

# Nomoto Model Evaluation

## Objective:

To evaluate the performance of first order nomoto model which will be used as an agent in reinforcement learning system for ship's navigation.

## Work done :

Model has been encoded in python

## First Order Nomoto Model:

$$T\dot{r} + r = K\delta$$

—(1)

by solving this first order linear equation, we can get the relation between yaw rate and given rudder angle,

$$r = K\delta_0 (1 - e^{-t/T})$$

—(2)

As we know that, from governing equation  $k$  and  $T$  are nomoto model parameters. in order to calculate these values,

$$\begin{aligned} I_z\dot{r} + mx_G(\dot{u} + u_0r) &= N \\ &= N_r.r + N_{\dot{r}}.\dot{r} + N_{\delta}.\delta \end{aligned}$$

rearranging this equation,

$$[I_z - N_{\dot{r}}]\dot{r} + [mx_Gu_0 - N_r]r = N_{\delta}.\delta$$

when converting into the form of governing equation,

$$\underbrace{\frac{[I_z - N_{\dot{r}}]}{[mx_Gu_0 - N_r]}}_T \dot{r} + r = \underbrace{\frac{N_{\delta}}{[mx_Gu_0 - N_r]}}_K \delta$$

—(3)

with standard reference from **I.T.T.C**,  $T$  and  $K$  values should follow the following range, Accordingly, it is considered that  $K$  indicates the angular velocity eventually reached, and therefore turning ability, and  $T$  indicates the quickness from moving from one stationary state to another stationary state *i.e* quick responsibility

$$\begin{aligned} T &\longrightarrow \text{ranging from 0.1 to 100} \\ K &\longrightarrow \text{ranging from 0 to 0.999} \end{aligned}$$

We can take this numerical values from MMG model, Yasukawa Paper which belongs to *KVLCC2* tanker ship,

$$\begin{aligned} x_G &= 11.2, \\ m &= 3.126 \times 10^8, \\ u_0 &= 7.75, \\ I_z &= 1.99 \times 10^{12} \\ N_d &= 5.8 \times 10^1 \\ N_r &= -1.3309 \times 10^1 \\ N_{\dot{r}} &= 1.199 \times 10^{12} \text{ (*subjected to change*) for this value } k = 0.49 \text{ and } T = 3.619 \end{aligned}$$

Here, Encoded Nomoto model is evaluated for constant  $T = 15$  and different set of  $K$  values, **80 step units** were taken for  $\delta = 35$  degree

