

task1 final version

April 29, 2020

```
In [6]: ### use generate_graph() to transform adjeceny matrix to graph
import numpy as np
from graph_tools import *
def generate_graph(AM):
    d = Graph(directed=False)
    d.add_vertex(len(AM)-1)
    for i in range(len(AM)):
        for j in range(i,len(AM)):
            if AM[i][j]==1:
                d.add_edge(i,j)
    return d

In [7]: generate_graph([[0, 0, 1, 1],[ 0 ,0,1, 1],[ 1, 1, 0, 0],[ 1, 1, 0, 0]])

Out[7]: // Generated by graph-tools (version 1.0) at 2020/17/04/29/20 16:17:44
// undirected, 4 vertices, 4 edges
graph export_dot {
    node [color=gray90,style=filled];
    "0";
    "1";
    "2";
    "3";
    "0" -- "2";
    "0" -- "3";
    "1" -- "2";
    "1" -- "3";
}

In [8]: ###get adjeceny matrix from user
def enter_adjMatrix():
    n = int(input("Enter number of rows(columns) in the matrix: "))
    matrix = []
    print("Enter the %s x %s matrix row by row: "% (n, n))
    for i in range(n):
        matrix.append(list(map(int, input().rstrip().split())))
    return matrix

In [9]: AM=enter_adjMatrix()
AM1=enter_adjMatrix()
```

Enter number of rows(columns) in the matrix: 4

Enter the 4 x 4 matrix row by row:

0 1 0 1

1 0 1 0

0 1 0 1

1 0 1 0

Enter number of rows(columns) in the matrix: 4

Enter the 4 x 4 matrix row by row:

0 0 1 1

0 0 1 1

1 1 0 0

1 1 0 0

```
In [10]: g0=generate_graph(AM)
         g0
```

```
Out[10]: // Generated by graph-tools (version 1.0) at 2020/18/04/29/20 16:18:35
// undirected, 4 vertices, 4 edges
graph export_dot {
    node [color=gray90,style=filled];
    "0";
    "1";
    "2";
    "3";
    "0" -- "1";
    "0" -- "3";
    "1" -- "2";
    "2" -- "3";
}
```

```
In [11]: g1=generate_graph(AM1)
         g1
```

```
Out[11]: // Generated by graph-tools (version 1.0) at 2020/18/04/29/20 16:18:35
// undirected, 4 vertices, 4 edges
graph export_dot {
    node [color=gray90,style=filled];
    "0";
    "1";
    "2";
    "3";
    "0" -- "2";
    "0" -- "3";
    "1" -- "2";
    "1" -- "3";
}
```

```
In [12]: def composite_permutation(p,g):
         g1=[0]*len(p)
```

```

s=min(g)
if len(p)==len(g):
    for i in range(len(p)):
        g1[i]=g[((p[i]-s)%len(p))]
    pass
    return g1
composite_permutation([0,1,3,2],[0,1,3,2])

```

Out [12]: [0, 1, 2, 3]

```

In [14]: ### apply permutation to the adjacency matrix by using apply_permute()
def apply_permut(AM,p):
    M=np.array(AM)
    s=min(p)
    for i in range(len(p)):
        p[i]=p[i]-s
    for i in range(len(p)):
        M[:,i] = M[p,i]
    for i in range(len(p)):
        M[i,:] = M[i,p]
    return M

```

```

In [15]: s=apply_permut(AM,[1,4,2,3])
s
generate_graph(s)

```

```

Out [15]: // Generated by graph-tools (version 1.0) at 2020/18/04/29/20 16:18:39
// undirected, 4 vertices, 4 edges
graph export_dot {
    node [color=gray90,style=filled];
    "0";
    "1";
    "2";
    "3";
    "0" -- "1";
    "0" -- "2";
    "1" -- "3";
    "2" -- "3";
}

```

```

In [16]: def apply_permut(AM,p):
    M=np.array(AM)
    M1=np.zeros([len(p),len(p)])
    #print(M)
    for i in range(len(p)):
        M1[:,i] = M[p[i],i]
    for i in range(len(p)):
        M1[i,:] = M[i,p]
    return M1

