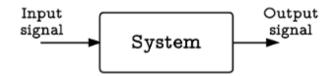
# Introduction to Digital Signal Processing Systems

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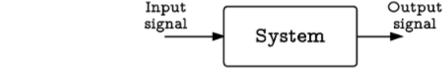
Department of Bioengineering Christian Medical College, Bagayam Vellore 632002 A collection of objects united by some form of interaction or interdependence<sup>1</sup>.

From the signal processing point of view, a system is any physical device or algorithm that performs some operation on a signal to transform it into another signal. B



<sup>&</sup>lt;sup>1</sup>Zadeh, Lotfi A., and Charles A. Deoser. *Linear system theory*. New York: McGraw Hill, 1963.

# What is a system?



Can be thought of a mapping function. e.g.

$$y[n] = \mathcal{H}\left(x[n]\right)$$

# Operations on signals

#### Operations on the dependent variable

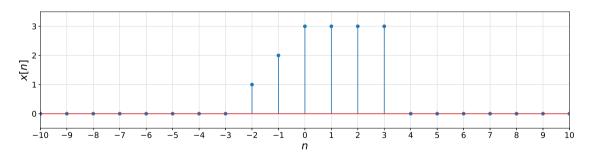
- ► Scaling:  $y[n] = a \cdot x[n]$
- ▶ **Addition**:  $y[n] = x_1[n] + x_2[n]$

#### Operations on the independent variable

- ▶ Time shifting:  $y[n] = x[n-k], k \in \mathbb{Z}$
- ▶ Time reversal:  $y[n] = x[-n], k \in \mathbb{Z}$

## Operation on the independent variable: **Time shifting**

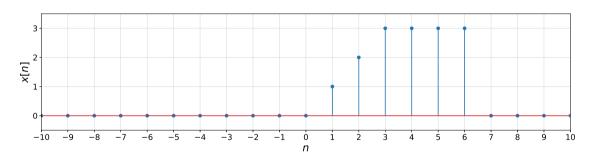
Consider  $x\left[ n\right]$  shown below,



What does x [n-3] look like?

# Operation on the independent variable: Time shifting

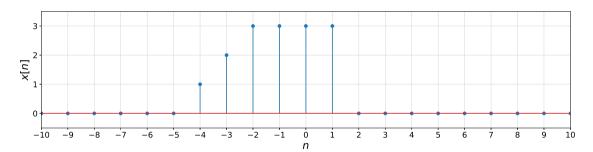
$$x[n-3]$$



What about x [n+2]?

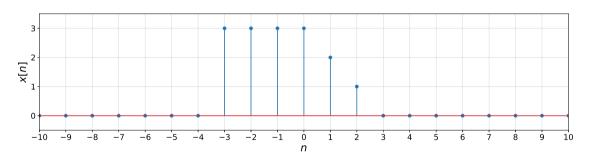
# Operation on the independent variable: Time shifting

$$x[n+2]$$



#### Operation on the independent variable: **Time reversal**

$$x[-n]$$



And x[-n]?

Based on the properties of the system.

► Linearity: satisfies the properties of scaling and superposition. Let us assume,

$$\mathcal{H}: x_i[n] \mapsto y_i[n]$$

The system  ${\cal H}$  is linear, if and only if,

$$\mathcal{H}: \sum_{i} a_{i} x_{i} [n] \mapsto \sum_{i} a_{i} y_{i} [n]$$

Which of these systems are linear?

1. 
$$y[n] = k_1 x[n] + k_2 x[t-2]$$

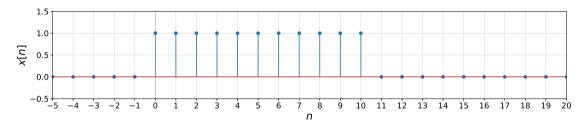
2. 
$$y[n] = \sum_{k=n-N}^{n} x[k]$$

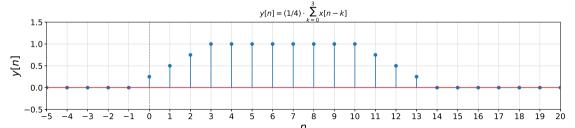
3. 
$$y[n] = 0.5x[n] + 1.5$$

► Memory: a system whose output depends on past or future values of its input is a system with memory, else the system is memoryless.

Note: the system may or may not depends on its present.

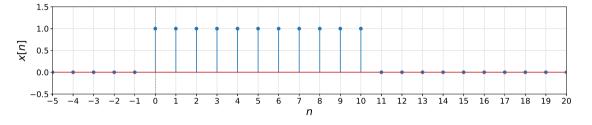
$$\begin{cases} y\left[n\right] = 0.5x\left[n\right] & \text{Memoryless system} \\ y\left[n\right] = \sum_{k=m_1}^{m_2} x\left[n-k\right] & \text{System with memory} \end{cases}$$

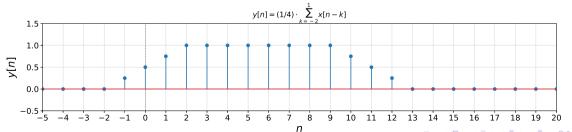




► Causality: a system whose output depends on the past and present only values of the input is a causal system.

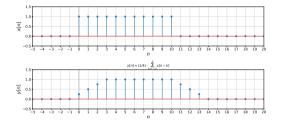
#### Causality

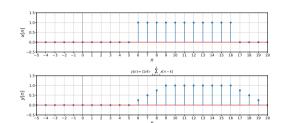


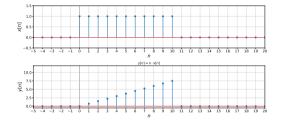


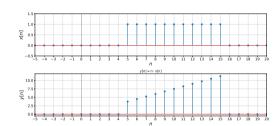
► Time invariance: system remains the same with time. If a system is time-invariant, then

$$\mathcal{H}: x[n] \mapsto y[n] \iff f: x[n-k] \mapsto y[n-k]$$









**Stability**: bounded input produces bounded output.

$$|x[n]| < M_x < \infty \mapsto |y[n]| < M_y < \infty$$