DS2 HW3

Siyan Chen 4/6/2019

(a) Produce some graphical summaries of the Weeklydata.

```
transparentTheme(trans = .4)
featurePlot(x = df[, 2:7],
                 y = df$Direction,
                 scales = list(x=list(relation = "free"),
                                    y=list(relation = "free")),
                 plot = "density", pch = "|")
                  Lag4
                                                          Lag5
                                                                                                Volume
                                                                               0.5
0.000.050.100.150.20
                                       0.000.050.100.150.20
                                                                               0.1 0.2 0.3 0.4
             -10
                                                     -10
                                                                                             2
     -20
                       0
                                10
                                            -20
                                                               0
                                                                        10
                                                                                        0
                                                                                                   4
                                                                                                        6
                                                                                                             8
                                                                                                                 10
                                                          Lag2
                  Lag1
                                                                                                  Lag3
                                                                               0.000.050.100.150.20
                                       0.000.050.100.150.20
0.000.050.100.150.20
                                10
                                                     -10
                                                               0
                                                                        10
                                                                                             -10
                                                                                                               10
    -20
             -10
                       0
                                            -20
                                                                                    -20
                                                                                                       0
```

(b) Use the full data set to perform a logistic regression with Direction as the response and the five Lagv ariables plus Volumeas predictors. Do any of the predictors appear to be statistically significant? If so, which ones?

Feature

```
subset = rowTrain,
             family = binomial)
contrasts(df$Direction)
##
       Uр
## Down
       0
## Up
        1
summary(glm_fit)
##
## Call:
## glm(formula = Direction ~ Lag1 + Lag2 + Lag3 + Lag4 + Lag5 +
      Volume, family = binomial, data = df, subset = rowTrain)
##
##
## Deviance Residuals:
##
      Min
                10
                     Median
                                  3Q
                                          Max
## -1.8407 -1.2503
                     0.9628
                              1.0737
                                       1.6492
##
## Coefficients:
##
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 0.31400
                          0.10037
                                   3.129 0.00176 **
## Lag1
              -0.06315
                          0.03027 -2.086 0.03694 *
              0.07588
                          0.03136
                                    2.420 0.01553 *
## Lag2
              0.00262
                          0.03144
                                    0.083 0.93358
## Lag3
              -0.02396
                          0.03023 -0.793 0.42807
## Lag4
## Lag5
              -0.02942
                          0.03184 -0.924 0.35547
              -0.05148
## Volume
                          0.04150 -1.241 0.21478
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 1122.4 on 816 degrees of freedom
## Residual deviance: 1108.2 on 810 degrees of freedom
## AIC: 1122.2
## Number of Fisher Scoring iterations: 4
```

Yes, predictors Lag1, Lag2 appear to be statistically significant.

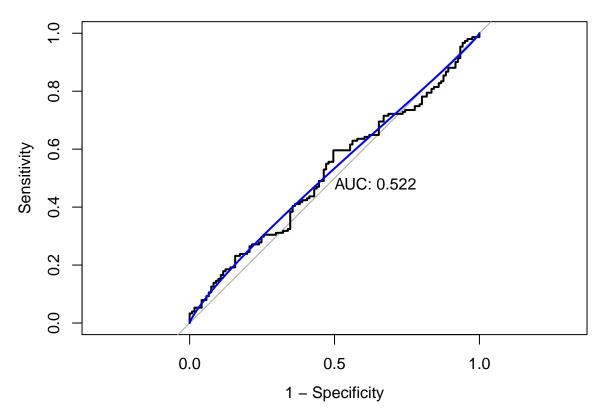
(c) Compute the confusion matrix and overall fraction of correct predictions. Briefly explain what the confusion matrix is telling you.

```
## Confusion Matrix and Statistics
##
             Reference
##
## Prediction Down Up
##
         Down
                16
                    28
         Uр
               105 123
##
##
##
                  Accuracy: 0.511
##
                    95% CI: (0.4499, 0.5719)
       No Information Rate: 0.5551
##
##
       P-Value [Acc > NIR] : 0.9361
##
##
                     Kappa: -0.0568
   Mcnemar's Test P-Value: 4.397e-11
##
##
##
               Sensitivity: 0.8146
##
               Specificity: 0.1322
##
            Pos Pred Value: 0.5395
##
            Neg Pred Value: 0.3636
##
                Prevalence: 0.5551
##
            Detection Rate: 0.4522
##
      Detection Prevalence: 0.8382
         Balanced Accuracy: 0.4734
##
##
##
          'Positive' Class : Up
##
```

From the confusion matrix, sensiticity is 0.8146 (the probability of true "Up" is 0.8146 when the direction is predicted to be Up) and the sensitivity is 0.1322 (the probability of not "Up" is 0.1322 when the direction is predicted to be down) Accuracy tells the overall probability of correct classifier is 0.511. Kappa is negative, which means that there is less agrrement than would be expected by chance give the marginal distribution.

