4) run the next task. Most inter-task DVS algorithms differ during step (2) in computing the maximum allowed time for the next task τ which is the sum of WCET of τ and the slack time available for τ.

A generic inter-task DVS algorithm consists of two parts: slack estimation and slack distribution. The goal of the slack estimation part is to identify as much slack times as possible while the goal of the slack distribution part is to distribute the resulting slack times so that the resulting speed schedule is as uniform as possible. Slack times generally come from two sources; *static slack times* are the extra times available for the next task that can be identified statically, while dynamic slack times are caused from run-time variations of the task executions.

1) Slack estimation methods: Static slack estimation Maximum constant speed: One of the most commonly used static slack estimation methods is to compute the maximum constant speed, which is defined as the lowest possible clock speed that guarantees the feasible schedule of a task set [26]. For example, in EDF scheduling, if the worst case processor utilization (WCPU) U of a given task set is lower than 1.0 under the maximum speed f_{max}, the task set can be scheduled with a new maximum speed $f'_{max} = U \cdot f_{max}$. Although more complicated, the maximum constant speed can be statically calculated as well for RM scheduling [5], [26].

a) Dynamic slack estimation: Three widely-used techniques of estimating dynamic slack times are briefly described below.

Stretching to NTA: even though a given task set is scheduled with the maximum constant speed, since the actual execution times of tasks are usually much less than their WCETs, the tasks usually have dynamic slack times. One simple method to estimate the dynamic slack time is to use the arrival time of the next task [26]. (The arrival time of the next task is denoted by NTA.) Assume that the current task τ is scheduled at time t. If NTA of τ is later than $(t + \text{WCET}(\tau))$, task τ can be executed at a lower speed so that its execution completes exactly at the NTA.

Priority-based slack stealing: this method exploits the basic properties of priority-driven scheduling such as RM and EDF. The basic idea is that when a higher-priority task completes its execution earlier than its WCET, the following lower-priority tasks can use the slack time from the completed higher-priority task. It is also possible for a higher-priority task to utilize the slack times from completed lower-priority tasks. However, the latter type of slack stealing is computationally expensive to implement precisely. Therefore, the existing algorithms are based on heuristics [2], [10].

Utilization updating: the actual processor utilization during run time is usually lower than the worst case processor utilization. The utilization updating technique estimates the required processor performance at the current scheduling point by recalculating the expected worst case processor utilization using the actual execution times of completed task instances [17]. When the processor utilization is updated, the clock speed can be adjusted accordingly. The main merit of this method is its simple implementation, since only the processor utilization of completed task instances have to be updated at each scheduling point.

b) Slack distribution methods: In distributing slack times, most inter-task DVS algorithms have adopted a greedy approach, where all the slack times are given to the next activated task. This approach is not an optimal solution, but the greedy approach is widely used because of its simplicity.

V. Representative Algorithms

Many DVS algorithms have been proposed or developed, especially for hard real-time systems. Since lowering the supply voltage also decreases the maximum achievable clock speed, various DVS algorithms for hard real-time systems have the goal of reducing supply voltage dynamically to the lowest possible level while satisfying the tasks' timing constraints [11]. The following is a representative list of DVS algorithms that have been proposed for addressing energy efficiency on mobile devices: two of which are based on the RM scheduling policy, while the other algorithms are based on the EDF scheduling policy, the two most widely used real-time system models [14]. Two algorithms were selected for intra-task DVS, one from path-based intra-task DVS algorithms, and the other from stochastic methods.

