

Report for Comp Exam

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1 Problem Setup

1.1 Randomized Controlled Trials

In RCTs, participants are randomly assigned to conditions so treatment is assigned by randomization. As a consequence of randomization, an unbiased estimate of the ATE can be directly computed from the data. An unbiased estimate of the ATE is $E[Y_i(1) - Y_i(0)] = E[Y(1)] - E[Y(0)]$.

1.2 Observational Studies

An observational study has the same intent as a randomized experiment: to estimate a causal effect. However, an observational study differs from a RCT in one design issue: the use of randomization to allocate participants to treatment and control groups.

In observational studies, the treated subjects often differ systematically from untreated subjects. In general, $E[Y(1) | t = 1] \neq E[Y(1)]$ holds. Thus, an unbiased estimate of the average treatment effect cannot be obtained by directly comparing outcomes between the the treated and the control groups.

1.3 Strong Ignorability

The treatment assignment is defined to be strongly ignorable [Rosenbaum and Rubin, 1983] if the following two conditions hold: 1). $(Y(1), Y(0)) \perp\!\!\!\perp t | X$ and 2). $0 < \Pr(t = 1 | X) < 1$. The first condition says that treatment assignment is independent of the potential outcomes conditional on the observed features of subjects. The second condition says that every subject has a nonzero probability to receive either treatment. The aforementioned first condition is also referred to as the "no-hidden confounding variables" assumption that all factors determining the outcome of each condition are observed.

2 Random Causal Forests

[Wager and Athey, 2015] proposed random causal forest (RCF) to infer treatment effect. From the conceptual point of view, causal trees can be viewed as

nearest neighbor methods with an adaptive neighborhood metric. Assume that there are n observed independent samples $(X_i, Y_i, W_i)_{i=1}^n$. The workflow of the RCF is that a causal tree is first built by recursively splitting the feature space until all samples are partitioned into a set of leaves L , each of which contains a few training samples. Then, for a data point x , the predicted outcome $\hat{\mu}(x)$ is evaluated by identifying the leaf $L(x)$ containing x and calculating

$$\hat{\mu} = \frac{1}{|\{i : X_i \in L(x)\}|} \sum_{\{i : X_i \in L(x)\}} Y_i$$

Given a test point x , the closest points to x are those fall in the same leaf as it. The authors believe that the leaf is small enough that the responses Y_i are roughly identically distributed. Then the treatment effect $\hat{\tau}$ for any $x \in L(x)$ is estimated as following:

$$\begin{aligned} \hat{\tau}(x) = & \frac{1}{|\{i : W_i = 1, X_i \in L(x)\}|} \sum_{\{i : W_i = 1, X_i \in L(x)\}} Y_i \\ & - \frac{1}{|\{i : W_i = 0, X_i \in L(x)\}|} \sum_{\{i : W_i = 0, X_i \in L(x)\}} Y_i \end{aligned} \quad (1)$$

RCF assumes that there is overlapping in the data, i.e., for some $\epsilon > 0$ and all $x \in [0, 1]^d$,

$$\epsilon < \mathbb{P}[W = 1 \mid X = x] < 1 - \epsilon$$

This condition effectively guarantees that, for large enough n , there will be enough treatment and control units near any test point x for local methods to work.

2.1 Honest Trees and Forests

The authors also define the Honest Trees and Forests in [Wager and Athey, 2015]. A tree is honest if, for each training example i , it only uses the response Y_i to estimate the within-leaf treatment effect τ using Equation 1 or to decide where to place the splits, but not both. There are two causal forest algorithms proposed from [Wager and Athey, 2015] that satisfy this condition.

The first algorithm, which is called double-sample trees, achieves honesty by dividing its training data into two halves \mathcal{I} and \mathcal{J} . Then, it uses the \mathcal{J} -sample to place the splits, while holding out the \mathcal{I} -sample to do within-leaf estimation. The details of the algorithm is shown in Algorithm 1.

Another approach to build honest trees is inspired by the idea of propensity score matching, which is called propensity trees. The idea behind this approach is to train a classification tree to predict the propensity score, which is the treatment assignments W_i , and ignore the outcome Y_i when placing splits. This method is useful in observational studies since propensity score is aimed to

Algorithm 1: Double-sample Causal Trees

Input: n training examples of (X_i, Y_i, W_i) , where X_i are features, Y_i is the response, and W_i is the treatment assignment.

A minimum leaf size k .

- 1 Draw a random subsample of size s from $\{1, \dots, n\}$ without replacement, and then divide it into two disjoint sets of size $|\mathcal{I}| = \lfloor s/2 \rfloor$ and $|\mathcal{J}| = \lceil s/2 \rceil$
- 2 Grow a tree via recursive partitioning. The splits are chosen using any data from the \mathcal{J} sample and X - or W -observations from the \mathcal{I} sample, but without using Y -observations from \mathcal{I} -sample.
- 3 Estimate leaf-wise response using only the \mathcal{I} -sample observations.

The algorithm estimates $\hat{\tau}(x)$ using Equation 1 on the \mathcal{I} sample. The splitting criteria is to maximize the variance of $\hat{\tau}(X_i)$ for $i \in \mathcal{J}$. Each leaf of the tree must contain k or more \mathcal{I} -sample observations of each treatment class.

reduce the selection bias by equating groups based on these features. The details of the algorithm is shown in Algorithm 2.

Algorithm 2: Propensity Trees

Input: n training examples of (X_i, Y_i, W_i) , where X_i are features, Y_i is the response, and W_i is the treatment assignment.

A minimum leaf size k .

