

The Art of Presenting Science

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Greatest communicators

Who?

Bullshit Rules

Bullshit rule: 1
Work will speak for itself

On August 30, 2012 Mochizuki released four preprints, whose total size was about 500 pages, that develop [inter-universal Teichmüller theory](#) and apply it to attempt to prove several very famous problems in [Diophantine geometry](#).^[8] These include the strong [Szpiro conjecture](#), the hyperbolic [Vojta conjecture](#) and the [abc conjecture](#) over every number field. The preprints have not been published. In September 2018, Mochizuki posted a report on his work by [Peter Scholze](#) and [Jakob Stix](#) asserting that the third preprint contains an irreparable flaw; he also posted several documents containing his rebuttal of their criticism.^[9] The majority of number theorists have found Mochizuki's preprints very difficult to follow and have not accepted the conjectures as settled, although there are a few prominent exceptions, including Go Yamashita, [Ivan Fesenko](#), and Yuichiro Hoshi, who vouch for the work and have written expositions of the theory.^{[10][11]}

Reality Rules

Reality rule: 1

Your work: your product

Talk: advertisement of your work

Good product with bad advertisement ☹️

Bad product with good advertisement ☹️

Bullshit Rules

Bullshit rule: 2

Every slide must be packed from top left to bottom right with text

More in paper

Specific problem To determine the safety of inlining the lambda term let at the call site $\{(\ell \dots)\}$, we need to know that for every environment ρ in which this call is evaluated, that $\rho[x] = \langle \text{let}, \rho' \rangle$ and $\rho'(v) = \rho'(v)$ for each free variable v in the term let .²

$$\eta(b) = \hat{b} \text{ iff } \eta(g(b)) = \hat{g}(\hat{b}).$$

$$\frac{\hat{\beta}(e_i) \in \widehat{\text{Bind}}_1 \quad \hat{b}_i \in \widehat{\text{Bind}}_1}{\hat{\beta}(e_i) \equiv' \hat{b}_i},$$

$$\begin{aligned} g_B^{-1}(b) &= b \\ g_B^{-1}(g(b)) &= \begin{cases} b & \eta(b) = \eta(b') \text{ for some } g(b') \in B \\ g(b) & \text{otherwise} \end{cases} \\ g_B^{-1}(\text{lam}, \beta) &= (\text{lam}, g_B^{-1}(\beta)) \\ g_B^{-1}(\beta) &= \lambda v. g_B^{-1}(\beta(v)) \\ g_B^{-1}(ve) &= \lambda b. g_B^{-1}(ve(b)). \end{aligned}$$

Theorem 2. If $\alpha^q(\beta_1) = \hat{\beta}_1$ and $\alpha^q(\beta_2) = \hat{\beta}_2$, and $\hat{\beta}_1(v) = \hat{\beta}_2(v)$ and $\hat{\beta}_1(v) \in \widehat{\text{Bind}}_1$, then $\beta_1(v) = \beta_2(v)$.

Theorem 1. If $\alpha^q(\zeta) \subseteq \zeta$ and $\zeta \Rightarrow \zeta'$, then there exists a state ζ' such that $\zeta \Rightarrow \zeta'$ and $\alpha^q(\zeta') \subseteq \zeta'$.

$$\text{alloc} : \text{Var} \times \text{Time} \rightarrow \text{Bind}$$

$$\text{tick} : \text{Call} \times \text{Time} \rightarrow \text{Time}$$

$$\widehat{\text{alloc}} : \text{Var} \times \widehat{\text{Time}} \rightarrow \widehat{\text{Bind}}$$

$$\widehat{\text{tick}} : \text{Call} \times \widehat{\text{Time}} \rightarrow \widehat{\text{Time}}$$

$$\alpha^q(\text{call}, \beta, ve, t) = \langle \alpha^q(V), \alpha^q(\beta), \alpha^q(ve), \eta(t) \rangle$$

$$\alpha_{\text{BEnv}}^q(\beta) = \lambda v. \eta(\beta(v))$$

$$\alpha_{\text{VEnv}}^q(ve) = \lambda b. \bigcup_{\eta(b)=\hat{b}} \alpha^q(ve(b))$$

