

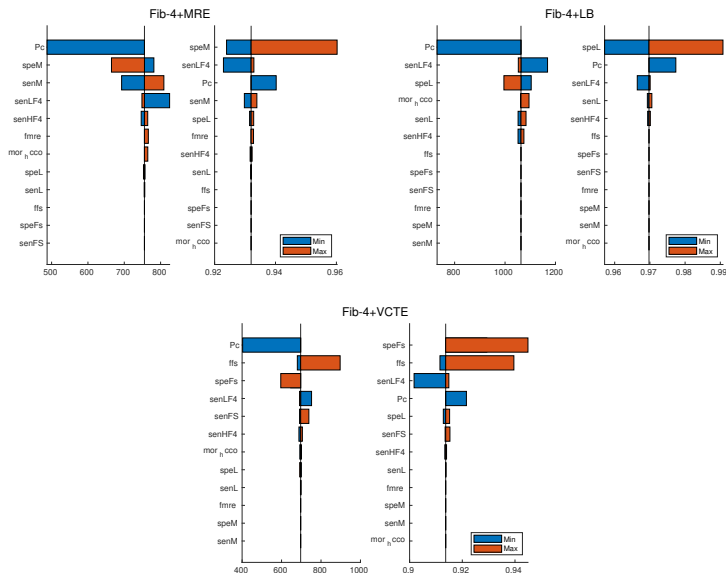
Coding Assignment 1 Write-up

Andrew Sivaprakasam

03/20/2021

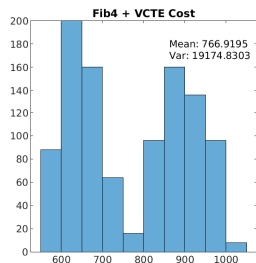
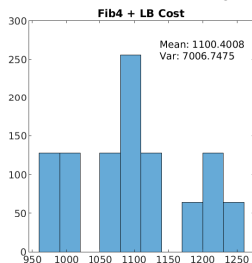
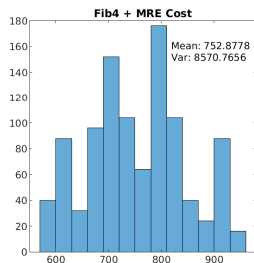
Question 2 | One-Way Sensitivity Analysis Tornado Plots

Observations of how sensitive the model output is to the specified parameters.

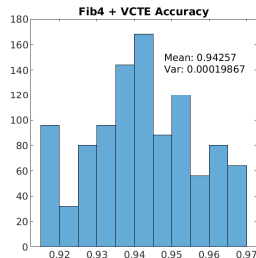
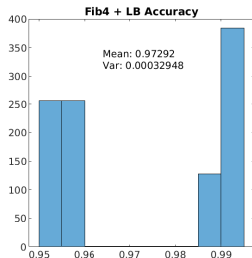
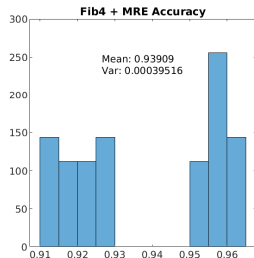


Question 3a | Full-Factorial Histograms

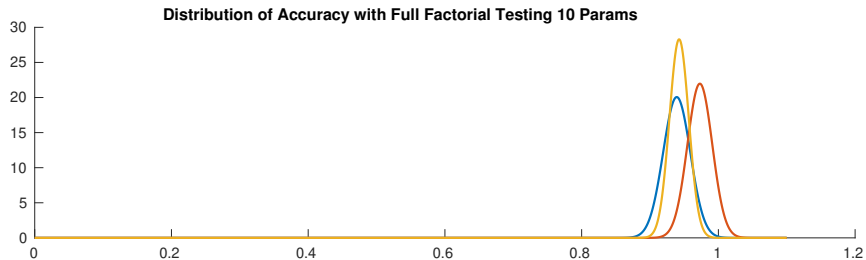
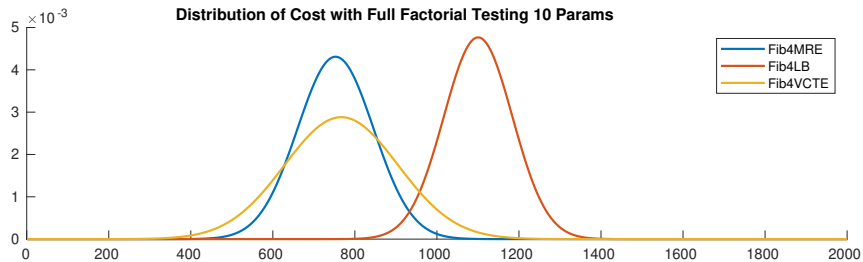
Distribution of Cost with Full Factorial Testing 10 Params



