

# Roseler\_ESN\_3D

January 2, 2020

## 1 Predicting Roseler System using Echo State Neural Network

### 1.0.1 Importing Required Libraries

```
[1]: import numpy as np
import seaborn as sns
import matplotlib.pyplot as plt
import ESN
import pandas as pd
```

### 1.0.2 Set seed for random weights generator

```
[2]: def set_seed(seed=None):
    """Making the seed (for random values) variable if None"""

    # Set the seed
    if seed is None:
        import time
        seed = int((time.time()*10**6) % 4294967295)
    try:
        np.random.seed(seed)
    except Exception as e:
        print( "!!! WARNING !!!: Seed was not set correctly.")
        print( "!!! Seed that we tried to use: "+str(seed))
        print( "!!! Error message: "+str(e))
        seed = None
    print( "Seed used for random values:", seed)
    return seed
```

```
[3]: ## Set a particular seed for the random generator (for example seed = 42), or
    ↪ use a "random" one (seed = None)
# NB: reservoir performances should be averaged accross at least 30 random
    ↪ instances (with the same set of parameters)
seed = 42 #None #42
```

```
[4]: set_seed(seed) #random.seed(seed)
```

Seed used for random values: 42

[4]: 42

```
[5]: initLen = 100
      trainLen = initLen + 800
      testLen = 700
```

```
[6]: df = pd.read_excel(r'C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
      ↳Prediction-Phase-2\Final_Version\3D_ReservoirComputing\Input\Roseler_
      ↳Data\Roseler Data.xlsx', index = False)
```

```
[7]: df.shape
```

[7]: (1649, 4)

## 2 EDA

```
[8]: import os

if not os.path.exists(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↳Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler"):
    os.mkdir(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↳Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler")

[9]: from matplotlib import rcParams
      rcParams.update({'figure.autolayout': True})
      fig = plt.figure()
      ax=fig.add_axes([0,0,1,1])
      ax.plot(df['t'],df['x'])
      plt.title('Plot of X w.r.t time of entire data', fontsize=16)
      plt.xlabel('t', fontsize = 14)
      plt.ylabel('x', fontsize = 14)
      plt.savefig(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↳Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler\X_with_Time.
↳png", bbox_inches = "tight")
      plt.show()
```

C:\Users\INFO-DSK-02\Anaconda3\lib\site-packages\ipykernel\_launcher.py:9:

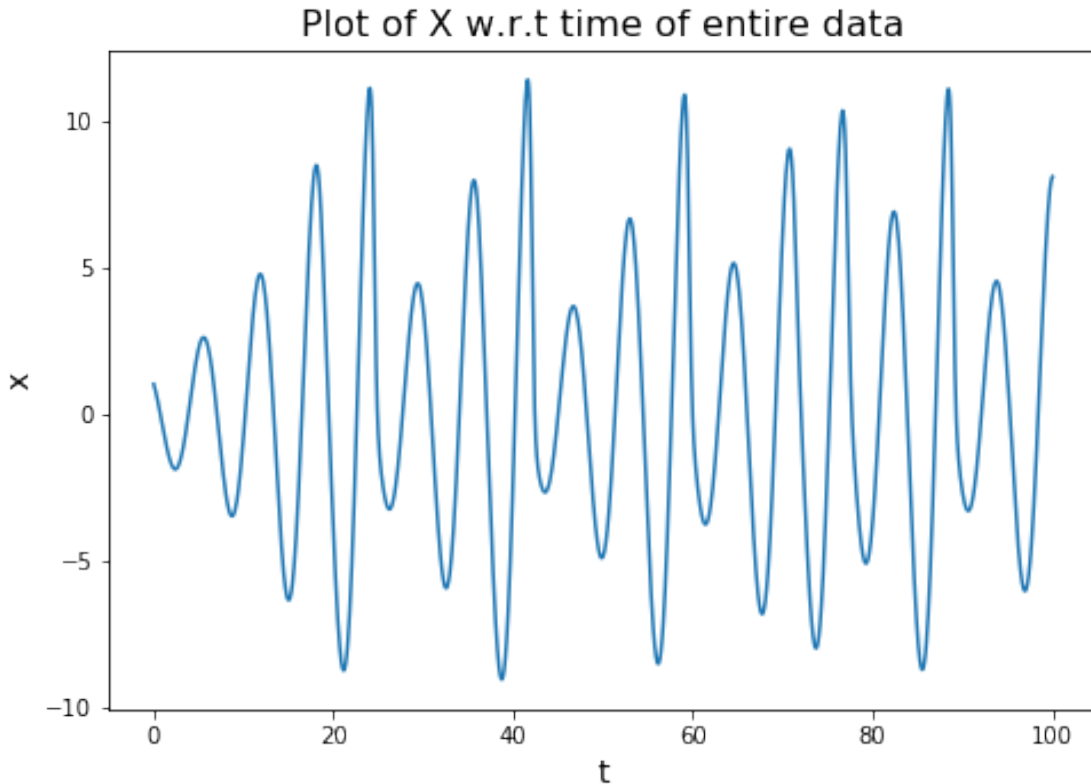
UserWarning: This figure includes Axes that are not compatible with  
tight\_layout, so results might be incorrect.

if \_\_name\_\_ == '\_\_main\_\_':

C:\Users\INFO-DSK-02\Anaconda3\lib\site-packages\IPython\core\pylabtools.py:128:

UserWarning: This figure includes Axes that are not compatible with  
tight\_layout, so results might be incorrect.

fig.canvas.print\_figure(bytes\_io, \*\*kw)



```
import plotly.graph_objects as go import numpy as np
```

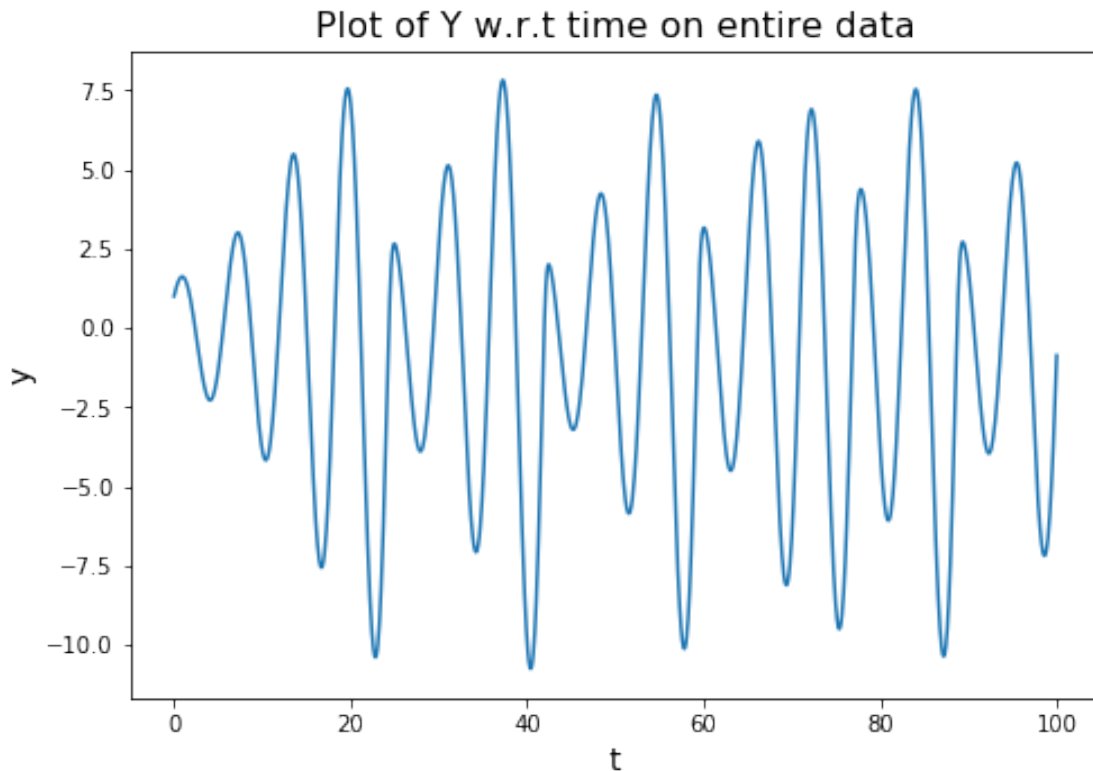
```
fig = go.Figure(data=go.Scatter(x=df['t'], y=df['x'], mode='markers')) fig.update_layout( ti-
tle="Plot of X w.r.t time of entire data", xaxis_title="Time", yaxis_title="X", font=dict( fam-
ily="Courier New, monospace", size=18, color="#7f7f7f" ) ) fig.show()
```

```
[10]: fig = plt.figure()
ax=fig.add_axes([0,0,1,1])
ax.plot(df['t'],df['y'] )
plt.title('Plot of Y w.r.t time on entire data', fontsize=16)
plt.xlabel('t', fontsize = 14)
plt.ylabel('y', fontsize = 14)
plt.savefig(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↪Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler\Y_with_Time.
↪png", bbox_inches = "tight")
plt.show()
```

