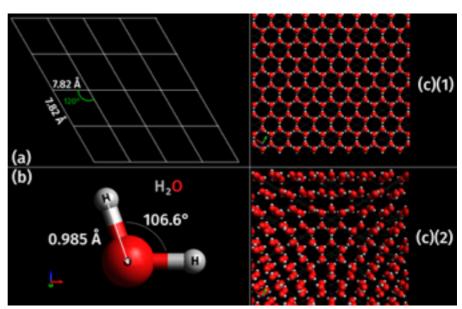
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Crystal structure

In <u>crystallography</u>, **crystal structure** is a description of the ordered arrangement of <u>atoms</u>, <u>ions</u> or <u>molecules</u> in a <u>crystalline material</u>.^[3] Ordered structures occur from the intrinsic nature of the constituent particles to form symmetric patterns that repeat along the principal directions of <u>three-dimensional space</u> in matter.

The smallest group of particles in the material that constitutes the repeating pattern is the **unit cell** of the structure. The unit cell completely defines the symmetry and structure of the entire crystal lattice, which is built up by repetitive <u>translation</u> of the unit cell along its principal axes. The repeating patterns are said to be located at the points of the <u>Bravais</u> lattice.



The (3-D) crystal structure of H_2O ice Ih (c) consists of bases of H_2O ice molecules (b) located on lattice points within the (2-D) hexagonal space lattice (a). The values for the H–O–H angle and O–H distance have come from *Physics of Ice*^[1] with uncertainties of $\pm 1.5^{\circ}$ and ± 0.005 Å, respectively. The white box in (c) is the unit cell defined by Bernal and Fowler^[2]

The lengths of the principal axes, or edges, of the unit cell and the angles between them are the <u>lattice constants</u>, also called *lattice parameters*. The <u>symmetry</u> properties of the crystal are described by the concept of <u>space groups</u>.^[3] All possible symmetric arrangements of particles in three-dimensional space may be described by the 230 space groups.

The crystal structure and symmetry play a critical role in determining many physical properties, such as <u>cleavage</u>, <u>electronic band structure</u>, and <u>optical transparency</u>.

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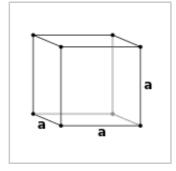
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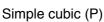
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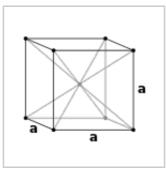
External links

Unit cell

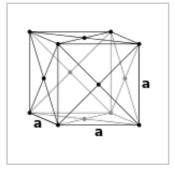
Crystal structure is described in terms of the geometry of arrangement of particles in the unit cell. The unit cell is defined as the smallest repeating unit having the full symmetry of the crystal structure. The geometry of the unit cell is defined as a parallelepiped, providing six lattice parameters taken as the lengths of the cell edges (a, b, c) and the angles between them (α, β, γ) . The positions of particles inside the unit cell are described by the <u>fractional coordinates</u> (x_i, y_i, z_i) along the cell edges, measured from a reference point. It is only necessary to report the coordinates of a smallest asymmetric subset of particles. This group of particles may be chosen so that it occupies the smallest physical space, which means that not all particles need to be physically located inside the boundaries given by the lattice parameters. All other particles of the unit cell are generated by the symmetry operations that characterize the symmetry of the unit cell. The collection of symmetry operations of the unit cell is expressed formally as the <u>space</u> group of the crystal structure. [5]







Body-centered cubic (I)



Face-centered cubic (F)

Miller indices

Vectors and planes in a crystal lattice are described by the three-value Miller index notation. This syntax uses the indices ℓ , m, and n as directional orthogonal parameters, which are separated by 90° . [6]

By definition, the syntax (ℓmn) denotes a plane that intercepts the three points a_1/ℓ , a_2/m , and a_3/n , or some multiple thereof. That is, the Miller indices are proportional to the inverses of the intercepts of the plane with the unit cell (in

the basis of the lattice vectors). If one or more of the indices is zero, it means that the planes do not intersect that axis (i.e., the intercept is "at infinity"). A plane containing a coordinate axis is translated so that it no longer contains that axis before its Miller indices are determined. The Miller indices for a plane are <u>integers</u> with no common factors. Negative indices are indicated with horizontal bars, as in (123). In an orthogonal coordinate system for a cubic cell, the Miller indices of a plane are the Cartesian components of a vector normal to the plane.