Distribution of Accuracy with Full Factorial Testing 10 Params



Question 3a | Full-Factorial Fitted Distributions



Question 3b| Full-Factorial Percent ≥ 300 (from Code)

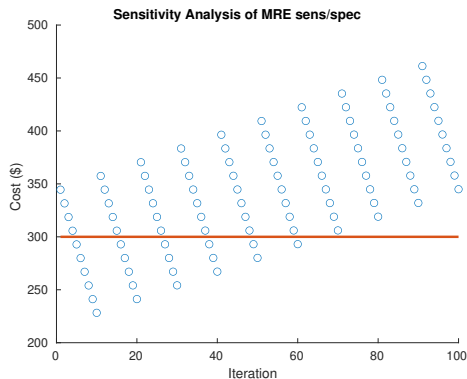
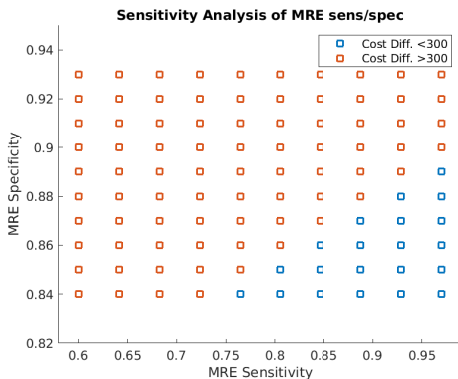
The percent of trials where the difference $|LB_{cost} - MRE_{cost}| > 300$ was 61.7188%

See q3.m 252-253:

```
diff = abs(Fib4MRE_cost_out-Fib4LB_cost_out);  
percent_greater = sum(diff>300)*100/L;
```

Question 3c| Full-Factorial Sensitivity Analysis on MRE

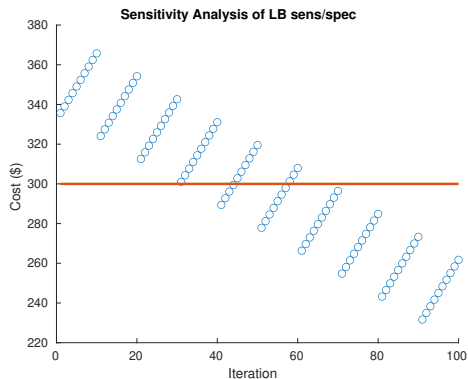
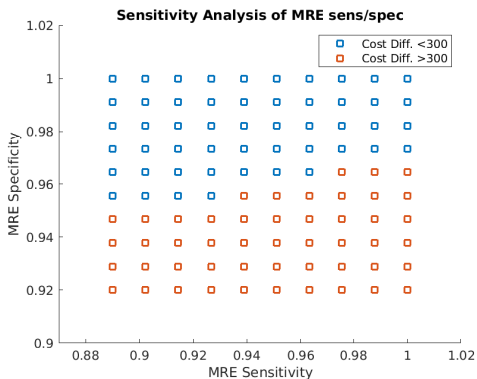
The effect of varying MRE specificity and sensitivity params (speM & senM) on the cost difference between MRE and LB can be visualized as follows:



79% of the simulated outputs for cost difference were greater than 300.