C:\Users\INFO-DSK-02\Anaconda3\lib\site-packages\ipykernel\_launcher.py:7:

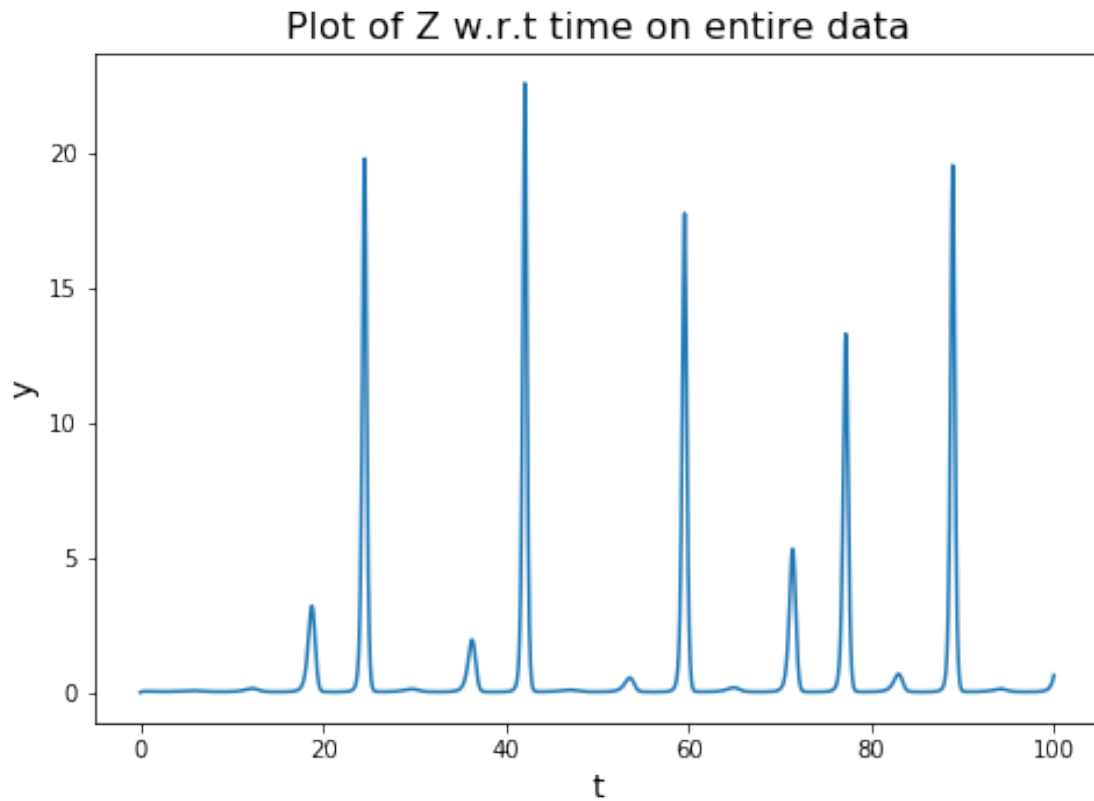
UserWarning: This figure includes Axes that are not compatible with  
tight\_layout, so results might be incorrect.

```
import sys
```



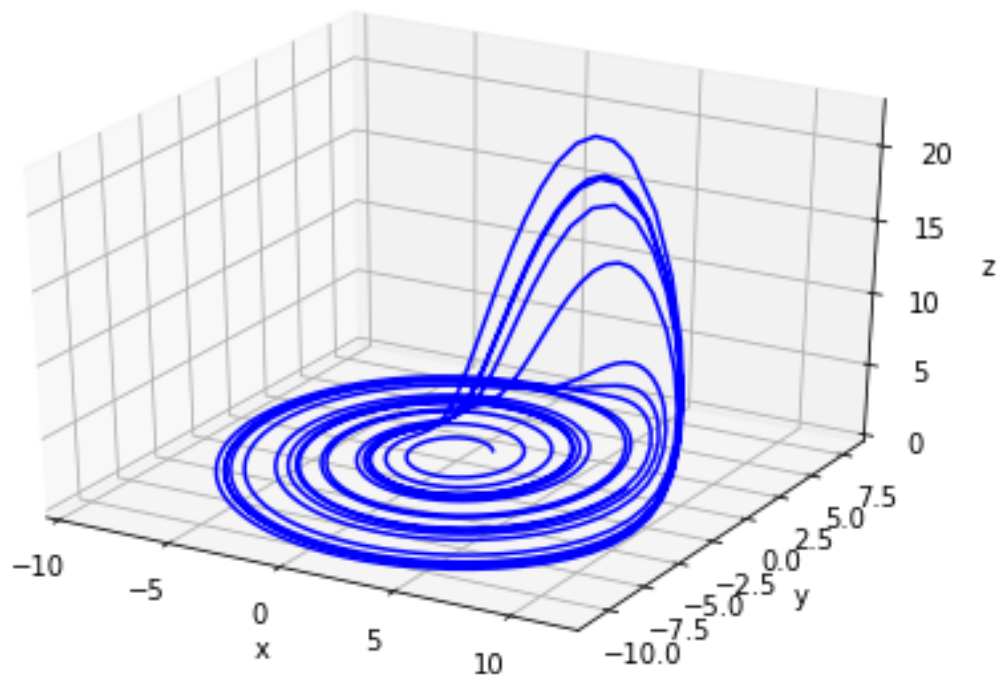
```
[11]: fig = plt.figure()
ax=fig.add_axes([0,0,1,1])
ax.plot(df['t'],df['z'] )
plt.title('Plot of Z w.r.t time on entire data', fontsize=16)
plt.xlabel('t', fontsize = 14)
plt.ylabel('y', fontsize = 14)
plt.savefig(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↳Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler\Z_with_Time.
↳png", bbox_inches = "tight")
plt.show()
```

C:\Users\INFO-DSK-02\Anaconda3\lib\site-packages\ipykernel\_launcher.py:7:  
 UserWarning: This figure includes Axes that are not compatible with  
 tight\_layout, so results might be incorrect.  
 import sys



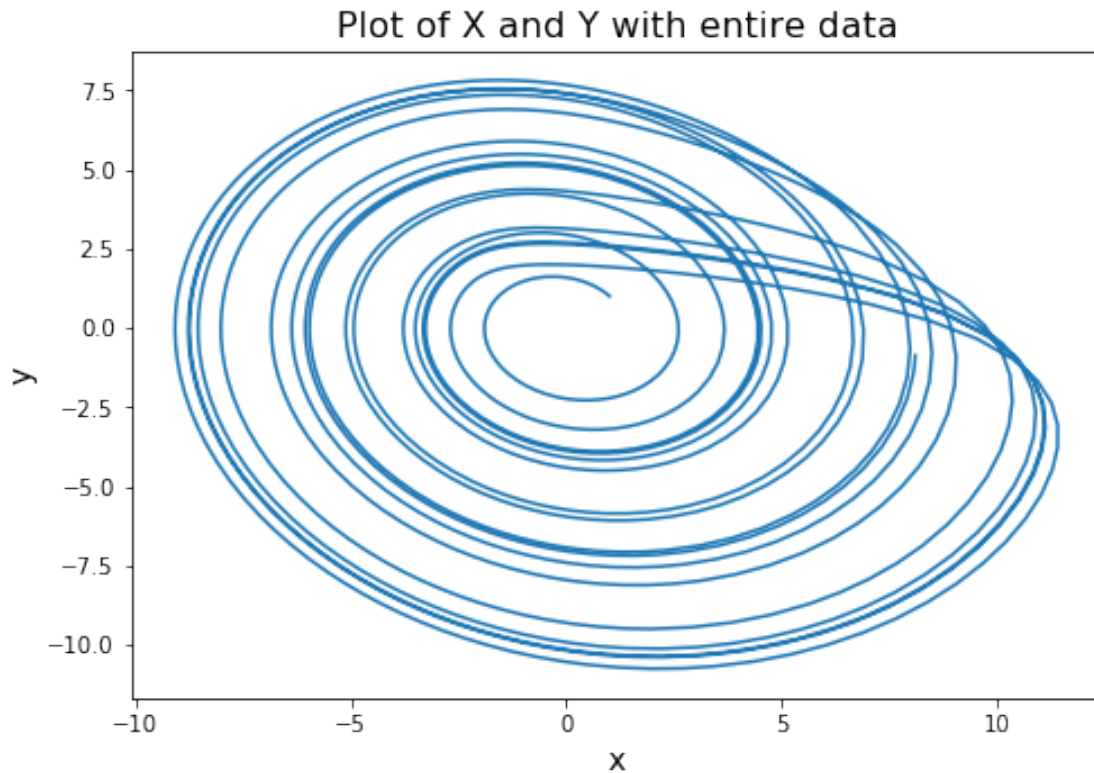
```
[12]: from mpl_toolkits import mplot3d
fig = plt.figure()
ax = plt.axes(projection="3d")

ax.plot3D(df.x, df.y, df.z, 'blue')
ax.set_xlabel('x')
ax.set_ylabel('y')
ax.set_zlabel('z')
plt.savefig(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↳Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler\3D_Plot_X_Y_Z_entire_
↳png", bbox_inches = "tight")
plt.show()
```



