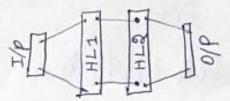
Policy Gradient



Policy Net - a Network - NN

Minimizing the F1 smooth loss, means, it is working for maximizing two consecutive action cumulative reward. -> Q-learning -

→ Policy Gradient → Sampling the episodes and optimizing the policy net by gradient ascent.

objective Function:

$$J(\theta) = E\left[\sum_{t=0}^{T-1} r_{t+1}\right] \longrightarrow 0$$

here, Nomenclature: {5, at, St+1, V++1}

Gradient Ascent:
$$\theta \leftarrow \theta + \frac{\partial}{\partial \theta} \left[J(\theta) \right] = --- \bigcirc$$

As we all know that, $E[f(x)] = \sum_{\alpha} P(x)f(x)$.

$$J(\theta) = E\left[\sum_{t=0}^{T-1} V_{t+1} | T_{\theta}\right]$$

$$J(\theta) = \sum_{t=0}^{T-1} P(S_{t}, a_{t}|T) r_{t+1} - - - - - G$$

i -> Arbitary Starting Point

T → Given Trajectory

Differentiating both sides with respect to policy Parameter of using $\frac{d}{dx} \left[\log f(x) \right] = \frac{f'(x)}{f(x)}$ $\nabla_{\theta} J(\theta) = \sum_{t=1}^{T-1} \nabla_{\theta} P(S_t, a_t | T) V_{t+1}$ $= \sum_{t=i}^{T-1} P(S_{t}, a_{t}|T) \cdot \frac{\nabla_{\theta} P(S_{t}, a_{t}|T)}{P(S_{t}, a_{t}|T)} r_{t+1}$ = \(\subseteq \text{P(St, at | T). V_t Log P(St, at | T). V_t+1}\) 50. Substituting in the equation 1, $\nabla_{\theta} J(\theta) = E \left[\sum_{t=1}^{T-1} \nabla_{\theta} \log P(s_{t}, a_{t}|T) V_{t+1} \right]$ This approximate can be done by re-writing the equation, $\nabla_{\theta} J(\theta) \sim \sum_{t=1}^{T-1} \nabla_{\theta} \log P(s_{t}, a_{t}|T) V_{t+1} = -6$ looking expression for Volog P(St, at | T), $P(S_t, a_t | T) = P(S_0, a_0, S_1, a_1, \dots, S_{t-1}, a_{t-1}, S_t, a_t | T_{\theta})$ = P(So) TTg(a,1So) P(S,1So, ao) TTg (a2151)P(52151, a TTA(a3152) P(S31S2,A2). P(St-11St-2, at-2) TA (at-11St-2) ... P(St | St-1, at-1) TTg(at, St

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here, the function term, Vo log P(St, At IT),
Volog P(St, atIT) = Volog P(So) + Volog To (ao1So) +
                             Volog P(S,150,a0) + Volog TTO (a2151)+.
                            ... + Volug P(St-1/St-2, at-2)
                                    + Volog A (at 15t-1)+.
                                + Va log P(St, St-1, at-1) + Va log Ta (at)
 Here, it is important to note that P(5+1St-1, 9+-1) is
 not dependant on the policy parameter & and solely
  dependant on environment reinforcement learning.
  \nabla_{\theta} \log P(S_{t}, a_{t}|T) = \sum_{t'=0}^{\infty} \nabla_{\theta} \log T_{\theta}(a_{t'}|S_{t'})
  from. Vo log P(St, atIT) = 0 + Volog Ta (a, 150) + 0+
                                    Valog TTA (a2152) +0+ ... +.
                                       .+0+ Volog Tta (at-115+-1)+
                                       ··· + Valog To (at 15ta)
         \nabla_{\theta} \log P(S_{t}, a_{t}|T) = \sum_{t'=0}^{t} \nabla_{\theta} \log \Pi_{\theta} (a_{t'}|S_{t'}) = ---6
  from equation 6) & 6, \nabla_{\theta} J(\theta) = \sum_{t=0}^{T-1} V_{t+1} \left\{ \sum_{t=0}^{t} \nabla_{\theta} \log T_{\theta} (a_{t} \cdot 15_{t}) \right\} - - - \Phi
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$$= V_{1} \left[\sum_{t'=0}^{0} \nabla_{\theta} \log \Pi_{\theta}(a_{t'}|S_{t'}) \right] + V_{2} \left[\sum_{t'=0}^{1} \nabla_{\theta} \log \Pi_{\theta}(a_{t'}|S_{t'}) \right]$$