Question 3d| Full-Factorial Sensitivity Analysis on LB

The effect of varying LB specificity and sensitivity params (speM & senM) on the cost difference between MRE and LB can be visualized as follows:

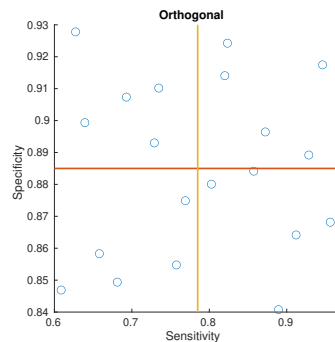
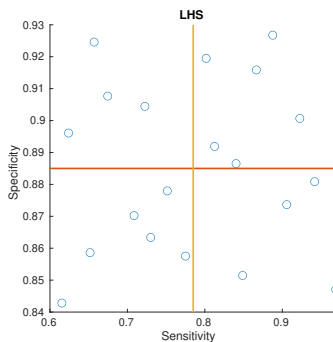
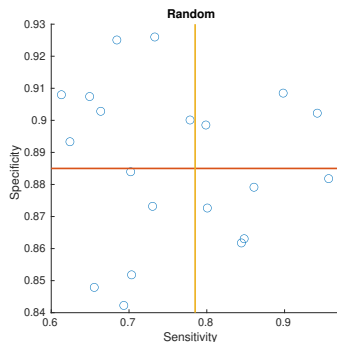


49% of the simulated outputs for cost difference were greater than 300.

Sample-Based Sensitivity Analysis

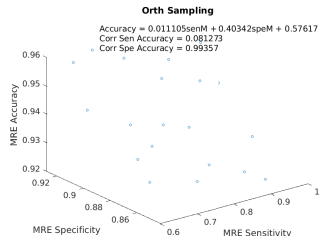
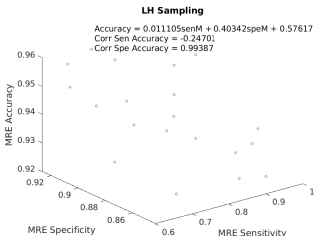
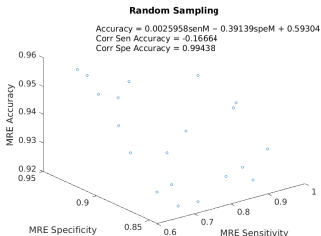
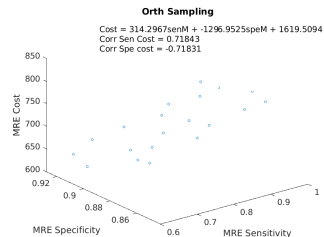
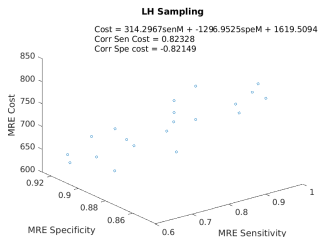
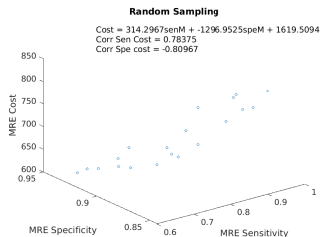
Here is a verification that my sampling was done correctly. I created a brute-force method for orthogonal sampling, `orth_samples.m`.

Verification of Sampling Distributions | MRE



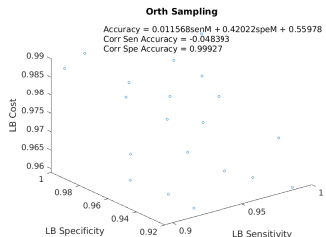
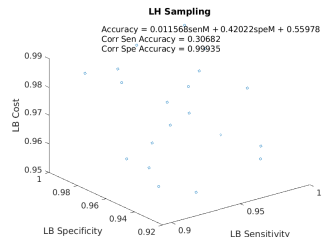
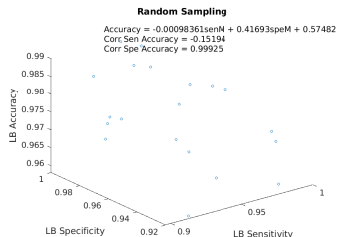
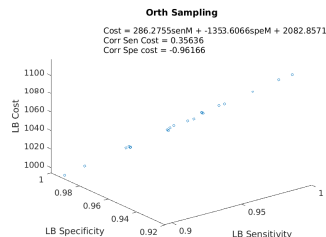
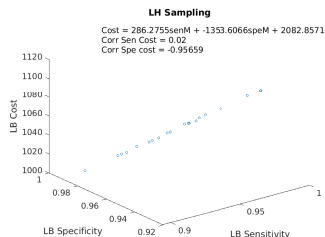
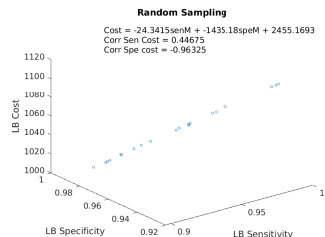
Question 3e | Sample-Based Sensitivity Analysis for MRE

Here are the 3D plots, regression equations and Pearson's correlation coefficients for the MRE sample-based Sensitivity Analysis.