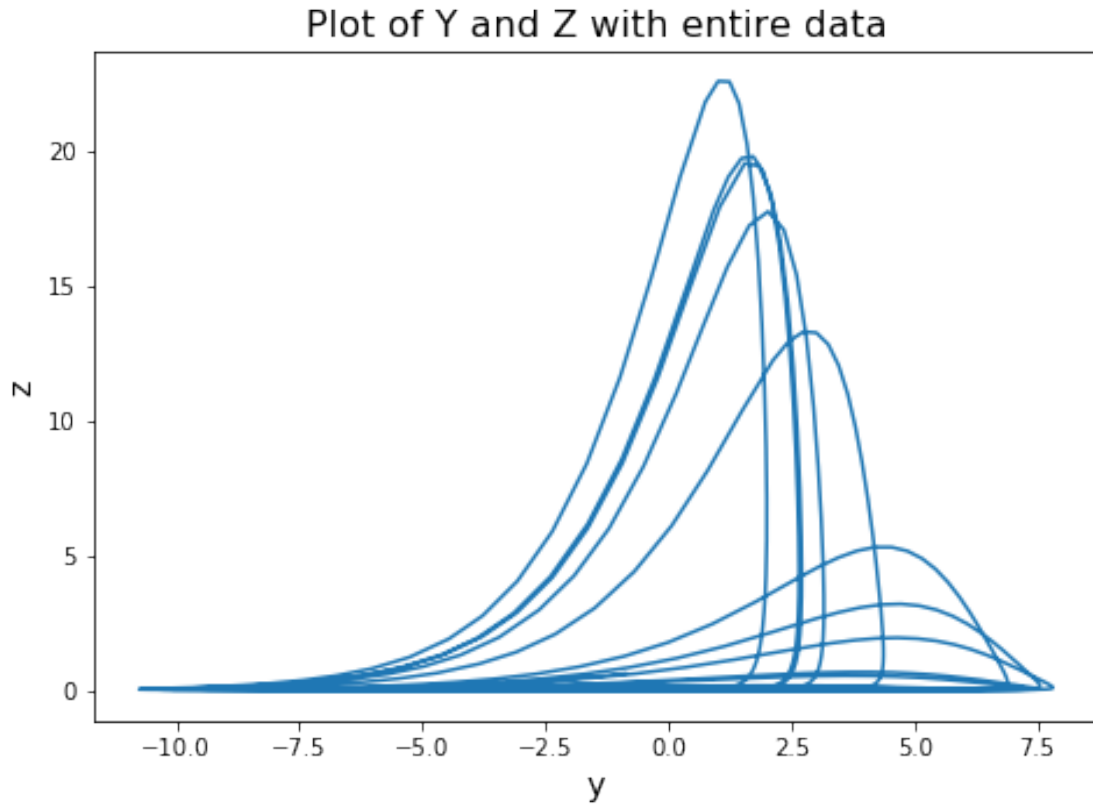
```
[13]: fig = plt.figure()
ax=fig.add_axes([0,0,1,1])
ax.plot(df['x'],df['y'] )
plt.title('Plot of X and Y with entire data', fontsize=16)
plt.xlabel('x', fontsize = 14)
plt.ylabel('y', fontsize = 14)
plt.savefig(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↳Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler\X_Y_on_Entire_data.
↳png", bbox_inches = "tight")
plt.show()
```

C:\Users\INFO-DSK-02\Anaconda3\lib\site-packages\ipykernel\_launcher.py:7:  
 UserWarning: This figure includes Axes that are not compatible with  
 tight\_layout, so results might be incorrect.  
 import sys



```
[14]: fig = plt.figure()
ax=fig.add_axes([0,0,1,1])
ax.plot(df['y'],df['z'] )
plt.title('Plot of Y and Z with entire data', fontsize=16)
plt.xlabel('y', fontsize = 14)
plt.ylabel('z', fontsize = 14)
plt.savefig(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↳Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler\Y_Z_on_
↳Entire_data.png", bbox_inches = "tight")
plt.show()
```

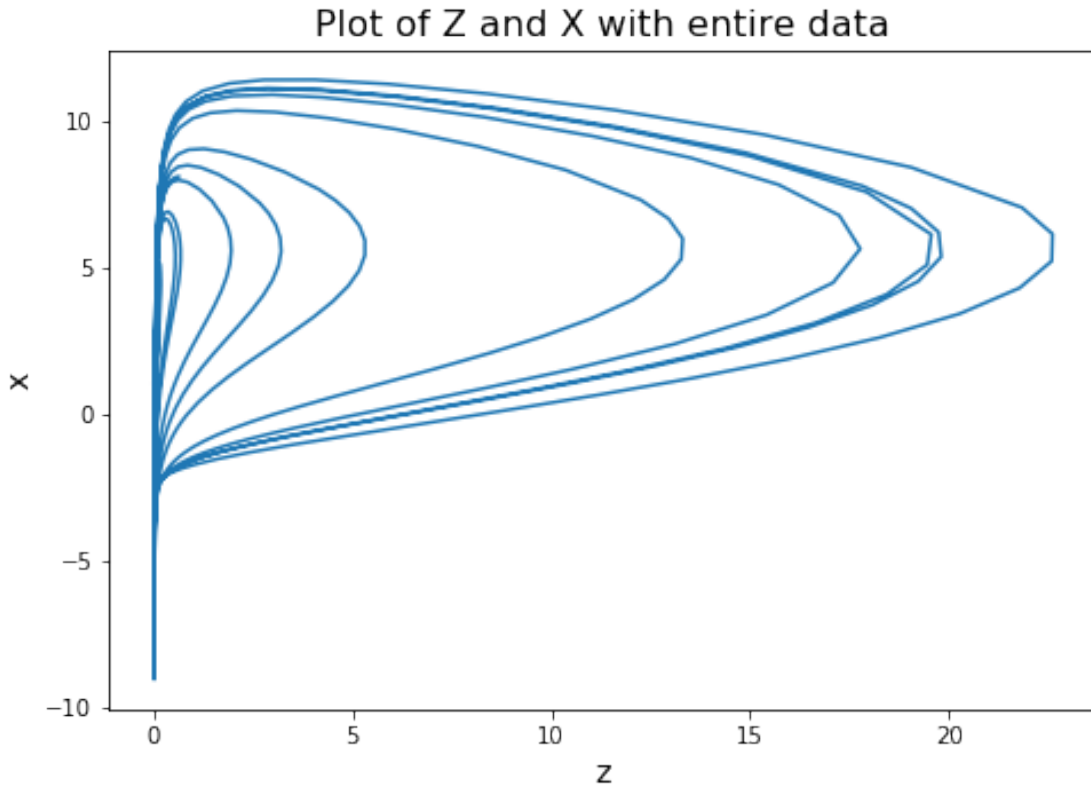
C:\Users\INFO-DSK-02\Anaconda3\lib\site-packages\ipykernel\_launcher.py:7:  
 UserWarning: This figure includes Axes that are not compatible with  
 tight\_layout, so results might be incorrect.  
 import sys



```
[15]: fig = plt.figure()
ax=fig.add_axes([0,0,1,1])
ax.plot(df['z'],df['x'] )
plt.title('Plot of Z and X with entire data', fontsize=16)
plt.xlabel('z', fontsize = 14)
plt.ylabel('x', fontsize = 14)
plt.savefig(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↳Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler\Z_X_on_
↳Entire_data.png", bbox_inches = "tight")
plt.show()
```

C:\Users\INFO-DSK-02\Anaconda3\lib\site-packages\ipykernel\_launcher.py:7:  
 UserWarning: This figure includes Axes that are not compatible with  
 tight\_layout, so results might be incorrect.  
 import sys





### 2.0.1 Split data for training and testing and creating teaches to train ESN on Input data

```
[16]: data_in = df[['x','y','z']]
      data_T =df['t']
```

```
[17]: data_in = np.array(data_in)
      data_t = np.array(data_T)
```

```
[18]: train_in = np.array(data_in[0:trainLen])
      train_out = np.array(data_in[0+10:trainLen+10])
      test_in = np.array(data_in[trainLen:trainLen+testLen])
      test_out = np.array(data_in[trainLen+10:trainLen+testLen+10])
```

```
[19]: train_in_t = np.array(data_T[0:trainLen])
      train_out_t = np.array(data_T[0+10:trainLen])
      test_in_t = np.array(data_T[trainLen:trainLen+testLen])
      test_out_t = np.array(data_T[trainLen+10:trainLen+testLen+10])
```

```
[20]: len(test_in_t)
```

[20]: 700

### 2.0.2 Modify Parameters to tune ESN for better fit

```
[21]: n_reservoir = 400 # number of recurrent units
      leak_rate = 0.2 # leaking rate (=1/time_constant_of_neurons)
      spectral_radius = 1.1 # Scaling of recurrent matrix
      input_scaling = 1. # Scaling of input matrix
      proba_non_zero_convec_W = 0.2 # Sparsity of recurrent matrix: Perceptage of
      ↪non-zero connections in W matrix
      proba_non_zero_convec_Win = 1. # Sparsity of input matrix
      proba_non_zero_convec_Wfb = 1. # Sparsity of feedback matrix
      regularization_coef = 0.1 #None # regularization coefficient, if None,
      ↪pseudo-inverse is use instead of ridge regression
```

```
[22]: n_inputs = 3
      input_bias = True # add a constant input to 1
      n_outputs = 3
```

```
[23]: N = n_reservoir#100
      dim_inp = n_inputs #26
```