Considering only (ℓ mn) planes intersecting one or more lattice points (the *lattice planes*), the distance d between adjacent lattice planes is related to the (shortest) <u>reciprocal lattice</u> vector orthogonal to the planes by the formula

$$d=rac{2\pi}{|\mathbf{g}_{\ell mn}|}$$

Planes with different Miller indices in cubic crystals

Planes and directions

The crystallographic directions are geometric <u>lines</u> linking nodes (<u>atoms</u>, <u>ions</u> or <u>molecules</u>) of a crystal. Likewise, the crystallographic <u>planes</u> are geometric *planes* linking nodes. Some directions and planes have a higher density of nodes. These high density planes have an influence on the behavior of the crystal as follows:^[3]

- Optical properties: Refractive index is directly related to density (or periodic density fluctuations).
- Adsorption and reactivity: Physical adsorption and chemical reactions occur at or near surface atoms or molecules. These phenomena are thus sensitive to the density of nodes.
- Surface tension: The condensation of a material means that the atoms, ions or molecules are more stable if they
 are surrounded by other similar species. The surface tension of an interface thus varies according to the density
 on the surface.
- Microstructural <u>defects</u>: <u>Pores</u> and <u>crystallites</u> tend to have straight grain boundaries following higher density planes.
- Cleavage: This typically occurs preferentially parallel to higher density planes.
- Plastic deformation: <u>Dislocation</u> glide occurs preferentially parallel to higher density planes. The perturbation carried by the dislocation (<u>Burgers vector</u>) is along a dense direction. The shift of one node in a more dense direction requires a lesser distortion of the crystal lattice.

Some directions and planes are defined by symmetry of the crystal system. In monoclinic, rhombohedral, tetragonal, and trigonal/hexagonal systems there is one unique axis (sometimes called the **principal axis**) which has higher rotational symmetry than the other two axes. The **basal plane** is the plane perpendicular to the principal axis in these crystal systems. For triclinic, orthorhombic, and cubic crystal systems the axis designation is arbitrary and there is no principal axis.

Cubic structures

For the special case of simple cubic crystals, the lattice vectors are orthogonal and of equal length (usually denoted a); similarly for the reciprocal lattice. So, in this common case, the Miller indices (ℓmn) and [ℓmn] both simply denote normals/directions in <u>Cartesian coordinates</u>. For cubic crystals with <u>lattice constant</u> a, the spacing d between adjacent (ℓmn) lattice planes is (from above):

$$d_{\ell mn} = rac{a}{\sqrt{\ell^2 + m^2 + n^2}}$$

Because of the symmetry of cubic crystals, it is possible to change the place and sign of the integers and have equivalent directions and planes:

- Coordinates in angle brackets such as (100) denote a family of directions that are equivalent due to symmetry operations, such as [100], [010], [001] or the negative of any of those directions.
- Coordinates in curly brackets or braces such as {100} denote a family of plane normals that are equivalent due to symmetry operations, much the way angle brackets denote a family of directions.

For <u>face-centered cubic</u> (fcc) and <u>body-centered cubic</u> (bcc) lattices, the primitive lattice vectors are not orthogonal. However, in these cases the Miller indices are conventionally defined relative to the lattice vectors of the cubic <u>supercell</u> and hence are again simply the <u>Cartesian</u> directions.