$$+ V_{3} \left[\sum_{t'=0}^{a} \nabla_{\theta} \log \Pi_{\theta}(a_{t'}|S_{t'}) \right] + \dots$$

$$+ V_{T-1} \left[\sum_{t'=0}^{T-1} \nabla_{\theta} \log \Pi_{\theta}(a_{t'}|S_{t'}) \right]$$

$$= V_{1} \nabla_{\theta} \log \Pi_{\theta}(a_{0}|S_{0}) + V_{\theta} \left[\nabla_{\theta} \log \Pi_{\theta}(a_{0}|S_{0}) + \nabla_{\theta} \log \Pi_{\theta}(a_{1}|S_{1}) \right]$$

$$+ V_{3} \left[\nabla_{\theta} \log \Pi_{\theta}(a_{0}|S_{0}) + \nabla_{\theta} \log \Pi_{\theta}(a_{1}|S_{1}) + \nabla_{\theta} \log \Pi_{\theta}(a_{2}|S_{2}) \right]$$

$$+ \nabla_{\theta} \log \Pi_{\theta}(a_{0}|S_{0}) \left[V_{1} + V_{2} + V_{3} + \dots + V_{T} \right]$$

$$+ \nabla_{\theta} \log \Pi_{\theta}(a_{0}|S_{0}) \left[V_{1} + V_{2} + V_{3} + \dots + V_{T} \right]$$

$$+ \nabla_{\theta} \log \Pi_{\theta}(a_{1}|S_{1}) \left[V_{2} + V_{3} + \dots + V_{T} \right]$$

$$+ \nabla_{\theta} \log \Pi_{\theta}(a_{2}|S_{1}) \left[V_{3} + V_{4+1} + \dots + V_{T} \right]$$

$$+ \nabla_{\theta} \log \Pi_{\theta}(a_{1}|S_{1}) \left[V_{2} + V_{3} + \dots + V_{T} \right]$$

$$+ \nabla_{\theta} \log \Pi_{\theta}(a_{1}|S_{1}) \left[V_{2} + V_{3} + \dots + V_{T} \right]$$

$$+ \nabla_{\theta} \log \Pi_{\theta}(a_{1}|S_{1}) \left[V_{3} + V_{4+1} + \dots + V_{T} \right]$$

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$$+ \nabla_{\theta} \log \Pi_{\theta}(a_{1}|S_{1}) \left[V_{3} + V_{4+1} + \dots + V_{T} \right]$$

$$+ \nabla_{\theta} \log \Pi_{\theta}(a_{1}|S_{1}) \left[V_{4} + V_{4} + \dots + V_{T} \right]$$

$$+ \nabla_{$$

 $J(\theta) = E[\gamma^{0}r_{1} + \gamma^{0}r_{2} + \gamma^{0}r_{3} + \dots + \gamma^{0}r_{T-1}]TT_{\theta}]$ 1 - - - - - 0

We can perform a similar derivation to obtain,
$$\nabla_{\theta} J(\theta) = \sum_{t=0}^{T-1} \nabla_{\theta} \log T_{\theta}(a_{t}|S_{t}) \left[\sum_{t'=t+1}^{T} y^{t'-t-1} \right]$$
 and simplifying
$$\sum_{t'=0}^{T-1} y^{T'-t-1} r_{t'} \text{ to } G_{1t}$$

$$\nabla_{\theta} J(\theta) = \sum_{t=0}^{T-1} \nabla_{\theta} \log T_{\theta}(a_{t}|S_{t}) G_{1t}$$
 Policy update equation

Pseudo Code:

Initialise
$$\theta$$
 arbitarily for each episode $\{S_1, a_1, v_2, \ldots, S_{T-1}, a_{T-1}, v_7\}$ -TT_{\$\text{\$de}\$} for each episode $\{S_1, a_1, v_2, \ldots, S_{T-1}, a_{T-1}, v_7\}$ -TT_{\$\text{\$de}\$} for $t = 1$ to $t - 1$ do $\theta \leftarrow \theta + \alpha = 0$ To $\theta \leftarrow \theta + \alpha = 0$ To $\theta \leftarrow \theta + \alpha = 0$ To $\theta \leftarrow \theta = 0$ and for end for return $\theta \leftarrow \theta$