### 2.0.3 Generating weights for input and hidden layers

```
[24]: ### Generating random weight matrices with custom method
      W = np.random.rand(N,N) - 0.5
      if input_bias:
          Win = np.random.rand(N,dim_inp+1) - 0.5
      else:
          Win = np.random.rand(N,dim_inp) - 0.5
      Wfb = np.random.rand(N,n_outputs) - 0.5
```

```
[25]: ## delete the fraction of connections given the sparsity (i.e. proba of
      ↪non-zero connections):
      mask = np.random.rand(N,N) # create a mask Uniform[0;1]
      W[mask > proba_non_zero_convec_W] = 0 # set to zero some connections given by
      ↪the mask
      mask = np.random.rand(N,Win.shape[1])
      Win[mask > proba_non_zero_convec_Win] = 0
      # mask = np.random.rand(N,Wfb.shape[1])
      # Wfb[mask > proba_non_zero_convec_Wfb] = 0
```

```
[26]: ## SCALING of matrices
      # scaling of input matrix
      Win = Win * input_scaling
      # scaling of recurrent matrix
```

```
# compute the spectral radius of these weights:
print( 'Computing spectral radius...')
original_spectral_radius = np.max(np.abs(np.linalg.eigvals(W)))
#TODO: check if this operation is quicker: max(abs(linalg.eig(W)[0])) #from
↳scipy import linalg
print( "default spectral radius before scaling:", original_spectral_radius)
# rescale them to reach the requested spectral radius:
W = W * (spectral_radius / original_spectral_radius)
print( "spectral radius after scaling", np.max(np.abs(np.linalg.eigvals(W))))
```

```
Computing spectral radius...
default spectral radius before scaling: 2.6206385401678642
spectral radius after scaling 1.0999999999999956
```

## 2.1 Input data dimensions

```
[27]: print('Dimensions of Training data: ', train_in.shape[1])
      print('Dimensions of Testing data: ', test_in.shape[1])
```

```
Dimensions of Training data: 3
Dimensions of Testing data: 3
```

### 2.1.1 Pass Parameters to ESN

```
[28]: reservoir = ESN.ESN(lr=leak_rate, W=W, Win=Win, input_bias=input_bias,
↳ridge=regularization_coef, Wfb=None, fbfunc=None)
```

## 2.2 Input data to reservoir model

```
[29]: internal_trained = reservoir.train(inputs=[train_in], teachers=[train_out],
↳wash_nr_time_step=initLen, verbose=False)
output_pred, internal_pred = reservoir.run(inputs=[test_in,], reset_state=False)
errorLen = len(test_out[:]) #testLen #2000
```

## 2.3 Dimensions of the output data

```
[30]: print('Shape of Output data Dimensions: ', output_pred[0].shape[1])
```

```
Shape of Output data Dimensions: 3
```

### 2.3.1 Create dataframe for predicted values and test values

```
[31]: import pandas as pd
      df_pred = pd.DataFrame(output_pred[0])
```

```
[32]: output_pred[0].shape
```

```
[32]: (700, 3)
```

```
[33]: test_out = pd.DataFrame(test_out)
```

### 2.3.2 MSE for X

```
[34]: ## printing errors made on test set
# mse = sum( np.square( test_out[:] - output_pred[0] ) ) / errorLen
# print( 'MSE = ' + str( mse ) )
mse_x = np.mean((test_out[0][:] - df_pred[0])**2) # Mean Squared Error: see
↳https://en.wikipedia.org/wiki/Mean_squared_error
rmse_x = np.sqrt(mse_x) # Root Mean Squared Error: see https://en.wikipedia.org/
↳wiki/Root-mean-square_deviation for more info
nmrse_mean_x = abs(rmse_x / np.mean(test_out[0][:])) # Normalised RMSE (based
↳on mean)
nmrse_maxmin_x = rmse_x / abs(np.max(test_out[0][:]) - np.min(test_out[0][:]))
↳# Normalised RMSE (based on max - min)
```

```
[35]: print("\n***** MSE and RMSE for Predictions on X *****")
print("Errors computed over %d time steps" % (errorLen))
print("\nMean Squared error (MSE) for x : \t\t%.4e " % (mse_x) )
print("Root Mean Squared error (RMSE) for x : \t\t%.4e\n " % rmse_x )
print("Normalized RMSE (based on mean) for x : \t%.4e " % (nmrse_mean_x) )
print("Normalized RMSE (based on max - min) for x : \t%.4e " % (nmrse_maxmin_x)
↳)
print("*****\n")
```

```
***** MSE and RMSE for Predictions on X *****
```

```
Errors computed over 700 time steps
```

```
Mean Squared error (MSE) for x :          8.9935e-02
```

```
Root Mean Squared error (RMSE) for x :    2.9989e-01
```

```
Normalized RMSE (based on mean) for x :    3.2858e-01
```

```
Normalized RMSE (based on max - min) for x : 1.5126e-02
```

```
*****
```

### 2.3.3 MSE for Y

```
[36]: ## printing errors made on test set
# mse = sum( np.square( test_out[:] - output_pred[0] ) ) / errorLen
# print( 'MSE = ' + str( mse ) )
mse_y = np.mean((test_out[1][:] - df_pred[1])**2) # Mean Squared Error: see
↳https://en.wikipedia.org/wiki/Mean_squared_error
```

```

rmse_y = np.sqrt(mse_x) # Root Mean Squared Error: see https://en.wikipedia.org/
↳wiki/Root-mean-square_deviation for more info
nmrse_mean_y = abs(rmse_y / np.mean(test_out[1][:])) # Normalised RMSE (based
↳on mean)
nmrse_maxmin_y = rmse_y / abs(np.max(test_out[1][:]) - np.min(test_out[1][:]))
↳# Normalised RMSE (based on max - min)

```

```

[37]: print("\n***** MSE and RMSE for Predictions on Y *****")
print("Errors computed over %d time steps" % (errorLen))
print("\nMean Squared error (MSE) for Y : \t\t%.4e " % (mse_y) )
print("Root Mean Squared error (RMSE) for Y : \t\t%.4e\n " % rmse_y )
print("Normalized RMSE (based on mean) for Y : \t%.4e " % (nmrse_mean_y) )
print("Normalized RMSE (based on max - min) for Y : \t%.4e " % (nmrse_maxmin_y))
↳)
print("*****\n")

```

\*\*\*\*\* MSE and RMSE for Predictions on Y \*\*\*\*\*

Errors computed over 700 time steps

Mean Squared error (MSE) for Y : 3.3645e-02

Root Mean Squared error (RMSE) for Y : 2.9989e-01

Normalized RMSE (based on mean) for Y : 1.3777e+00

Normalized RMSE (based on max - min) for Y : 1.6762e-02

\*\*\*\*\*

### 2.3.4 MSE for Z

```

[38]: ## printing errors made on test set
# mse = sum( np.square( test_out[:] - output_pred[0] ) ) / errorLen
# print( 'MSE = ' + str( mse ) )
mse_y = np.mean((test_out[2][:] - df_pred[1])**2) # Mean Squared Error: see
↳https://en.wikipedia.org/wiki/Mean_squared_error
rmse_y = np.sqrt(mse_x) # Root Mean Squared Error: see https://en.wikipedia.org/
↳wiki/Root-mean-square_deviation for more info
nmrse_mean_y = abs(rmse_y / np.mean(test_out[2][:])) # Normalised RMSE (based
↳on mean)
nmrse_maxmin_y = rmse_y / abs(np.max(test_out[2][:]) - np.min(test_out[2][:]))
↳# Normalised RMSE (based on max - min)

```

```

[39]: print("\n***** MSE and RMSE for Predictions on Z *****")
print("Errors computed over %d time steps" % (errorLen))
print("\nMean Squared error (MSE) for Z : \t\t%.4e " % (mse_y) )
print("Root Mean Squared error (RMSE) for Z : \t\t%.4e\n " % rmse_y )
print("Normalized RMSE (based on mean) for Z : \t%.4e " % (nmrse_mean_y) )

```

```
print("Normalized RMSE (based on max - min) for Z : \t%.4e " % (nmrse_maxmin_y)\n")
print("*****\n")
```