Interplanar spacing

The spacing d between adjacent (hkl) lattice planes is given by:^[7]

Cubic:

$$\frac{1}{d^2} = \frac{h^2 + k^2 + l^2}{a^2}$$

Dense crystallographic planes

Tetragonal:

$$rac{1}{d^2} = rac{h^2 + k^2}{a^2} + rac{l^2}{c^2}$$

Hexagonal:

$$rac{1}{d^2} = rac{4}{3} \left(rac{h^2 + hk + k^2}{a^2}
ight) + rac{l^2}{c^2}$$

Rhombohedral:

$$rac{1}{d^2} = rac{(h^2 + k^2 + l^2) \sin^2 lpha + 2(hk + kl + hl)(\cos^2 lpha - \cos lpha)}{a^2 (1 - 3 \cos^2 lpha + 2 \cos^3 lpha)}$$

Orthorhombic:

$$rac{1}{d^2} = rac{h^2}{a^2} + rac{k^2}{b^2} + rac{l^2}{c^2}$$

Monoclinic:

$$rac{1}{d^2}=\left(rac{h^2}{a^2}+rac{k^2\sin^2eta}{b^2}+rac{l^2}{c^2}-rac{2hl\coseta}{ac}
ight)\csc^2eta$$

Triclinic:

$$\frac{1}{d^2} = \frac{\frac{h^2}{a^2}\sin^2\alpha + \frac{k^2}{b^2}\sin^2\beta + \frac{l^2}{c^2}\sin^2\gamma + \frac{2kl}{bc}\cos\alpha + \frac{2hl}{ac}\cos\beta + \frac{2hk}{ab}\cos\gamma}{1 - \cos^2\alpha - \cos^2\beta - \cos^2\gamma + 2\cos\alpha\cos\beta\cos\gamma}$$

Classification by symmetry

The defining property of a crystal is its inherent symmetry, by which we mean that under certain 'operations' the crystal remains unchanged. All crystals have translational symmetry in three directions, but some have other symmetry elements as well. For example, rotating the crystal 180° about a certain axis may result in an atomic configuration that is identical to the original configuration. The crystal is then said to have a twofold rotational symmetry about this axis. In addition to rotational symmetries like this, a crystal may have symmetries in the form of mirror planes and translational symmetries, and also the so-called "compound symmetries," which are a combination of translation and rotation/mirror symmetries. A full classification of a crystal is achieved when all of these inherent symmetries of the crystal are identified. [8]

Lattice systems

These <u>lattice systems</u> are a grouping of crystal structures according to the axial system used to describe their lattice. Each lattice system consists of a set of three axes in a particular geometric arrangement. There are seven lattice systems. They are similar to but not quite the same as the seven crystal systems.

Crystal	Lattice system	Schönflies	14 Bravais Lattices				
family			Primitive	Base- centered	Body- centered	Face- centered	
<u>triclinic</u>		Ci	a a B				
monoclinic		C _{2h}	$\beta \neq 90^{\circ}$ $a \neq c$ b	$\beta \neq 90^{\circ}$ $a \neq c$ b			
orthorhombic		D _{2h}					
tetragonal		D _{4h}					
<u>hexagonal</u>	rhombohedral	D _{3d}					
	hexagonal	D _{6h}					
<u>cubic</u>		O _h					

The simplest and most symmetric, the <u>cubic</u> (or isometric) system, has the symmetry of a <u>cube</u>, that is, it exhibits four threefold rotational axes oriented at 109.5° (the <u>tetrahedral angle</u>) with respect to each other. These threefold axes lie along the body diagonals of the cube. The other six lattice systems, are <u>hexagonal</u>, <u>tetragonal</u>, <u>rhombohedral</u> (often confused with the trigonal crystal system), orthorhombic, monoclinic and triclinic.

Bravais lattices

Bravais lattices, also referred to as *space lattices*, describe the geometric arrangement of the lattice points, ^[6] and therefore the translational symmetry of the crystal. The three dimensions of space afford 14 distinct Bravais lattices describing the translational symmetry. All crystalline materials recognized today, not including <u>quasicrystals</u>, fit in one of these arrangements. The fourteen three-dimensional lattices, classified by lattice system, are shown above.