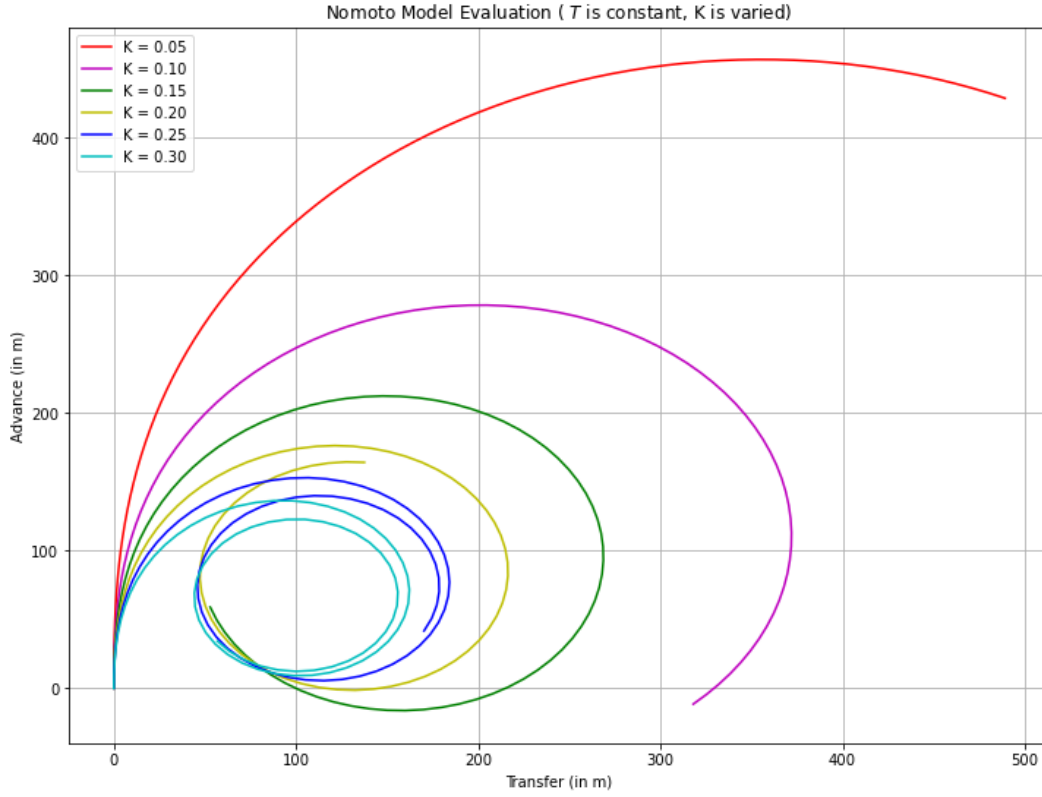


Figure 1 . Nomoto Model for  $T = C$  and different  $K$   
Source : *Nomotodof1.py*

Similarly, for constant  $K = 0.15$  and different  $T$  values, **80 step units** were taken for  $\delta = 35$  degree.

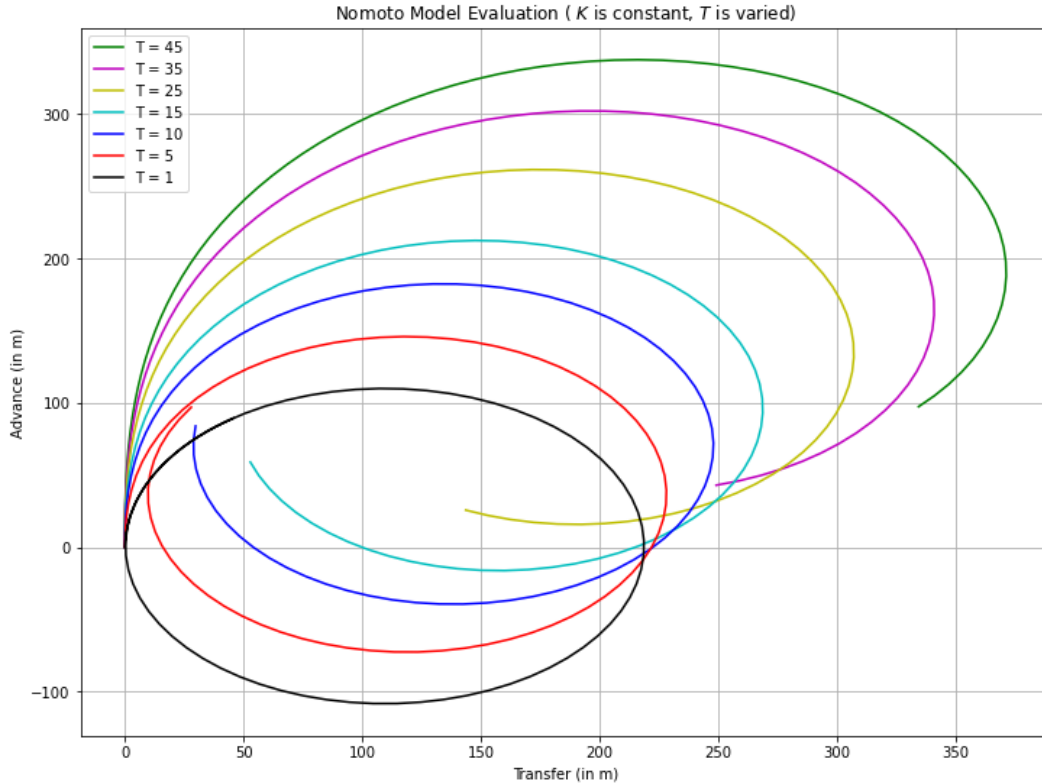


Figure 2 . Nomoto Model for  $K = C$  and different  $T$   
Source : *Nomotodof1.py*

Here, different combination of  $T$  and  $K$  values have been taken, **80 step units were taken** for  $\delta = 35$  degree.