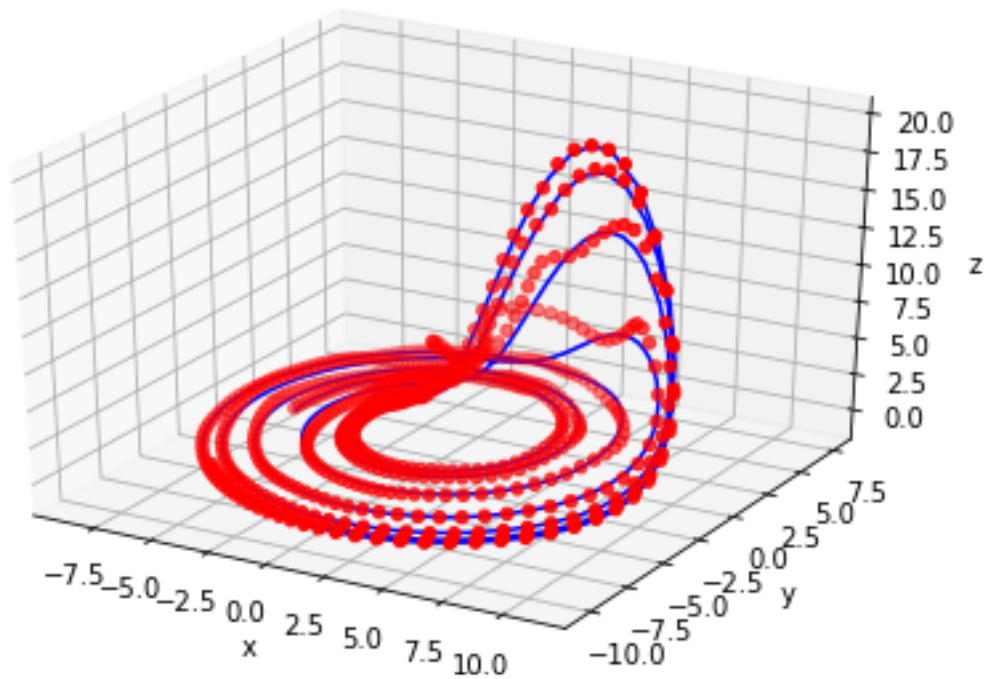
\*\*\*\*\* MSE and RMSE for Predictions on Z \*\*\*\*\*  
 Errors computed over 700 time steps

Mean Squared error (MSE) for Z : 2.9563e+01  
 Root Mean Squared error (RMSE) for Z : 2.9989e-01

Normalized RMSE (based on mean) for Z : 3.0044e-01  
 Normalized RMSE (based on max - min) for Z : 1.5347e-02  
 \*\*\*\*\*

### 3 3D Plot with predicted and actual values

```
[40]: from mpl_toolkits import mplot3d
fig = plt.figure()
ax = plt.axes(projection="3d")
ax.plot3D(test_out[0], test_out[1], test_out[2], 'blue')
ax.set_xlabel('x')
ax.set_ylabel('y')
ax.set_zlabel('z')
ax.scatter3D(df_pred[0], df_pred[1], df_pred[2], c='r')
plt.savefig(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension\
Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler\3D_Plot_X_Y_Z_entire_
png", bbox_inches = "tight")
plt.show()
```

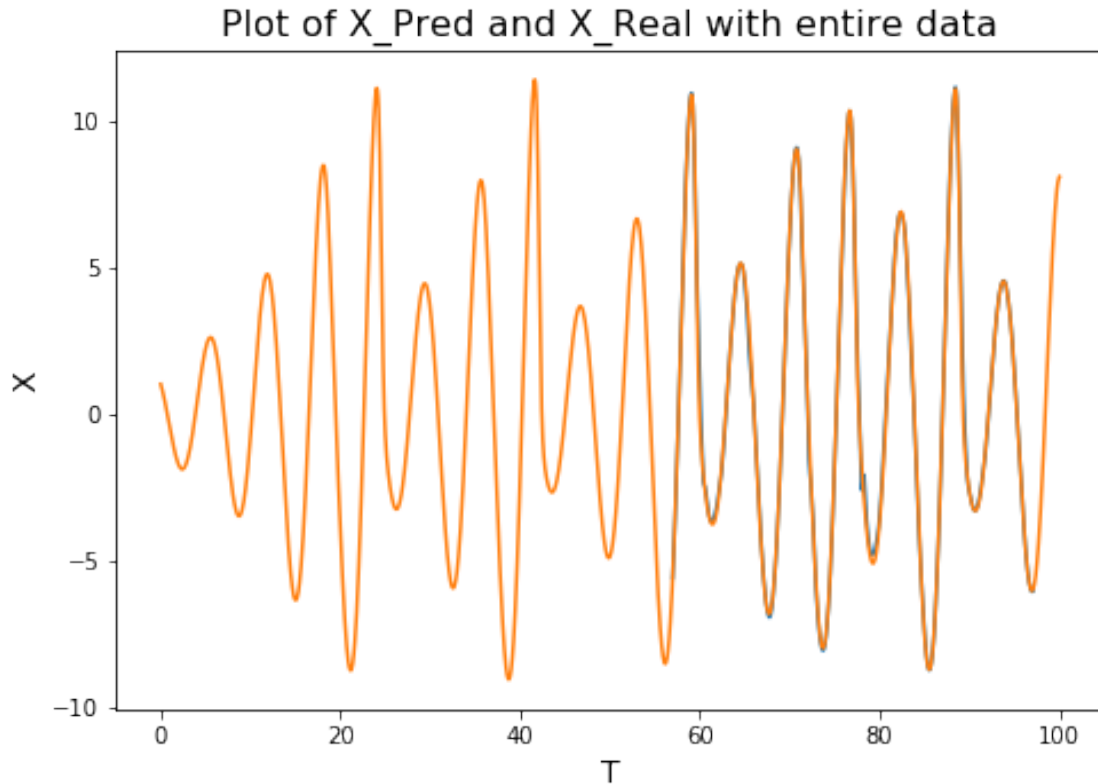


```
[41]: len(df_pred[0])
```

```
[41]: 700
```

```
[42]: fig = plt.figure()
ax=fig.add_axes([0,0,1,1])
ax.plot(test_out_t,df_pred[0])
plt.title('Plot of X_Pred and X_Real with entire data', fontsize=16)
plt.xlabel('T', fontsize = 14)
plt.ylabel('X', fontsize = 14)
ax.plot(df['t'],df['x'])
plt.savefig(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↳Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler\X_Pred_X_Real_on_
↳Entire_data.png", bbox_inches = "tight")
plt.show()
```

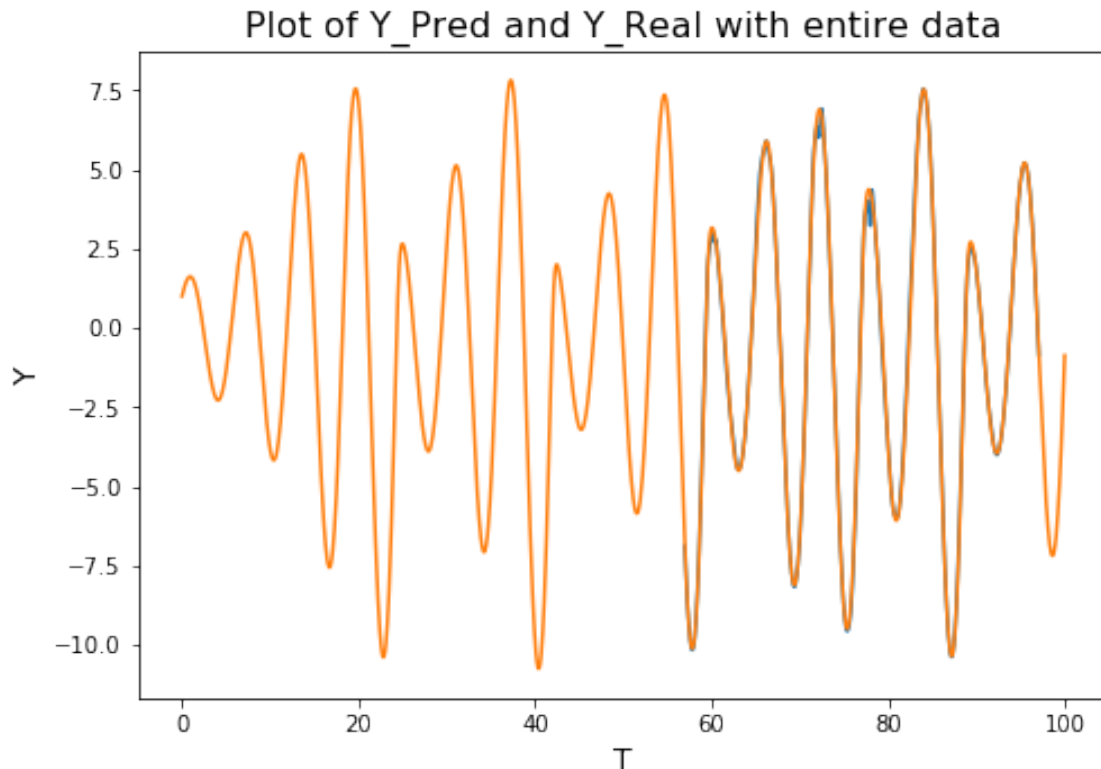
C:\Users\INFO-DSK-02\Anaconda3\lib\site-packages\ipykernel\_launcher.py:8:  
UserWarning: This figure includes Axes that are not compatible with  
tight\_layout, so results might be incorrect.



```
[43]: fig = plt.figure()
ax=fig.add_axes([0,0,1,1])
ax.plot(test_out_t,df_pred[1])
plt.title('Plot of Y_Pred and Y_Real with entire data', fontsize=16)
plt.xlabel('T', fontsize = 14)
plt.ylabel('Y', fontsize = 14)
ax.plot(df['t'],df['y'])
plt.savefig(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↳Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler\Y_Pred_Y_Real_on_
↳Entire_data.png", bbox_inches = "tight")
plt.show()
```