The crystal structure consists of the same group of atoms, the *basis*, positioned around each and every lattice point. This group of atoms therefore repeats indefinitely in three dimensions according to the arrangement of one of the Bravais lattices. The characteristic rotation and mirror symmetries of the unit cell is described by its <u>crystallographic</u> point group.

Crystal systems

A crystal system is a set of point groups in which the point groups themselves and their corresponding space groups are assigned to a lattice system. Of the 32 point groups that exist in three dimensions, most are assigned to only one lattice system, in which case the crystal system and lattice system both have the same name. However, five point groups are assigned to two lattice systems, rhombohedral and hexagonal, because both lattice systems exhibit threefold rotational symmetry. These point groups are assigned to the trigonal crystal system.

Crystal family	Crystal system	Point group / Crystal class	Schönflies	Point symmetry	Order	Abstract group
triclinic		pedial	C ₁	enantiomorphic polar	1	trivial \mathbb{Z}_1
		pinacoidal	C _i (S ₂)	centrosymmetric	2	cyclic \mathbb{Z}_2
monoclinic		sphenoidal	C ₂	enantiomorphic polar	2	cyclic \mathbb{Z}_2
		domatic	C _s (C _{1h})	polar	2	cyclic \mathbb{Z}_2
		prismatic	C _{2h}	centrosymmetric	4	$\frac{Klein\ four}{\mathbb{V} = \mathbb{Z}_2 \times \mathbb{Z}_2}$
orthorhombic		rhombic-disphenoidal	D ₂ (V)	enantiomorphic	4	$\frac{Klein\ four}{\mathbb{V} = \mathbb{Z}_2 \times \mathbb{Z}_2}$
		rhombic-pyramidal	C _{2v}	polar	4	$\frac{Klein\ four}{\mathbb{V} = \mathbb{Z}_2 \times \mathbb{Z}_2}$
		rhombic-dipyramidal	D _{2h} (V _h)	centrosymmetric	8	$\mathbb{V} imes \mathbb{Z}_2$
		tetragonal-pyramidal	C ₄	enantiomorphic polar	4	cyclic \mathbb{Z}_4
		tetragonal-		non-		