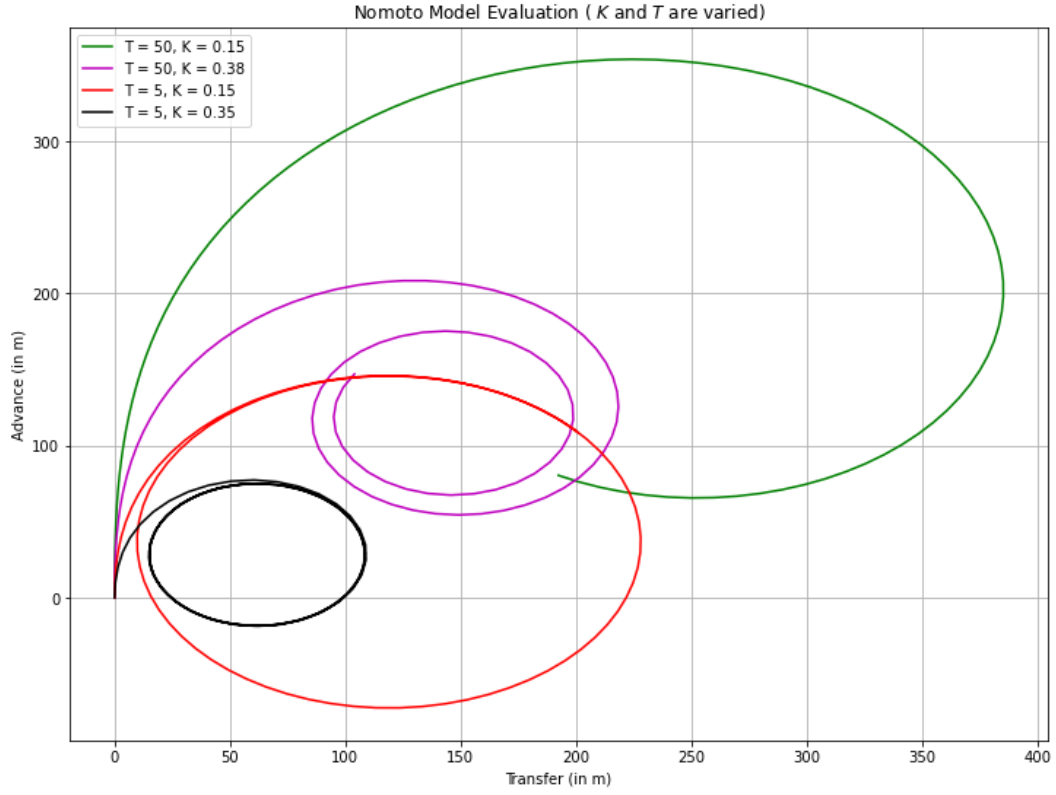


Figure 3 . Nomoto Model for different  $T$  and  $K$   
Source : *Nomotodof1.py*

At extend, Agent's action for straight line motion for any value of  $T$  and  $K$ , **100 step units were taken** for  $\delta = 0$  degree.