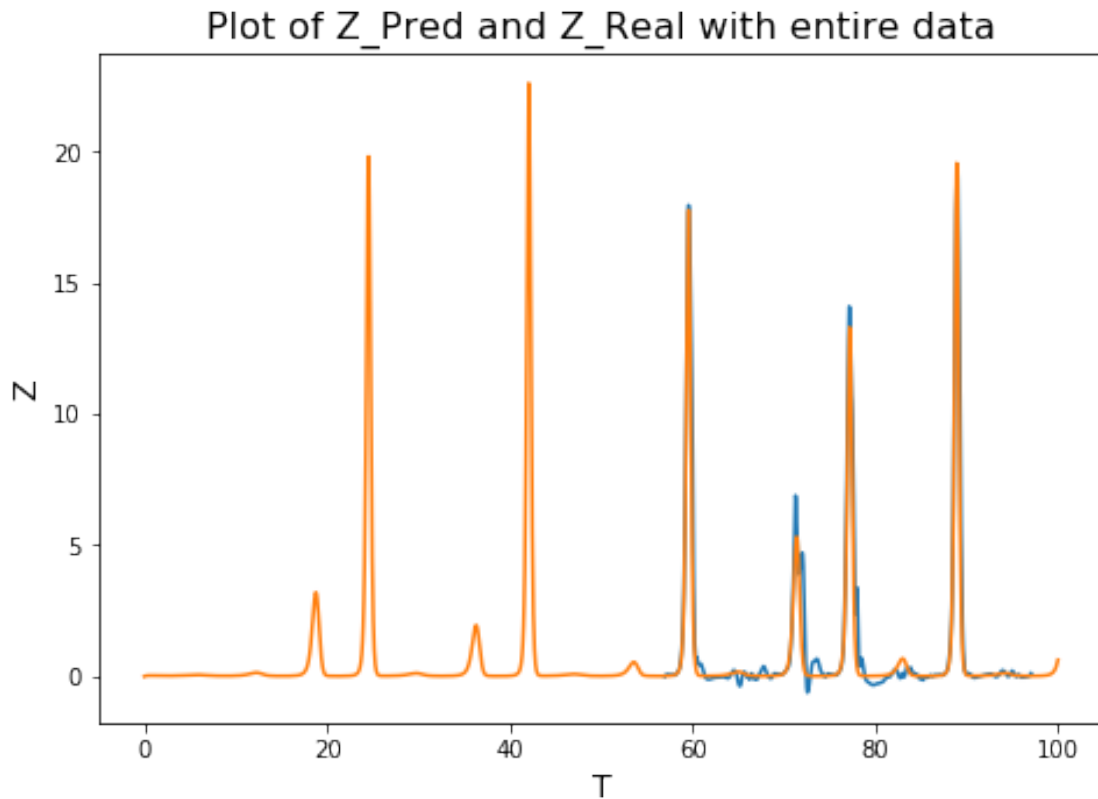
C:\Users\INFO-DSK-02\Anaconda3\lib\site-packages\ipykernel\_launcher.py:8:  
UserWarning: This figure includes Axes that are not compatible with  
tight\_layout, so results might be incorrect.





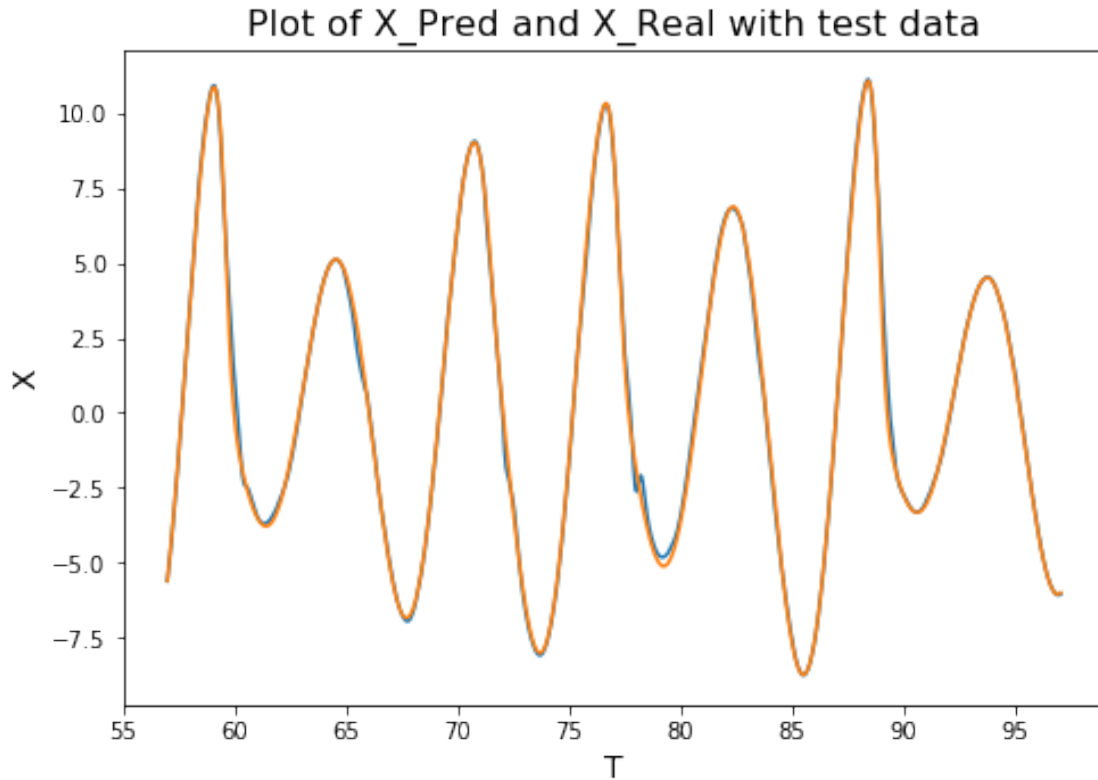
```
[44]: fig = plt.figure()
ax=fig.add_axes([0,0,1,1])
ax.plot(test_out_t,df_pred[2])
plt.title('Plot of Z_Pred and Z_Real with entire data', fontsize=16)
plt.xlabel('T', fontsize = 14)
plt.ylabel('Z', fontsize = 14)
ax.plot(df['t'],df['z'])
plt.savefig(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↳Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler\Z_Pred_Z_Real_on_
↳Entire_data.png", bbox_inches = "tight")
plt.show()
```

C:\Users\INFO-DSK-02\Anaconda3\lib\site-packages\ipykernel\_launcher.py:8:  
UserWarning: This figure includes Axes that are not compatible with  
tight\_layout, so results might be incorrect.



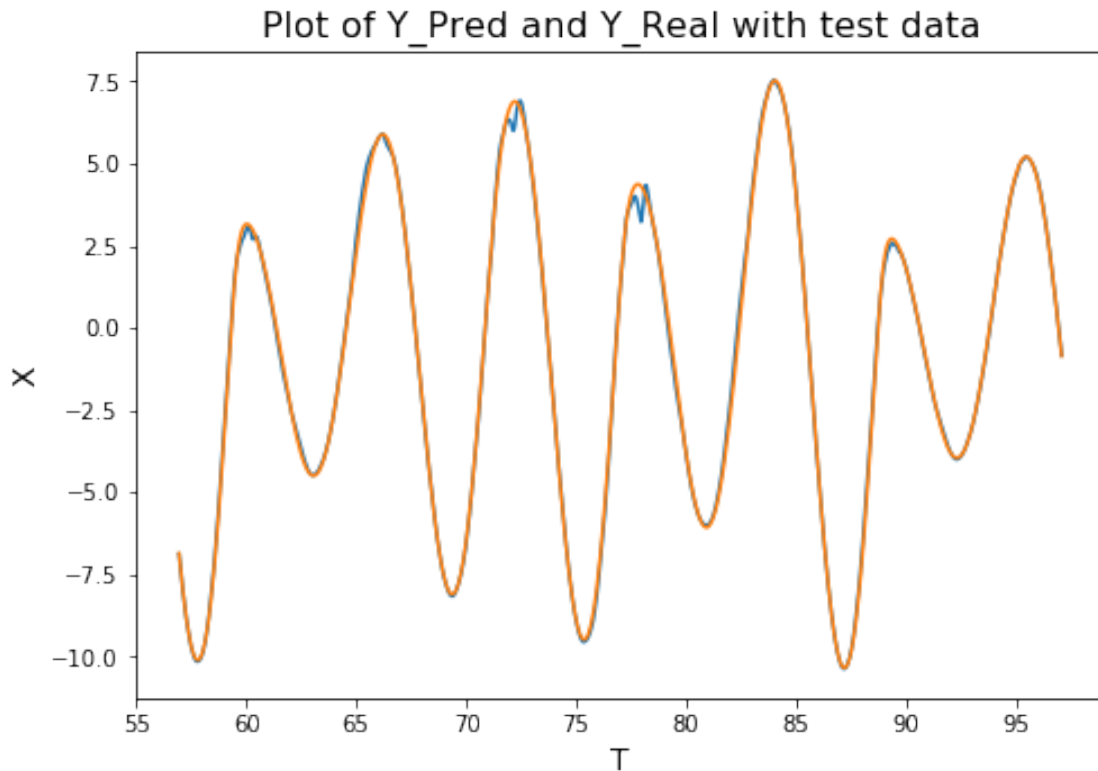
```
[45]: fig = plt.figure()
ax=fig.add_axes([0,0,1,1])
ax.plot(test_out_t,df_pred[0])
plt.title('Plot of X_Pred and X_Real with test data', fontsize=16)
plt.xlabel('T', fontsize = 14)
plt.ylabel('X', fontsize = 14)
ax.plot(test_out_t,test_out[0])
plt.savefig(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimensional_
↳Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler\X_pred_vs_X_Real_with
↳png", bbox_inches = "tight")
plt.show()
```