tetragonal		disphenoidal	S ₄	centrosymmetric	4	cyclic \mathbb{Z}_4
		tetragonal-dipyramidal	C _{4h}	centrosymmetric	8	$\mathbb{Z}_4 imes \mathbb{Z}_2$
		tetragonal- trapezohedral	D ₄	enantiomorphic	8	$rac{ ext{dihedral}}{\mathbb{D}_8=\mathbb{Z}_4 times\mathbb{Z}_2}$
		ditetragonal-pyramidal	C _{4v}	polar	8	$rac{ ext{dihedral}}{\mathbb{D}_8=\mathbb{Z}_4 times\mathbb{Z}_2}$
		tetragonal- scalenohedral	D _{2d} (V _d)	non- centrosymmetric	8	$rac{ ext{dihedral}}{\mathbb{D}_8=\mathbb{Z}_4 times\mathbb{Z}_2}$
		ditetragonal- dipyramidal	D _{4h}	centrosymmetric 16		$\mathbb{D}_8 imes \mathbb{Z}_2$
hexagonal	trigonal	trigonal-pyramidal	C ₃	enantiomorphic polar	3	cyclic Z ₃
		rhombohedral	C _{3i} (S ₆)	centrosymmetric 6		$rac{ ext{cyclic}}{\mathbb{Z}_6}=\mathbb{Z}_3 imes\mathbb{Z}_2$
		trigonal-trapezohedral	D ₃	enantiomorphic	6	$rac{ ext{dihedral}}{\mathbb{D}_6=\mathbb{Z}_3 times\mathbb{Z}_2}$
		ditrigonal-pyramidal	C _{3v}	polar	6	$rac{ ext{dihedral}}{\mathbb{D}_6=\mathbb{Z}_3 times\mathbb{Z}_2}$
		ditrigonal- scalenohedral	D _{3d}	centrosymmetric	12	$egin{array}{c} ext{dihedral} \ \mathbb{D}_{12} = \mathbb{Z}_6 times \mathbb{Z}_2 \ \end{array}$
	hexagonal	hexagonal-pyramidal	C ₆	enantiomorphic polar	6	$rac{ ext{cyclic}}{\mathbb{Z}_6}=\mathbb{Z}_3 imes\mathbb{Z}_2$
		trigonal-dipyramidal	C _{3h}	non- centrosymmetric	6	$rac{ ext{cyclic}}{\mathbb{Z}_6 = \mathbb{Z}_3 imes \mathbb{Z}_2}$
		hexagonal- dipyramidal	C _{6h}	centrosymmetric	12	$\mathbb{Z}_6 imes\mathbb{Z}_2$
		hexagonal- trapezohedral	D ₆	enantiomorphic	12	$\frac{\text{dihedral}}{\mathbb{D}_{12} = \mathbb{Z}_6 \rtimes \mathbb{Z}_2}$
		dihexagonal- pyramidal	C _{6v}	polar	12	$rac{ ext{dihedral}}{\mathbb{D}_{12}=\mathbb{Z}_6 times\mathbb{Z}_2}$
		ditrigonal-dipyramidal	D _{3h}	non- centrosymmetric	12	$\frac{\text{dihedral}}{\mathbb{D}_{12} = \mathbb{Z}_6 \rtimes \mathbb{Z}_2}$
		dihexagonal- dipyramidal	D _{6h}	centrosymmetric	24	$\mathbb{D}_{12} imes \mathbb{Z}_2$
cubic		tetartoidal	Т	enantiomorphic	12	alternating \mathbb{A}_4
		diploidal	T _h	centrosymmetric	24	$\mathbb{A}_4 imes \mathbb{Z}_2$
		gyroidal	0	enantiomorphic 24		symmetric S ₄
		hextetrahedral	T _d	non- centrosymmetric	24	symmetric S ₄
		hexoctahedral	O _h	centrosymmetric	48	$\mathbb{S}_4 imes \mathbb{Z}_2$

In total there are seven crystal systems: triclinic, monoclinic, orthorhombic, tetragonal, trigonal, hexagonal, and cubic.

Point groups

The crystallographic point group or *crystal class* is the mathematical group comprising the symmetry operations that leave at least one point unmoved and that leave the appearance of the crystal structure unchanged. These symmetry operations include

- Reflection, which reflects the structure across a reflection plane
- Rotation, which rotates the structure a specified portion of a circle about a rotation axis
- Inversion, which changes the sign of the coordinate of each point with respect to a center of symmetry or inversion point
- *Improper rotation*, which consists of a rotation about an axis followed by an inversion.

Rotation axes (proper and improper), reflection planes, and centers of symmetry are collectively called *symmetry elements*. There are 32 possible crystal classes. Each one can be classified into one of the seven crystal systems.

Space groups

In addition to the operations of the point group, the space group of the crystal structure contains translational symmetry operations. These include:

- Pure translations, which move a point along a vector
- Screw axes, which rotate a point around an axis while translating parallel to the axis.^[9]
- Glide planes, which reflect a point through a plane while translating it parallel to the plane.

There are 230 distinct space groups.

Atomic coordination

By considering the arrangement of atoms relative to each other, their coordination numbers (or number of nearest neighbors), interatomic distances, types of bonding, etc., it is possible to form a general view of the structures and alternative ways of visualizing them.^[10]

Close packing

The principles involved can be understood by considering the most efficient way of packing together equal-sized spheres and stacking <u>close-packed</u> atomic planes in three dimensions. For example, if plane A lies beneath plane B, there are two possible ways of placing an additional atom on top of layer B. If an additional layer was placed directly over plane A, this would give rise to the following series:

...ABABABAB...

