## **PROBABILITY**

## T SIVA PARVATHI - FWC22089

- 13.4.5 <sup>1</sup> Find the probability distribution of the number of successes in two tosses of a die, where a success is defined as
  - (a) number greater than 4
  - (b) six appears on at least one die

**Solution:** Given that a die tossed two times,

Variable	Values	Description
n	2	Number of tosses of a die
$X_1$	{1,2,3,4,5,6}	1st toss outcomes of a die
$X_2$	{1,2,3,4,5,6}	2st toss outcomes of a die
$p_1$	$\frac{1}{3}$	Pr(X > 4)
$q_1$	$1 - p_1$	$Pr(X \le 4)$
$p_2$	$\frac{1}{6}$	Pr(X=6)
$q_2$	$1 - p_2$	$Pr(X \neq 6)$

Table 2: Variable Description

## (a) number greater than 4

$$p_1 = \frac{1}{3} \tag{13.4.1.1}$$

$$p_1 = \frac{1}{3}$$
 (13.4.1.1)  
$$q_1 = 1 - p_1 = \frac{2}{3}$$
 (13.4.1.2)

In n Bernoulli trials with k success and (n-k) failures, the probability of k success in n-Bernoulli trials can be given as,

$$p_{X_i}(k) = \begin{cases} {}^{n}C_k p_1{}^{k} q_1{}^{n-k} & 0 \le k \le n \\ 0 & \text{otherwise} \end{cases}$$
 (13.4.1.3)

where, n=2

 $X_1$  and  $X_2$  are independent events, so the desired outcome is

$$X = X_1 + X_2 \tag{13.4.1.4}$$

Probability distribution of getting number greater than 4 is,

$$p_X(k) = \begin{cases} \frac{4}{9}, & k = 0\\ \frac{4}{9}, & k = 1\\ \frac{1}{9}, & k = 2 \end{cases}$$
 (13.4.1.5)

<sup>&</sup>lt;sup>1</sup>Read question numbers as (CHAPTER NUMBER).(EXERCISE NUMBER).(QUESTION NUMBER)

where,

k=0, not getting a favourable outcome on either die

k=1, getting a favourable outcome on one die

k=2, getting a favourable outcome on both die

## (b) six appears on at least one die

$$p_2 = \frac{1}{6} \tag{13.4.2.6}$$

$$p_2 = \frac{1}{6}$$
 (13.4.2.6)  
$$q_2 = 1 - p_2 = \frac{5}{6}$$
 (13.4.2.7)

In n Bernoulli trials with k success and (n-k) failures, the probability of k success in n-Bernoulli trials can be given as,

$$p_{X_i}(k) = \begin{cases} {}^{n}C_k p_2{}^{k} q_2{}^{n-k} & 0 \le k \le n \\ 0 & \text{otherwise} \end{cases}$$
 (13.4.2.8)

where, n=2

 $X_1$  and  $X_2$  are independent events, so the desired outcome is

$$X = X_1 + X_2 \tag{13.4.2.9}$$

Probability distribution of getting six on atleast one die is,

$$p_X(k) = \begin{cases} \frac{25}{36}, & k = 0\\ \frac{10}{36}, & k = 1\\ \frac{1}{36}, & k = 2 \end{cases}$$
 (13.4.2.10)