$$\alpha_b^q(d) = \{ \alpha_{[ve]}^q(d) \}$$

$$\alpha_{\text{Val}}^q(\text{lam}, \beta) = (\text{lam}, \alpha^q(\beta)).$$

Theorem 4. It is safe to rematerialize the expression e' in place of the expression e in the call site call off for every reachable compound abstract state of the form $\langle (\text{call}, \hat{\beta}', \hat{ve}, \hat{t}), \equiv \rangle$, it is the case that $\hat{E}(e', \hat{\beta}', \hat{ve}) = \langle \text{lam}', \hat{\beta}' \rangle$ and $\hat{E}(e, \hat{\beta}', \hat{ve}) = \langle \text{lam}, \hat{\beta} \rangle$ and the relation $\sigma \subseteq \text{Var} \times \text{Var}$ is a substitution that unifies the free variables of lam' with lam and for each $(v', v) \in \sigma$, $\hat{\beta}'(v') = \hat{\beta}(v)$.

Theorem 3. Given a compound abstract state $\langle (\text{call}, \hat{\beta}, \hat{ve}, \hat{t}), \equiv \rangle$ and two abstract bindings, \hat{b} and \hat{b}' , if $\alpha^q(\text{call}, \beta, ve, t) \subseteq \langle (\text{call}, \hat{\beta}, \hat{ve}, \hat{t}), \equiv \rangle$ and $\eta(b) = \hat{b}$ and $\eta(b') = \hat{b}'$ and $\hat{b} = \hat{b}'$, then $ve(b) = ve(b')$.

$$(\langle \langle \{f \ v_1 \dots v_n\}^{\hat{e}}, \hat{\beta}, \hat{ve}, \hat{t} \rangle, \equiv \rangle \rightsquigarrow \langle \langle \text{call}, \hat{\beta}', \hat{ve}', \hat{t}' \rangle, \equiv' \rangle), \text{ where:}$$

$$\hat{d}_i = \hat{E}(e_i, \hat{\beta}, \hat{ve})$$

$$\hat{d}_0 \ni \langle \langle \text{let}^q(v_1 \dots v_n) \text{ call} \rangle, \hat{\beta}' \rangle$$

$$\hat{t}' = \text{tick}(\text{call}, \hat{t})$$

$$\hat{b}_i = \widehat{\text{alloc}}(v_i, \hat{t}')$$

$$\hat{B} = \{ \hat{b}_i : \hat{b}_i \in \widehat{\text{Bind}}_1 \}$$

$$\hat{\beta}' = (\hat{g}_B^{-1} \hat{\beta}') [v_i \mapsto \hat{b}_i]$$

$$\hat{ve}' = (\hat{g}_B^{-1} \hat{ve}) \sqcup [\hat{b}_i \mapsto (\hat{g}_B^{-1} \hat{d}_i)],$$

$$(\langle \{f \ v_1 \dots v_n\}^{\hat{e}}, \hat{\beta}, \hat{ve}, \hat{t} \rangle \rightsquigarrow \langle \text{call}, \hat{\beta}', \hat{ve}', \hat{t}' \rangle), \text{ where:}$$

$$\hat{d}_i = \hat{E}(e_i, \hat{\beta}, \hat{ve})$$

$$\hat{d}_0 \ni \langle \langle \text{let}^q(v_1 \dots v_n) \text{ call} \rangle, \hat{\beta}' \rangle$$

$$\hat{t}' = \text{tick}(\text{call}, \hat{t})$$

$$\hat{b}_i = \widehat{\text{alloc}}(v_i, \hat{t}')$$

$$\hat{B} = \{ \hat{b}_i : \hat{b}_i \in \widehat{\text{Bind}}_1 \}$$

$$\hat{\beta}' = (\hat{g}_B^{-1} \hat{\beta}') [v_i \mapsto \hat{b}_i]$$

$$\hat{ve}' = (\hat{g}_B^{-1} \hat{ve}) \sqcup [\hat{b}_i \mapsto (\hat{g}_B^{-1} \hat{d}_i)],$$