Question 3f | Sample-Based Sensitivity Analysis for LB

Here are the 3D plots, regression equations and Pearson's correlation coefficients for the LB sample-based Sensitivity Analysis.



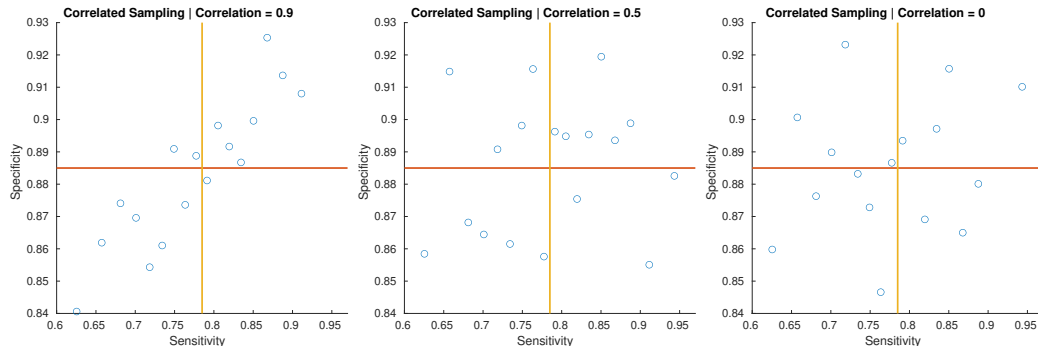
Question 3g | Rank/Statistical Tests

Rank transformations may be useful for particular sensitivity analyses, but depend on the type of data and sample selection. In grid-based techniques, the model outputs may have a sort of distribution or cluster of interest. With a rank transformation, visualizing this will be difficult, since the data is transformed to a uniform distribution.

Similarly, statistical tests may be employed when proper assumptions hold true. In this model, the outputs may not be normally distributed (as in the Fib + MRE/LB Accuracy full-factorial experiment).

Question 3h | Inducing Correlation in Sampling

Here is a verification that my sampling correlation was induced properly:



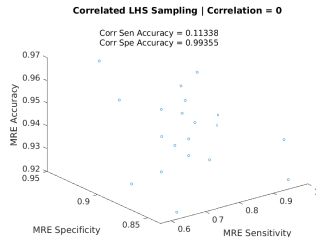
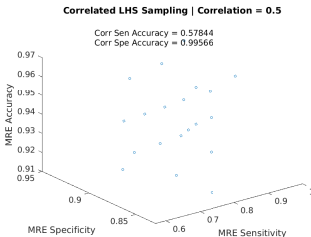
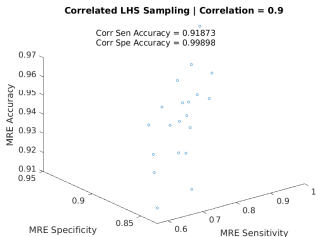
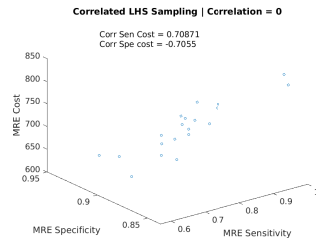
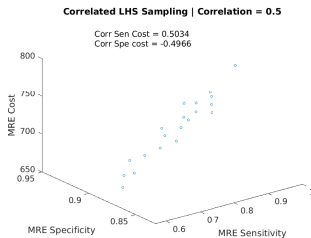
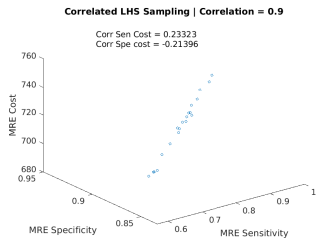
I chose these sampling correlations since there should in theory be a fairly strong correlation between sensitivity and specificity for a good clinical test. However, in some cases, they may not have as much correlation or be weakly correlated. I also assumed a normal distribution of sampling, since these test results are likely also normally distributed.