This arrangement of atoms in a crystal structure is known as **hexagonal close packing (hcp)**.

If, however, all three planes are staggered relative to each other and it is not until the fourth layer is positioned directly over plane A that the sequence is repeated, then the following sequence arises:

...ABCABCABC...

This type of structural arrangement is known as **cubic close packing (ccp)**.

The unit cell of a ccp arrangement of atoms is the face-centered cubic (fcc) unit cell. This is not immediately obvious as the closely packed layers are parallel to the {111} planes of the fcc unit cell. There are four different orientations of the close-packed layers.

The **packing efficiency** can be worked out by calculating the total volume of the spheres and dividing by the volume of the cell as follows:

$$rac{4 imesrac{4}{3}\pi r^3}{16\sqrt{2}r^3}=rac{\pi}{3\sqrt{2}}=0.7405...$$

The 74% packing efficiency is the maximum density possible in unit cells constructed of spheres of only one size. Most crystalline forms of metallic elements are hcp, fcc, or bcc (body-centered cubic). The coordination number of atoms in hcp and fcc structures is 12 and its atomic packing factor (APF) is the number mentioned above, 0.74. This can be compared to the APF of a bcc structure, which is 0.68.

The hcp lattice (left) and the fcc lattice (right)

Grain boundaries

Grain boundaries are interfaces where crystals of different orientations meet.^[6] A grain boundary is a single-phase interface, with crystals on each side of the boundary being identical except in orientation. The term "crystallite boundary" is sometimes, though rarely, used. Grain boundary areas contain those atoms that have been perturbed from their original lattice sites, dislocations, and impurities that have migrated to the lower energy grain boundary.

Treating a grain boundary geometrically as an interface of a single crystal cut into two parts, one of which is rotated, we see that there are five variables required to define a grain boundary. The first two numbers come from the unit vector that specifies a rotation axis. The third number designates the angle of rotation of the grain. The final two numbers specify the plane of the grain boundary (or a unit vector that is normal to this plane).^[10]

Grain boundaries disrupt the motion of dislocations through a material, so reducing crystallite size is a common way to improve strength, as described by the <u>Hall-Petch</u> relationship. Since grain boundaries are defects in the crystal structure they tend to decrease the <u>electrical</u> and <u>thermal conductivity</u> of the material. The high interfacial energy and relatively weak bonding in most grain boundaries often makes them preferred sites for the onset of corrosion and for the <u>precipitation</u> of new phases from the solid. They are also important to many of the mechanisms of <u>creep</u>.^[10]

Grain boundaries are in general only a few nanometers wide. In common materials, crystallites are large enough that grain boundaries account for a small fraction of the material. However, very small grain sizes are achievable. In nanocrystalline solids, grain boundaries become a significant volume fraction of the material, with profound effects on

such properties as <u>diffusion</u> and <u>plasticity</u>. In the limit of small crystallites, as the volume fraction of grain boundaries approaches 100%, the material ceases to have any crystalline character, and thus becomes an amorphous solid.^[10]

Defects and impurities

Real crystals feature <u>defects</u> or irregularities in the ideal arrangements described above and it is these defects that critically determine many of the electrical and mechanical properties of real materials. When one atom substitutes for one of the principal atomic components within the crystal structure, alteration in the electrical and thermal properties of the material may ensue.^[11] Impurities may also manifest as spin impurities in certain materials. Research on magnetic impurities demonstrates that substantial alteration of certain properties such as specific heat may be affected by small concentrations of an impurity, as for example impurities in semiconducting <u>ferromagnetic alloys</u> may lead to different properties as first predicted in the late 1960s.^{[12][13]} <u>Dislocations</u> in the crystal lattice allow <u>shear</u> at lower stress than that needed for a perfect crystal structure.^[14]

Prediction of structure

The difficulty of predicting stable crystal structures based on the knowledge of only the chemical composition has long been a stumbling block on the way to fully computational materials design. Now, with more powerful algorithms and high-performance computing, structures of medium complexity can be predicted using such approaches as evolutionary algorithms, random sampling, or metadynamics.