- `lppsEDF` and `lppsRM` which were proposed in [26], slack time of a task is estimated using the maximum constant speed and Stretching-to-NTA methods.
- `ccRM` algorithm proposed [17] is similar to `lppsRM` in the sense that it uses both the maximum constant speed and the Stretching-to-NTA methods. However, while `lppsRM` can adjust the voltage and clock speed only when a single task is active, `ccRM` extends the stretching to NTA method to the case where multiple tasks are active.
- In [17], two other DVS algorithms are proposed, `ccEDF` and `laEDF`, for EDF scheduling policy. These algorithms estimate slack time of a task using the utilization updating method. While `ccEDF` adjusts the voltage and clock speed based on run-time variation in processor utilization alone, `laEDF` takes a more aggressive approach by estimating the amount of work required to be completed before NTA.
- `DRA` proposed in [2], is a representative DVS algorithm that are based on the priority-based slack stealing method. The algorithm estimates the slack time of a task using the priority-based slack stealing method along with the maximum constant speed and the Stretching-to-NTA methods.
- `AGR`, an extension of `DRA` proposed in [2] is intended for more aggressive slack estimation and voltage/clock scaling. In `AGR`, in addition to the priority-based slack stealing, more slack times are identified by computing the amount of work required to be completed before NTA.
- `lpSEH` in [10] is based on the priority-based slack stealing method. It extends the priority-based slack stealing method by adding a procedure that estimates the slack time from lower-priority tasks that were completed earlier than expected. `DRA`, `AGR`, and `lpSEH` algorithms are somewhat similar to one another in the sense that all of them use the maximum constant speed in the off-line phase and the Stretching-to-NTA method in the on-line phase in addition to the priority-based slack stealing method.
- `darEDF` in [30] is based on an efficient slack task scheduling scheme that employs dynamic speed setting slack in run queue. The algorithm uses a dynamic version of the average rate heuristic first and delays slack absorption, resulting in better battery performance.

Shin's intra-task DVS algorithm [25] and Gruian's algorithm [5] are used as representative intra-task DVS algorithms which use path-based method and the stochastic method, respectively.

VI. Results

In [11] a performance comparison of most of the algorithms presented in section V was made using a simulation environment named SimDVS. This work is relevant because it is argued that although each DVS algorithm is shown to be quite effective in reducing the energy/power consumption of a target system under its own experimental scenarios, these DVS algorithms have not been quantitatively evaluated under a unified framework, making it a difficult task for low-power embedded system developers to select an appropriate DVS algorithm for a given application/system.

a) Impact of the number of task on the energy consumption: as the number of tasks increases, the energy efficiency of `lppsEDF`, `lppsRM`, and `ccRM` that only use the Stretching-to-NTA technique do not significantly improve, while that of the other more aggressive inter-task DVS algorithms improves significantly when compared with the energy consumption of an applicacion running on a DVS-unaware system with a power-down mode only. In the Stretching-to-NTA method, the slack time that can be exploited is limited to the time between the completion of a task instance and the arrival time of the next task instance, which is largely independent of the number of tasks in the system. For the other inter-task DVS algorithms, since the slack times can be taken from any completed task instance, as the number of task increases, each task has more

slack sources and can be scheduled with a lowered clock speed.

b) Worst case processor utilization of task set: except for lppsEDF, the energy consumption of inter-task DVS algorithms increases as a linear function of WCPU of a task set. For lppsEDF, the energy consumption increases faster than a linear function of WCPU of a task set. This indirectly indicates that the dynamic slack estimation method of lppsEDF is not very effective. lppsEDF shows better energy efficiency than ccEDF when WCPU is less than 0.7. In ccEDF, the clock speed is determined using the actual processor utilization at the scheduling point. Since the actual processor utilization increases when a low-speed task instance completes its execution, the next task instance needs to be executed in a higher speed. Such voltage fluctuation occurs more often as the WCPU decreases. Thus, as the WCPU decreases, the energy efficiency of ccEDF becomes worse than that of lppsEDF. The results for lppsRM and ccRM are very similar to that of lppsEDF.

c) Speed bound: the energy efficiency of AGR and lpSEH is very close to the theoretical lower bound[2] when the speed bound factor is near 0.5. For the aggressive inter-task DVS algorithms, the energy efficiency is highest when the speed bound factor was set to average case processor utilization (ACPU). When the selected speed bound factor is close to ACPU ($= 0,55 \times$WCPU), the best energy effciency is achieved for laEDF. For ccEDF this trend does not hold. For RM inter-task DVS algorithms, the performance gap between the energy efficiency and that of the theoretical lower bound was roughly 35$\sim$40%.