```

```
In [17]: apply_permut([[0, 1,0, 1],[ 1,0, 1,0],[0, 1,0, 1],[ 1,0, 1,0]], [0,3,1,2])
```

```
Out[17]: array([[0., 1., 1., 0.],
               [1., 0., 0., 1.],
               [0., 1., 1., 0.],
               [1., 0., 0., 1.]])
```

```
In [18]: ## check if two permutation produce the same graph using are_same()
```

```
def are_same(g0,g1):
    s=len(g0.vertices())
    q=len(g1.vertices())

    if s==q :
        if sorted(g0.edges())==sorted(g1.edges()):
            return True
        else:
            return False
    else :
        return False
```

```
In [19]: are_same(g0,g1)
```

```
Out[19]: False
```

```
In [20]: def tran_permu_to_graph(g):
          d = Graph(directed=False)
          d.add_vertex(len(g)-1)
          for i in range(len(g)):
              d.add_edge(g[(i)],g[(i+1)%len(g)])
          return d
```

```
In [21]: tran_permu_to_graph([0,3,1,2])
```

```
Out[21]: // Generated by graph-tools (version 1.0) at 2020/18/04/29/20 16:18:43
// undirected, 4 vertices, 4 edges
graph export_dot {
    node [color=gray90,style=filled];
    "0";
    "1";
    "2";
    "3";
    "0" -- "3";
    "0" -- "2";
    "1" -- "3";
    "1" -- "2";
}
```

```
In [22]: ### find the inverse of permutation using inv()
```

```
def inv(perm):
```

```

        s=min(perm)
        inverse = [0] * len(perm)
        for i, p in enumerate(perm):
            inverse[p-s] = i+s
        return inverse

In [23]: pi=[0,3,1,2]
        p=inv(pi)
        composite_permutation(p,[0,3,1,2])

Out[23]: [0, 1, 2, 3]

In [24]: ### transform the permutation to list of list using

def To_list(l):
    l1=[]
    for i in l:
        l1.append(list(i))
    return l1

In [42]: def graph_isomorphism(P,V):
        message_list=[]
        prover_move=True
        while len(message_list)<4:
            if prover_move :
                message_list=P(message_list)
            else :
                message_list=V(message_list)
            prover_move= not prover_move
            print(message_list[-1])
            if message_list[-1]== 'accept' or message_list[-1]== 'reject':
                return message_list
        return message_list

In [43]: import math
def honest_prover(AM,AM1,pi,mess_list):
    n=len(AM)
    sigma = np.random.permutation(range(0,n))
    if len(mess_list)==0:
        h=apply_permut(AM,sigma)
        H=generate_graph(h)
        mess_list.append(H)
    if len(mess_list)==2:
        ch=mess_list[1]
        if ch==0:
            mess_list.append(sigma)
        else:
            p=inv(pi)
            message_list.append(composite_permut(p,sigma))
    return mess_list

```

```
In [44]: def honest_verifier(AM,AM1,mess_list):
        if len(mess_list)==1:
            ch=random.choice(range(1))
            mess_list.append(ch)
        if len(mess_list)==3:
            phi=mess_list[2]
            H=mess_list[0]
            H0=apply_permut(AM,phi)
            H1=generate_graph(H0)
            r=are_same(H,H1)
            if r==True:
                mess_list.append('accept')
            else:
                mess_list.append('reject')

        return mess_list
```

```
In [45]: def test_isomorphism():
        # AM=enter_adjMatrix()
        # AM1=enter_adjMatrix()
        # pi=list(map(int, input('Enter pi:').split()))
        V=lambda msg: honest_verifier(AM,AM1,msg)
        P=lambda msg: honest_prover(AM,AM1,pi,msg)
        return graph_isomorphism(P,V)
```

```
In [46]: test_isomorphism()
```

```
// Generated by graph-tools (version 1.0) at 2020/06/04/29/20 17:06:06
```

```
// undirected, 4 vertices, 5 edges
```

```
graph export_dot {
    node [color=gray90,style=filled];
    "0";
    "1";
    "2";
    "3";
    "0" -- "1";
    "0" -- "2";
    "1" -- "3";
    "2" -- "2";
    "3" -- "3";
}
```

```
0
```

```
[1 3 0 2]
```

```
reject
```

```
/usr/lib/python3/dist-packages/ipykernel_launcher.py:11: FutureWarning: elementwise comparison
# This is added back by InteractiveShellApp.init_path()
```

```
Out[46]: [// Generated by graph-tools (version 1.0) at 2020/06/04/29/20 17:06:06
// undirected, 4 vertices, 5 edges
graph export_dot {
    node [color=gray90,style=filled];
    "0";
    "1";
    "2";
    "3";
    "0" -- "1";
    "0" -- "2";
    "1" -- "3";
    "2" -- "2";
    "3" -- "3";
}, 0, array([1, 3, 0, 2]), 'reject']
```

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In [ ]:
```

```
In [ ]:
```