(d) Plot the ROC curve using the predicted probability from logistic regression and report the AUC.

```
roc_glm = roc(df$Direction[-rowTrain], test.pred.prob)
plot(roc_glm, legacy.axes = TRUE, print.auc = TRUE)
plot(smooth(roc_glm), col = 4, add = TRUE)
```



Based on the plot, the AUC us 0.522, which suggests that the capability of logistic models distinguishing between classes is not good.

(e) Now fit the logistic regression model using a training data period from 1990 to 2008, with Lag1 and Lag2 as the predictors. Plot the ROC curve using the held out data(that is, the data from 2009 and 2010) and report the AUC.

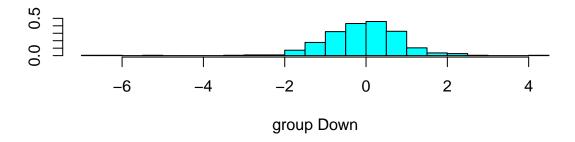
```
train_subset = df %>%
  filter(1990<=Year& Year<=2008)
test_subset = anti_join(df, train_subset)
## Joining, by = c("Year", "Lag1", "Lag2", "Lag3", "Lag4", "Lag5", "Volume", "Today", "Direction")
rowtrain = train_subset$Direction
rowtest = test_subset$Direction
glm_fit1 = glm(Direction~ Lag1 + Lag2,
               data = train_subset,
               family = binomial)
summary(glm_fit1)
##
## Call:
  glm(formula = Direction ~ Lag1 + Lag2, family = binomial, data = train_subset)
##
## Deviance Residuals:
##
                      Median
                                    3Q
       Min
                 1Q
                                            Max
                      0.9989
## -1.6149
           -1.2565
                                1.0875
                                         1.5330
##
```

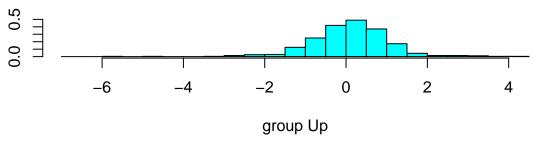
```
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) 0.21109 0.06456 3.269 0.00108 **
              -0.05421
                          0.02886 -1.878 0.06034 .
## Lag1
## Lag2
               0.05384
                          0.02905
                                   1.854 0.06379 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 1354.7 on 984 degrees of freedom
## Residual deviance: 1347.0 on 982 degrees of freedom
## AIC: 1353
##
## Number of Fisher Scoring iterations: 4
contrasts(train_subset$Direction)
##
       Uр
## Down 0
## Up
pred.test.value = predict(glm_fit1,
                          newdata = test_subset,
                          type = "response")
# Bayes Method Cutoff
pred.test = rep("Down", length(pred.test.value))
pred.test[pred.test.value>0.5] = "Up"
# Confusion Matrix
confusionMatrix(data = as.factor(pred.test),
               reference = as.factor(rowtest),
               positive = "Up")
## Confusion Matrix and Statistics
##
##
            Reference
## Prediction Down Up
        Down
              7 8
               36 53
##
        Uр
##
##
                 Accuracy : 0.5769
                   95% CI : (0.4761, 0.6732)
##
      No Information Rate: 0.5865
##
##
       P-Value [Acc > NIR] : 0.6193
##
##
                    Kappa : 0.035
##
   Mcnemar's Test P-Value: 4.693e-05
##
##
              Sensitivity: 0.8689
##
              Specificity: 0.1628
##
           Pos Pred Value : 0.5955
##
           Neg Pred Value: 0.4667
##
               Prevalence: 0.5865
           Detection Rate: 0.5096
##
```

```
Detection Prevalence: 0.8558
##
##
         Balanced Accuracy: 0.5158
##
##
           'Positive' Class : Up
##
# ROC
roc1 = roc(test_subset$Direction, pred.test.value)
plot(roc1, legacy.axes = TRUE, print.auc = TRUE)
plot(smooth(roc1), col = 4, add =TRUE)
    0.8
    9.0
Sensitivity
                                                 AUC: 0.556
    0.4
    0.0
                                               0.5
                        0.0
                                                                     1.0
                                         1 - Specificity
```

AUC is 0.556. The model does better job to classify compared to model in c.