Regarding the results of darEDF discussed in [30], the comparison with competing algorithms such as lppsEDF and lpSEH revelead that darEDF has the best performance both with respect to charge consumption and energy consumption, besides a lower runtime complexity than lpSEH wich has been proven to have close optimal energy saving according to [11].

A. Performance evaluation of Intra-Task DVS algorithms

The two representative intra-task DVS algorithms perform quite differently depending on available slack times. When the relative energy consumption ratio of intraGruian over intraShin was measured, if the ratio is larger than 1, intraGruian performs better than intraShin. When the slack ratio is less than 1.2, intraShin outperforms intraGruian because intraShin spends more time in the lower speed region than intraGruian. When the slack ratio is increased, intraGruian spends more time in the lower speed region than intraShin.

VII. Related Work

Although this work is focused in hard real-time scheduling algorithms, CPU scheduling and energy/power efficiency of soft real-time systems and mobile devices has been addressed as well. In [28] a framework to integrate DVS into soft real-time scheduling for open mobile systems is presented. Its goal is to achieve energy saving DVS while preserinf resource guarantees of soft real-time scheduling. In [29] an enery efficient soft real-time CPU scheduler intended for mobile multimedia systems named *GRACE-OS* is presented.

In [11] hybrid methods are discussed as well. By using this methods researchers try to answer quest of whether hybrid DVS algorithms will perform better than pure inter-task DVS or pure intra-task DVS. The study indicates that the performance of a HybridDVS algorithm can be better than a pure intra-task DVS algorithm or a pure inter-task DVS algorithm. However, the differences in energy efficiency depend on the characteristics of both the intra-task DVS and the inter-task DVS components used in the HybridDVS algorithm.

Another popular technique to reduce energy consumption of mobile devices is computation offloading in which an application reduce energy consumption by delegating code execution to other devices. Traditionally, computations are offloaded to remote servers. Selection of a proper offloading strategy can reduce power consumption and simultaneously enhance performance for mobile device. Following this technique, in [18] a computation offloading system for mobile devices named *Jade* is presented. *Jade* implements a multi-level task scheduling algorithm that enables energy and performance-aware task scheduling. It is built for mobile devices running Android operative system and it minimizes energy consumption of mobile devices through fine-grained computation offloading to the cloud. The algorithm (1) incorporates server status, (2) balances the workload between servers, and (3) offloads tasks to the most appropiate server according to the energy and computing demand of the task.

In [12] another offloading approach that combines the advantages of particioning mobile applications and in dynamically adaptin mobile execution targets in response to fluctuations in network conditions. The proposed approach is realized as the following two technical solutions: (1) a multitarget offloading program transformation that automatically rewrites a centralized program into a distributed program, whose local/remote distribution is determined dynamically at runtime; (2) a runtime system that determines the required local/remote distribution of the resulting distributed program based on the current execution environment. Combining these two solutions can effectively reduce the amount of energy consumed by mobile applications without having to change their source code by hand, thus optimizing them behind the scenes.

VIII. Conclusions

In this paper, real-time scheduling principles and algorithms and their impact on mobile device energy/power consumption are discussed. A high level introduction to the most popular hard real-time scheduling algorithms such as EDF and RM –according to the bibliography used as reference– are given and later we also introduced variations of these real-time algorithms in the context of Dynamic Voltage Scaling, which allows devices to bring good performace while having improved battery consumption.

According to the results, the efficiency of the algorithms vary depending of the impact of conditions such as number of

[2]Determined by the Yao's algorithm in [27]

tasks or worst case processor utilization, but even under those conditions improvements are experienced which maken them suitable for scenarios when energy concerns are required.

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