The crystal structures of simple ionic solids (e.g., NaCl or table salt) have long been rationalized in terms of <u>Pauling's rules</u>, first set out in 1929 by <u>Linus Pauling</u>, referred to by many since as the "father of the chemical bond". Pauling also considered the nature of the interatomic forces in metals, and concluded that about half of the five d-orbitals in the transition metals are involved in bonding, with the remaining nonbonding d-orbitals being responsible for the magnetic properties. He, therefore, was able to correlate the number of d-orbitals in bond

Crystal structure of sodium chloride (table salt)

formation with the bond length as well as many of the physical properties of the substance. He subsequently introduced the metallic orbital, an extra orbital necessary to permit uninhibited resonance of valence bonds among various electronic structures.^[16]

In the <u>resonating valence bond theory</u>, the factors that determine the choice of one from among alternative crystal structures of a metal or intermetallic compound revolve around the energy of resonance of bonds among interatomic positions. It is clear that some modes of resonance would make larger contributions (be more mechanically stable than others), and that in particular a simple ratio of number of bonds to number of positions would be exceptional. The resulting principle is that a special stability is associated with the simplest ratios or "bond numbers": $\frac{1}{2}$, $\frac{1}{3}$, $\frac{2}{3}$, $\frac{1}{4}$, etc. The choice of structure and the value of the <u>axial ratio</u> (which determines the relative bond lengths) are thus a result of the effort of an atom to use its valency in the formation of stable bonds with simple fractional bond numbers. [17][18]

After postulating a direct correlation between electron concentration and crystal structure in beta-phase alloys, <u>Hume-Rothery</u> analyzed the trends in melting points, compressibilities and bond lengths as a function of group number in the periodic table in order to establish a system of valencies of the transition elements in the metallic state. This treatment thus emphasized the increasing bond strength as a function of group number.^[19] The operation of directional forces were emphasized in one article on the relation between bond hybrids and the metallic structures. The resulting correlation between electronic and crystalline structures is summarized by a single parameter, the weight of the d-electrons per hybridized metallic orbital. The "d-weight" calculates out to 0.5, 0.7 and 0.9 for the fcc, hcp and bcc structures respectively. The relationship between d-electrons and crystal structure thus becomes apparent.^[20]

In crystal structure predictions/simulations, the periodicity is usually applied, since the system is imagined as unlimited big in all directions. Starting from a triclinic structure with no further symmetry property assumed, the system may be driven to show some additional symmetry properties by applying Newton's Second Law on particles in the unit cell and a recently developed dynamical equation for the system period vectors ^[21] (lattice parameters including angles), even if the system is subject to external stress.

Polymorphism

Polymorphism is the occurrence of multiple crystalline forms of a material. It is found in many crystalline materials including polymers, minerals, and metals. According to Gibbs' rules of phase equilibria, these unique crystalline phases are dependent on intensive variables such as pressure and temperature. Polymorphism is related to allotropy, which refers to elemental solids. The complete morphology of a material is described by polymorphism and other variables such as crystal habit, amorphous fraction or crystallographic defects. Polymorphs have different stabilities and may spontaneously convert from a metastable form (or thermodynamically unstable form) to the stable form at a particular temperature. They also exhibit different melting points, solubilities, and X-ray diffraction patterns.

One good example of this is the <u>quartz</u> form of <u>silicon</u> <u>dioxide</u>, or SiO₂. In the vast majority of <u>silicates</u>, the Si atom shows tetrahedral coordination by 4 oxygens. All but one of the crystalline forms involve tetrahedral {SiO₄} units linked together by shared vertices in different

Quartz is one of the several crystalline forms of silica, SiO_2 . The most important forms of silica include: α -quartz, β -quartz, tridymite, cristobalite, coesite, and stishovite.

arrangements. In different minerals the tetrahedra show different degrees of networking and polymerization. For example, they occur singly, joined together in pairs, in larger finite clusters including rings, in chains, double chains, sheets, and three-dimensional frameworks. The minerals are classified into groups based on these structures. In each of the 7 thermodynamically stable crystalline forms or polymorphs of crystalline quartz, only 2 out of 4 of each the edges of the $\{SiO_4\}$ tetrahedra are shared with others, yielding the net chemical formula for silica: SiO_2 .