(f) Repeat (e) using LDA and QDA.

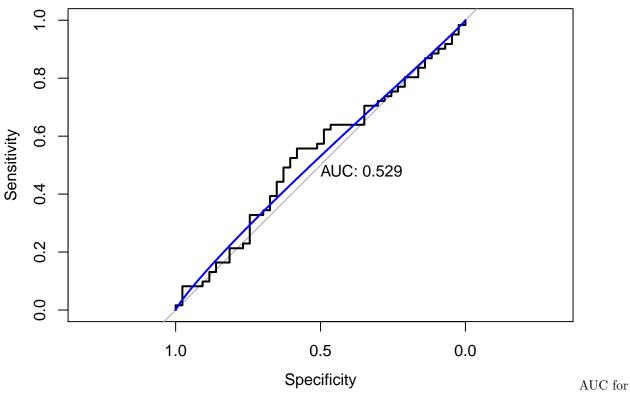




```
# evaluate the test set performance using roc
lda.pred = predict(lda.fit, newdata = test_subset)
head(lda.pred$posterior)
```

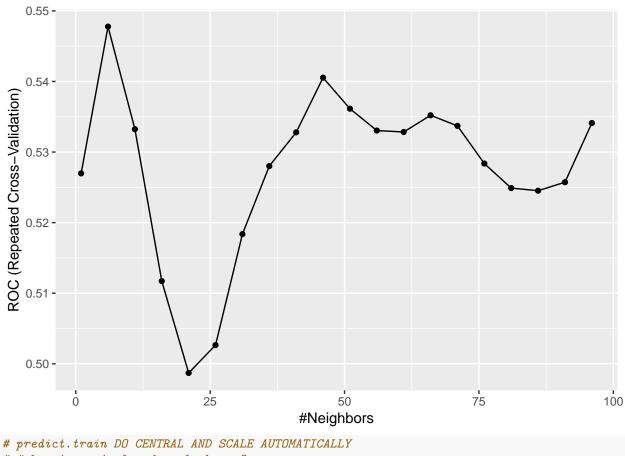
```
## QDA qda.fit = qda(Direction ~ Lag1 + Lag2, data = train_subset)
```

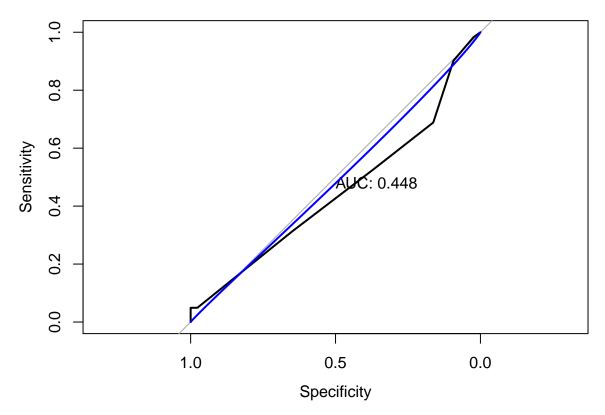
```
## QDA
qda.fit = qda(Direction ~ Lag1 + Lag2,
qda.pred = predict(qda.fit, newdata = test_subset)
head(qda.pred$posterior)
##
          Down
## 1 0.5436205 0.4563795
## 2 0.3528814 0.6471186
## 3 0.2227273 0.7772727
## 4 0.3483016 0.6516984
## 5 0.4598550 0.5401450
## 6 0.5119613 0.4880387
roc.qda = roc(test_subset$Direction, qda.pred$posterior[,2],
              levels = c("Down","Up"))
plot(roc.qda, legacy.axix = TRUE, print.auc = TRUE)
plot(smooth(roc.qda), col = 4, add = TRUE)
```



LDA is 0.557 and AUC for QDA is 0.529

(g) Repeat (e) using KNN. Briefly discuss your results.





AUC for KNN is 0.566.