$$\hat{\zeta} \in \hat{\Sigma} = \text{Call} \times \widehat{\text{BEnv}} \times \widehat{\text{VEnv}} \times \widehat{\text{Time}}$$

$$\hat{\beta} \in \widehat{\text{BEnv}} = \text{Var} \rightarrow \widehat{\text{Bind}}$$

$$\hat{ve} \in \widehat{\text{VEnv}} = \widehat{\text{Bind}} \rightarrow \hat{D}$$

$$\hat{d} \in \hat{D} = \mathcal{P}(\widehat{\text{Val}})$$

$$\widehat{\text{val}} \in \widehat{\text{Val}} = \widehat{\text{Clo}}$$

$$\widehat{\text{clo}} \in \widehat{\text{Clo}} = \text{Lam} \times \widehat{\text{BEnv}}$$

$$\hat{b} \in \widehat{\text{Bind}} \text{ is a finite set of bindings}$$

$$\hat{t} \in \widehat{\text{Time}} \text{ is a finite set of times}$$

Reality Rules

Reality rule: 2

Minimal text; Each slide should
showcase only one thing
YOU need to talk about the
content

Bullshit Rules

Bullshit rule: 3
Will convince my audience,
I have done LOTS of work

Reality Rules

Reality rule: 3
Quantity of work doesn't matter
Quality does

Bullshit Rules

Bullshit rule: 4
Pictures and Figures are pointless

Reality Rules

Reality rule: 4

**Picture is worth a thousand
words**

*Even in mathematical
communication*

Bullshit Rules

Bullshit rule: 5

Present every single step in proof
so that people will know I have
done it correctly

Reality Rules

Reality rule: 5

Writing an article is different from
presenting your work

Reality Rules

Reality rule: 5

Writing an article is different from
presenting your work
Encapsulate the ideas of the
theorems and proofs

Reality Rules

Reality rule: 5

Writing an article is different from
presenting your work
Encapsulate the ideas of the
theorems and proofs
True understanding

Bullshit Rules

Bullshit rule: 6
Don't talk about failures or
incorrect attempts

Reality Rules

Reality rule: 6
The path you took is more
important than result

Bullshit Rules

Bullshit rule: 7
Be serious;
No jokes, no deviations;
Only content

Reality Rules

Reality rule: 7
Your audience are not ROBOTS

Bullshit Rules

Bullshit rule: 8
Same content works for all
audience

Reality Rules

Reality rule: 8
Audience are our customers

Bullshit Rules

Bullshit rule: 9
No need to motivate the talk

Reality Rules

Reality rule: 9
Spend almost a quarter of the talk
on motivation

Bullshit Rules

Bullshit rule: 10

More slides \implies More work

Reality Rules

Reality rule: 10

If I Had More Time, I Would Have
Written a Shorter Letter.

Bullshit Rules

Bullshit rule: 11

Talk fast \implies More words \implies
More work

Reality Rules

Reality rule: 11
Talk short sentences at the right
pace.

Bullshit Rules

Bullshit rule: 12
Presentations should be
monologue.

Reality Rules

Reality rule: 12
Engage your audience.

Other points to remember

Have a catchy title

Other points to remember

Do not have an outline slide
It is boring; Suspense is lost

Other points to remember

Start with a question or an
interesting fact

Other points to remember

Start with a question or an
interesting fact
Use that as a motivation

Other points to remember

Tell a story
Build up the suspense

Other points to remember

Do not memorize your talk!

Other points to remember

Do not memorize your talk!
Try to adapt on the fly!

Other points to remember

Do not memorize your talk!
Try to adapt on the fly!
Extempore!

Other points to remember

You are the hero(ine)!

Other points to remember

You are the hero(ine)!

Don't become a villain!

Other points to remember

Show current slide/total slides

Other points to remember

Show current slide/total slides
Have a good climax

Other points to remember

Show current slide/total slides

Have a good climax

Finish on time with a bang!