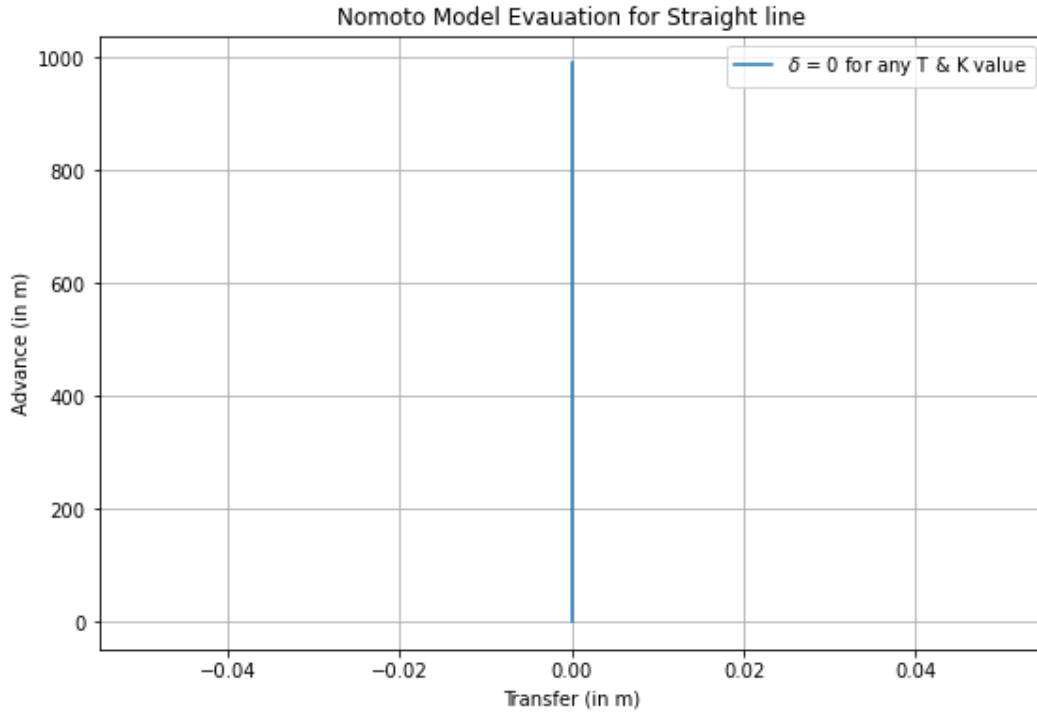


Figure 4 . Nomoto Model for straight line action  
Source : *Nomotodof1.py*

Here, the evaluation of *KVLCC2* ship model for aforementioned values **50 step units were taken** for  $\delta = 35$  degree.

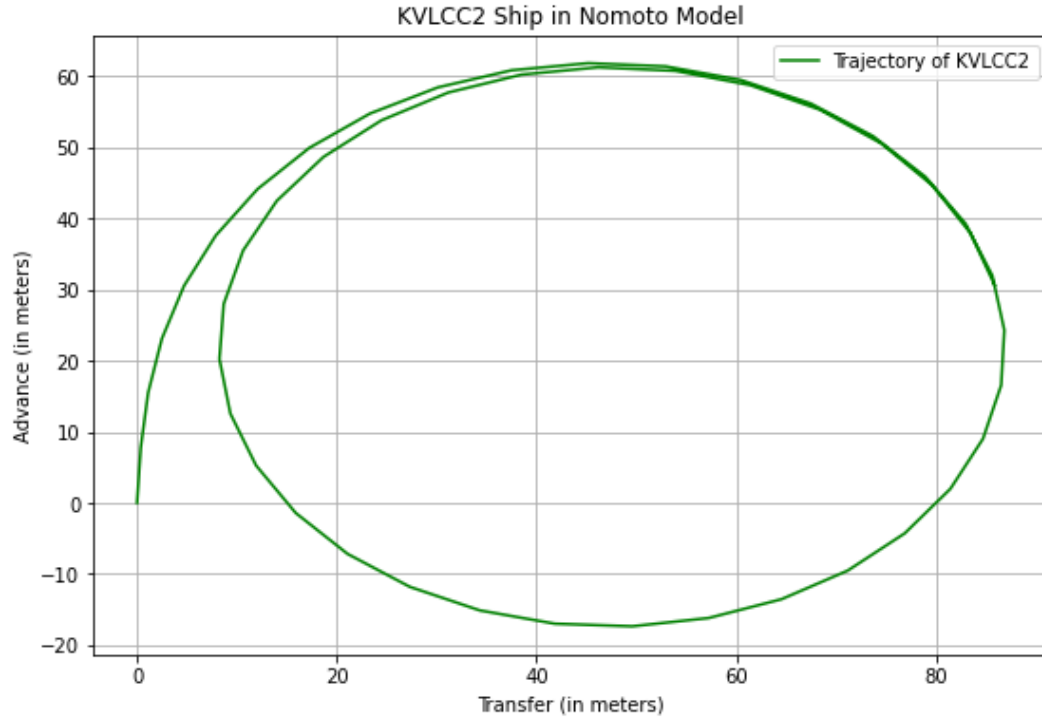


Figure 5 . *KVLCC2* ship evaluation with nomoto model  
Source : *Nomotodef1.py*