C:\Users\INFO-DSK-02\Anaconda3\lib\site-packages\ipykernel\_launcher.py:8:  
UserWarning: This figure includes Axes that are not compatible with  
tight\_layout, so results might be incorrect.



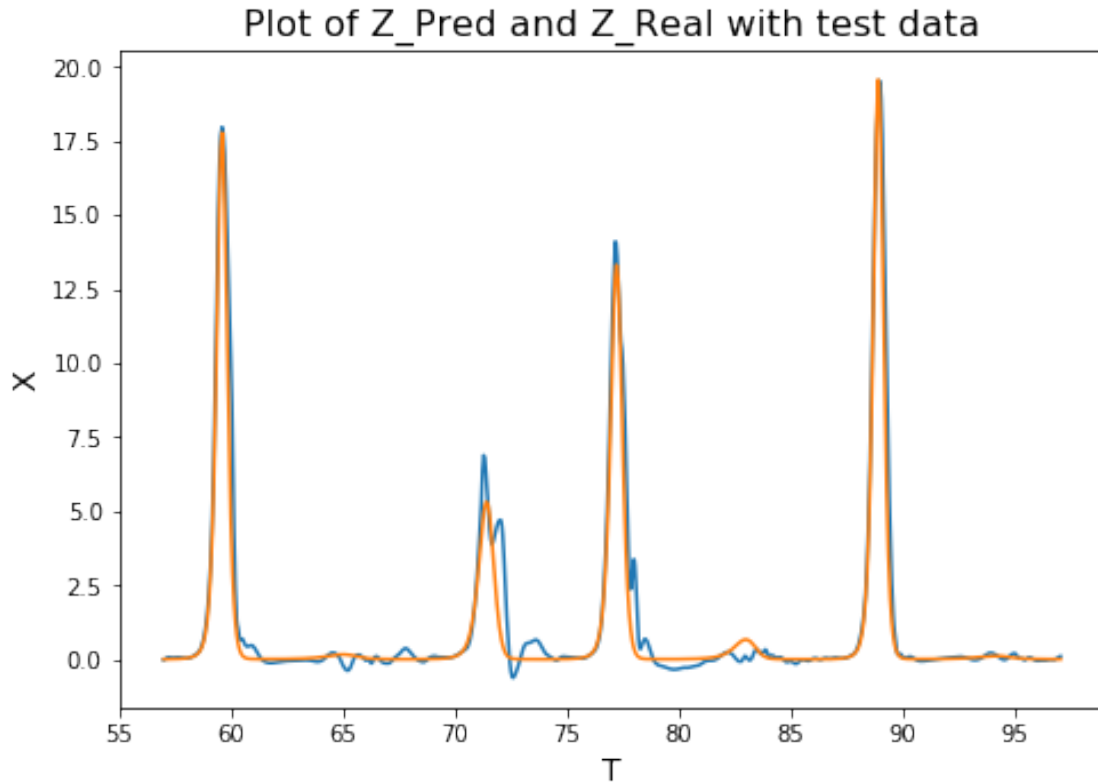
```
[46]: fig = plt.figure()
ax=fig.add_axes([0,0,1,1])
ax.plot(test_out_t,df_pred[1])
plt.title('Plot of Y_Pred and Y_Real with test data', fontsize=16)
plt.xlabel('T', fontsize = 14)
plt.ylabel('X', fontsize = 14)
ax.plot(test_out_t,test_out[1])
plt.savefig(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↪Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler\Y_pred_vs_Y_Real_with
↪png", bbox_inches = "tight")
plt.show()
```

C:\Users\INFO-DSK-02\Anaconda3\lib\site-packages\ipykernel\_launcher.py:8:  
 UserWarning: This figure includes Axes that are not compatible with  
 tight\_layout, so results might be incorrect.



```
[47]: fig = plt.figure()
ax=fig.add_axes([0,0,1,1])
ax.plot(test_out_t,df_pred[2])
plt.title('Plot of Z_Pred and Z_Real with test data', fontsize=16)
plt.xlabel('T', fontsize = 14)
plt.ylabel('X', fontsize = 14)
ax.plot(test_out_t,test_out[2])
plt.savefig(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↳Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler\Z_pred_vs_Z_Real_with
↳png", bbox_inches = "tight")
plt.show()
```

C:\Users\INFO-DSK-02\Anaconda3\lib\site-packages\ipykernel\_launcher.py:8:  
UserWarning: This figure includes Axes that are not compatible with  
tight\_layout, so results might be incorrect.



#### 4 Plotting Local Error from predicted and actual values

```
[48]: df_local_error = pd.DataFrame()
```

```
[49]: df_local_error['X_Local_Error'] = test_out[0] - df_pred[0]
df_local_error['Y_Local_Error'] = test_out[1] - df_pred[1]
df_local_error['Z_Local_Error'] = test_out[2] - df_pred[2]
```

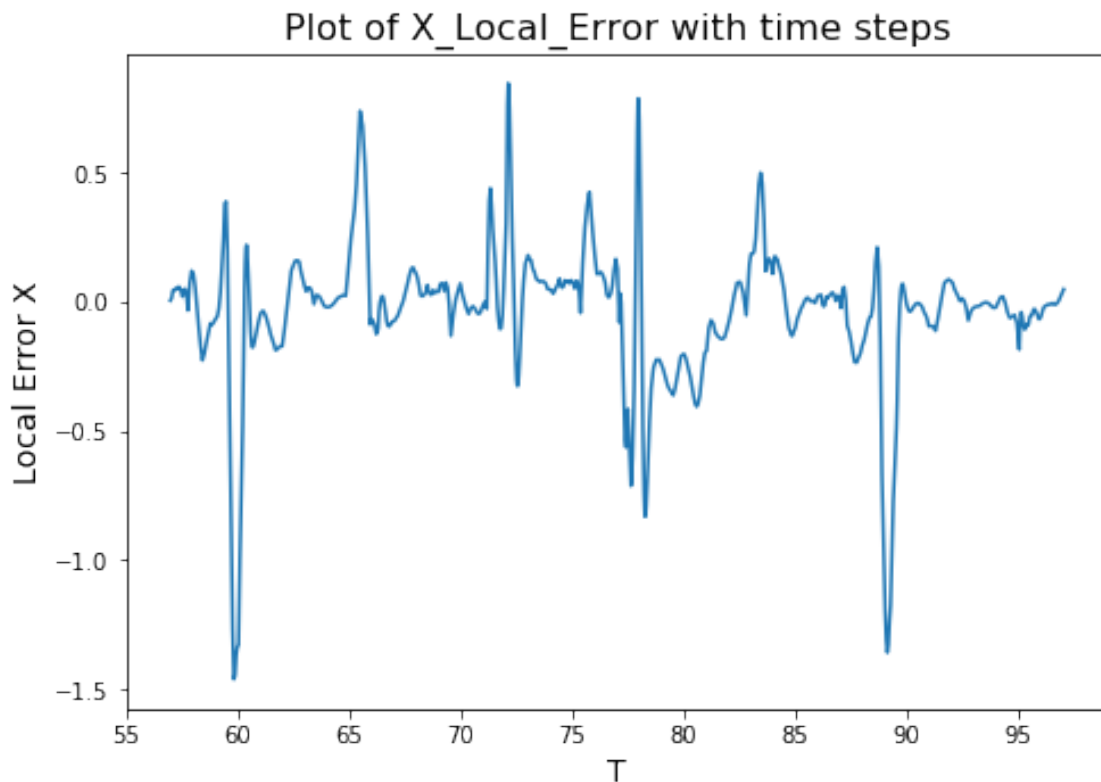
```
[50]: df_local_error.describe()
```

```
[50]:
```