Another example is elemental \underline{tin} (Sn), which is malleable near ambient temperatures but is $\underline{brittle}$ when cooled. This change in mechanical properties due to existence of its two major allotropes, α - and β -tin. The two allotropes that are encountered at normal pressure and temperature, α -tin and β -tin, are more commonly known as gray tin and white tin respectively. Two more allotropes, γ and σ , exist at temperatures above 161 °C and pressures above several GPa. White tin is metallic, and is the stable crystalline form at or above room temperature. Below 13.2 °C, tin exists in the gray form, which has a diamond cubic crystal structure, similar to diamond, silicon or germanium. Gray tin has no metallic properties at all, is a dull gray powdery material, and has few uses, other than a few specialized semiconductor applications. Although the α - β transformation temperature of tin is nominally 13.2 °C, impurities (e.g. Al, Zn, etc.) lower the transition temperature well below o °C, and upon addition of Sb or Bi the transformation may not occur at all. [24]

Physical properties

Twenty of the 32 crystal classes are <u>piezoelectric</u>, and crystals belonging to one of these classes (point groups) display <u>piezoelectricity</u>. All piezoelectric classes lack a center of symmetry. Any material develops a <u>dielectric</u> polarization when an electric field is applied, but a substance that has such a natural charge separation even in the absence of a field is called a polar material. Whether or not a material is polar is determined solely by its crystal structure. Only 10 of the 32 point groups are <u>polar</u>. All polar crystals are <u>pyroelectric</u>, so the 10 polar crystal classes are sometimes referred to as the pyroelectric classes.

There are a few crystal structures, notably the <u>perovskite structure</u>, which exhibit <u>ferroelectric</u> behavior. This is analogous to <u>ferromagnetism</u>, in that, in the absence of an electric field during production, the ferroelectric crystal does not exhibit a polarization. Upon the application of an electric field of sufficient magnitude, the crystal becomes permanently polarized. This polarization can be reversed by a sufficiently large counter-charge, in the same way that a ferromagnet can be reversed. However, although they are called ferroelectrics, the effect is due to the crystal structure (not the presence of a ferrous metal).

See also

- Brillouin zone
- Crystal engineering
- Crystal growth
- Crystallographic database
- Fractional coordinates
- Frank–Kasper phases
- Hermann–Mauguin notation Notation to represent symmetry in point groups, plane groups and space groups
- Laser-heated pedestal growth
- Liquid crystal State of matter with properties of both conventional liquids and crystals
- Patterson function
- Periodic table (crystal structure)
- Primitive cell
- Schoenflies notation Notation to represent symmetry in point groups
- Seed crystal
- Wigner-Seitz cell

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- The internal structure of crystals... Crystallography for beginners (http://www.xtal.iqfr.csic.es/Cristalografia/index-en.html)
- Appendix A from the manual for Atoms, software for XAFS (http://iffwww.iff.kfa-juelich.de/icp/atoms/atoms.sgml-7. html)
- Intro to Minerals: Crystal Class and System (http://dave.ucsc.edu/myrtreia/crystal.html)
- Introduction to Crystallography and Mineral Crystal Systems (http://www.rockhounds.com/rockshop/xtal/index.html)
- Crystal planes and Miller indices (http://www.ece.byu.edu/cleanroom/EW_orientation.phtml)
- Interactive 3D Crystal models (http://www.ibiblio.org/e-notes/Cryst/Cryst.htm)
- Specific Crystal 3D models (http://chemannex.weebly.com/crystal-structures.html)
- Crystallography Open Database (with more than 140,000 crystal structures)

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