Correction!

In reality there is more often a trade-off between sensitivity and specificity (not all clinical tests are perfect). Would have been more realistic to have shifted sampling to more properly represent ROC curve!

Question 3h | Inducing Correlation in Sampling - MRE

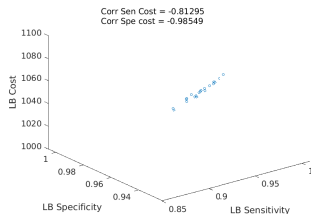
Here are the results with correlated sampling for MRE sens/spec. Correlation decreases from left to right.



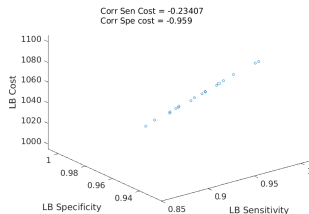
Question 3h | Inducing Correlation in Sampling - LB

Here are the results with correlated sampling for LB sens/spec. Correlation decreases from left to right.

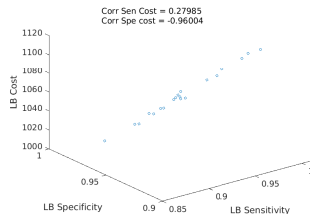
Correlated LHS Sampling | Correlation = 0.9



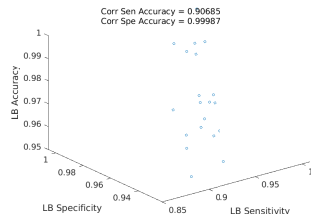
Correlated LHS Sampling | Correlation = 0.5



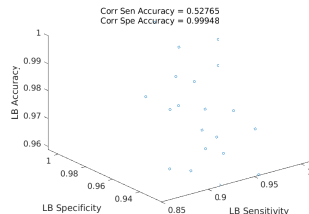
Correlated LHS Sampling | Correlation = 0



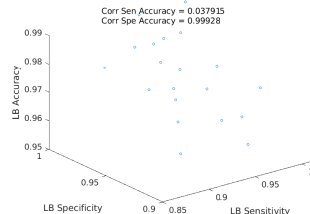
Correlated LHS Sampling | Correlation = 0.9



Correlated LHS Sampling | Correlation = 0.5



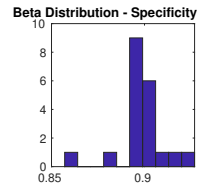
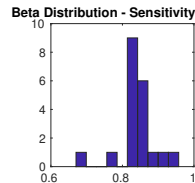
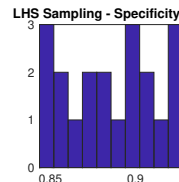
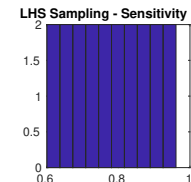
Correlated LHS Sampling | Correlation = 0



Question 3i | Importance Sampling

I changed my sampling distribution from uniform (as in random, lhs, orthogonal sampling). I used a $\text{Beta}(\alpha, \beta)$ distribution with $\alpha = 5$ and $\beta = 2$ for both MRE specificity and sensitivity to simulate a more optimistic sampling distribution. This beta distribution implies that the model output means are representative of samples with left-skewed sensitivity and specificity.

The distributions compared to the uniform distribution found in the LHS sampling technique



Question 3i | Importance Sampling

The output averages were as follows:

| | Parameter Varied | |
|-----------------|------------------|----------|
| | MRE Sens | MRE Spec |
| Cost | 767.0697 | 706.8664 |
| Accuracy | 0.9324 | 0.9471 |

As sensitivity is skewed left, the accuracy decreases and cost increases. Conversely, as specificity is skewed left, the accuracy increases, and the cost decreases. This could be because a higher positive test rate (true in screening tests with higher sensitivity) results in a required confirmatory test with another method with additional costs. A more specific test means less false positives, which prevents decreases the likelihood of this added cost.