	X_Local_Error	Y_Local_Error	Z_Local_Error
count	700.000000	700.000000	700.000000
mean	-0.058042	0.023551	-0.319826
std	0.294431	0.182038	0.898724
min	-1.461199	-0.609048	-5.363095
25%	-0.109939	-0.046879	-0.325064
50%	-0.015497	0.016382	-0.033417
75%	0.064458	0.071963	0.055664
max	0.845738	1.085623	0.689659

```
[51]: fig = plt.figure()
ax=fig.add_axes([0,0,1,1])
ax.plot(test_out_t,df_local_error['X_Local_Error'] )
plt.title('Plot of X_Local_Error with time steps', fontsize=16)
plt.xlabel('T', fontsize = 14)
plt.ylabel('Local Error X', fontsize = 14)
plt.savefig(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↳Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler\Y_Z_on_
↳Local_Error_X.png", bbox_inches = "tight")
plt.show()
```

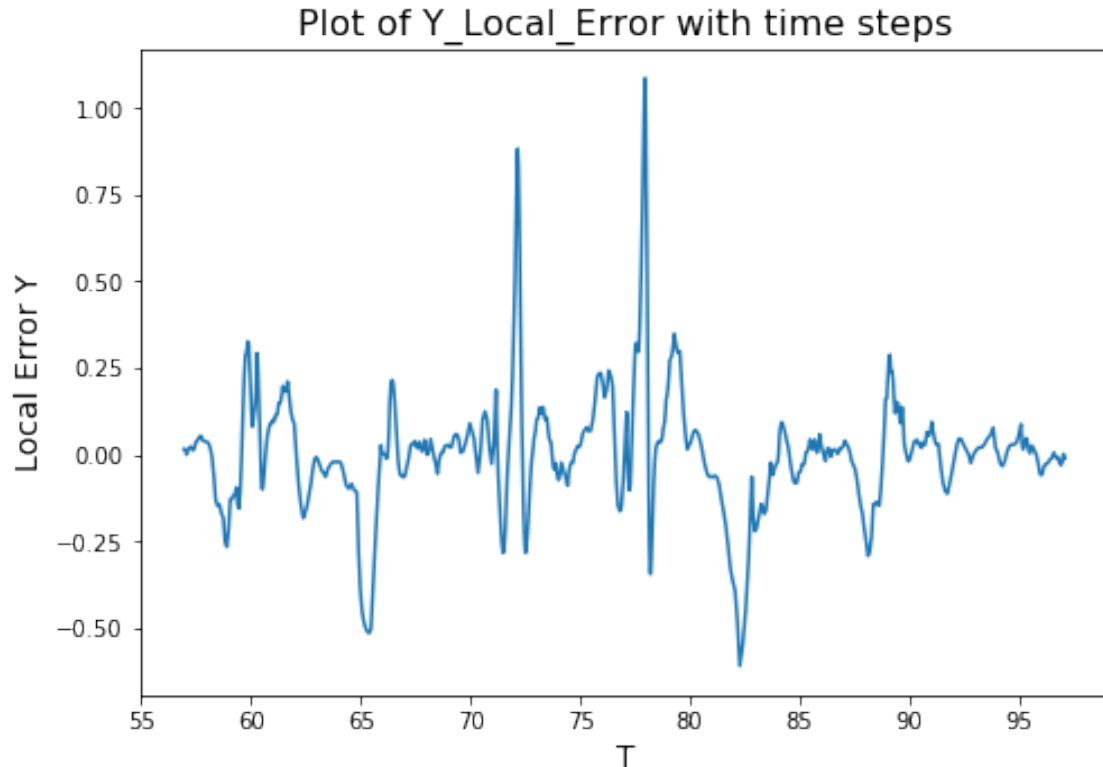
C:\Users\INFO-DSK-02\Anaconda3\lib\site-packages\ipykernel\_launcher.py:7:  
UserWarning: This figure includes Axes that are not compatible with  
tight\_layout, so results might be incorrect.  
import sys



```
[52]: fig = plt.figure()
ax=fig.add_axes([0,0,1,1])
ax.plot(test_out_t,df_local_error['Y_Local_Error'] )
plt.title('Plot of Y_Local_Error with time steps', fontsize=16)
plt.xlabel('T', fontsize = 14)
plt.ylabel('Local Error Y', fontsize = 14)
```

```
plt.savefig(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↳Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler\Y_Z_on_
↳Local_Error_Y.png", bbox_inches = "tight")
plt.show()
```

C:\Users\INFO-DSK-02\Anaconda3\lib\site-packages\ipykernel\_launcher.py:7:  
UserWarning: This figure includes Axes that are not compatible with  
tight\_layout, so results might be incorrect.  
import sys

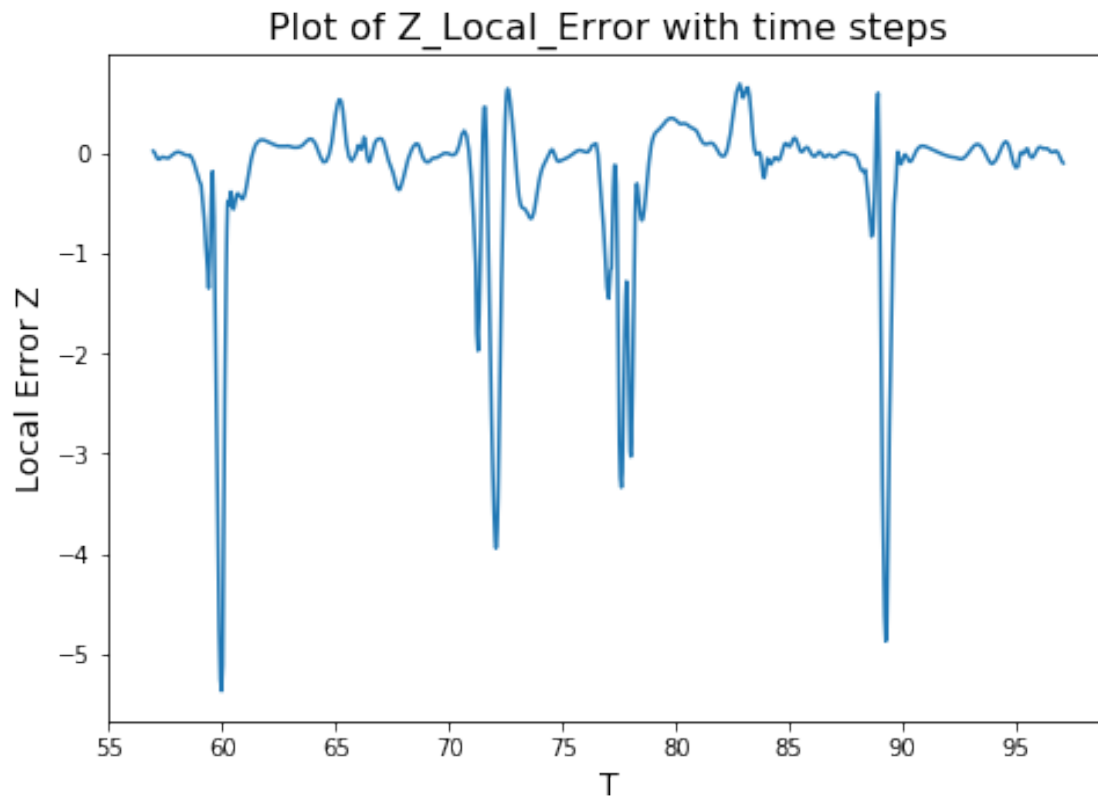


```
[53]: fig = plt.figure()
ax=fig.add_axes([0,0,1,1])
ax.plot(test_out_t,df_local_error['Z_Local_Error'] )
plt.title('Plot of Z_Local_Error with time steps', fontsize=16)
plt.xlabel('T', fontsize = 14)
plt.ylabel('Local Error Z', fontsize = 14)
plt.savefig(r"C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↳Prediction-Phase-2\Final_Version\3D_ReservoirComputing\images\Roseler\Y_Z_on_
↳Local_Error_Z.png", bbox_inches = "tight")
plt.show()
```

C:\Users\INFO-DSK-02\Anaconda3\lib\site-packages\ipykernel\_launcher.py:7:

UserWarning: This figure includes Axes that are not compatible with tight\_layout, so results might be incorrect.

```
import sys
```



```
[54]: df_pred.columns= ['X_pred', 'Y_pred', 'Z_pred']
```

```
[55]: df_pred.head()
```

```
[55]:
```

	X_pred	Y_pred	Z_pred
0	-5.614088	-6.887247	-0.001867
1	-5.212370	-7.284159	0.014969
2	-4.807194	-7.647914	0.044172
3	-4.398919	-7.980135	0.070426
4	-3.985817	-8.284720	0.081080

```
[56]: test_out.columns = ['X_test', 'Y_test', 'Z_test']
```

```
[57]: df_out = pd.concat([df_pred, test_out], axis = 1)
```

```
[58]: df_out['Test_T'] = test_out_t
```



```
[59]: df_out.to_excel(r'C:\Users\INFO-DSK-02\Desktop\Lorentz Multi Dimension_
↳ Prediction-Phase-2\Final_Version\3D_ReservoirComputing\Output\Reseler_Preds\Roseler_Output.
↳ xlsx', index= False)
```