- 1 Draw a random subsample $\mathcal{I} \in 1, \dots, n$ of size $|\mathcal{I}| = s$ (no replacement).
 - 2 Train a classification tree using sample \mathcal{I} where the outcome is the treatment assignment, i.e., on the (X_i, W_i) pairs with $i \in \mathcal{I}$. Each leaf of the tree must have k or more observations of each treatment class.
 - 3 Estimate $\tau(x)$ using Equation 1 on the leaf containing x .
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3 Counterfactual Inference

The problem of causal inference is often framed in terms of counterfactual problems such as "Would this particular student benefit more from the video hint or the text hint when the student cannot solve a problem?" In the binary intervention set, there are two possible interventions $\mathcal{T} = \{0, 1\}$, where intervention 1 is often referred as the "treated" and intervention 0 is the "control." Given a sample of subjects and a treatment, each subject has a pair of potential outcomes: Y_0 and Y_1 , the outcomes under the control and the treatment, respectively. Let t be an indicator variable denoting the treatment received ($t = 0$ for the control and $t = 1$ for the treatment). Only one outcome, which is called factual out-

come, $y_F(\mathbf{x}) = t \cdot Y_1(\mathbf{x}) + (1-t) \cdot Y_0(\mathbf{x})$, is observed for the subject \mathbf{x} , where $\mathbf{x} \in \mathcal{X}$ are the observed features for the subject. The unobserved outcomes are referred to as the counterfactual outcome, denoted as $y_{CF}(\mathbf{x}) = (1-t) \cdot Y_1(\mathbf{x}) + t \cdot Y_0(\mathbf{x})$. In other words, when a subject \mathbf{x} is assigned to the "control" ($t = 0$), $y_F(\mathbf{x})$ is equal to $Y_1(\mathbf{x})$, and $y_{CF}(\mathbf{x})$ is equal to $Y_0(\mathbf{x})$. The other way around, $y_F(\mathbf{x})$ is equal to $Y_0(\mathbf{x})$, and $y_{CF}(\mathbf{x})$ is equal to $Y_1(\mathbf{x})$. The estimated individual treatment effect (ITE) is then calculated by $\text{ITE}(\mathbf{x}) = Y_1(\mathbf{x}) - Y_0(\mathbf{x})$. The goal of counterfactual inference is to predict the counterfactual outcome given the observed data $D_n = \{(\mathbf{x}_i, t_i, y_F^i)_{i=1}^n\}$ from either RCTs or observational studies in order to estimate the ITE.

We assume n samples $\{(x_i, t_i, y_F^i)\}_{i=1}^n$ form an empirical distribution $\hat{p}^F = \{(x_i, t_i)\}_{i=1}^n$. We call this empirical distribution $\hat{p}^F \sim p^F$ the empirical factual distribution. In order to calculate ITE, we need to infer the counterfactual outcome which is dependent on the empirical distribution $\hat{p}^{CF} = \{(x_i, 1-t_i)\}_{i=1}^n$, which is called the empirical counterfactual distribution $\hat{p}^{CF} \sim p^{CF}$. The p^F and p^{CF} may not be equal because the distributions of the control and the treated populations may be different. The inequality of two distributions may cause the counterfactual inference over a different distribution than the one observed from the experiment. In machine learning terms, this scenario is usually referred to as domain adaptation, where the distribution of features in test data are different than the distribution of features in training data.

[Johansson et al., 2016] proposed Balancing Neural Networks (BNN) which can be applied to solve the counterfactual inference problem. They used a form of regularizer to enforce the similarity between the distributions of representations learned for populations with different interventions, for example, the representations for students who received text hints versus those who received video hints. This reduces the variance from fitting a model on one distribution and applying it to another. Because of random assignment to the interventions in RCTs, the distributions of the populations within different interventions are highly likely to be identical. However, in the observational study, we may end up with the situation where only male students receive video hints and female students receive text hints. Without enforcing the similarity between the distributions of representations for male and female students, it is not safe to make a prediction of the outcome if male students receive text hints.

The Counterfactual Regression (CFR) [Shalit et al., 2016] is built on the BNN. The important difference between these two models is that the CFR uses a more powerful distribution metric in the form of IPMs to learn a balancing representation.

The structure of CFR is illustrated in Figure 1. To learn a representation of deep features Φ , the CFR uses fully connected layers with ReLU activation function, where $\text{Relu}(z) = \max(0, z)$. We need to generalize from factual distribution to counterfactual distribution in the feature representation Φ to obtain accurate estimation of counterfactual outcome. The common successful approaches for domain adaptation encourage similarity between the latent feature representations w.r.t the different distributions. This similarity is often enforced

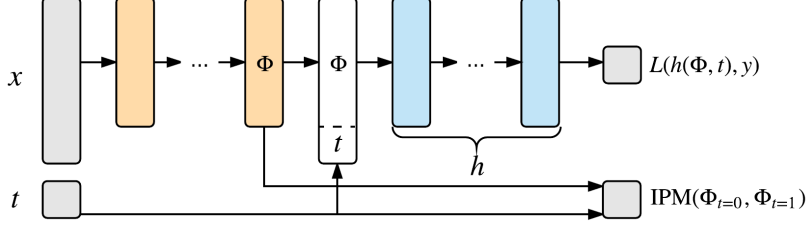


Figure 1: CFR for ITE estimation. L is a loss function, IPM is an integral probability metric

by minimizing a certain distance between the domain-specific hidden features. The distance between two distributions is usually referred to as the discrepancy distance, introduced by [Mansour et al., 2009], which is a hypothesis class dependent distance measure tailored for domain adaptation.

Integral Probability Metric (IPM) are used to measure the distance between two distributions $p_0 = p(x|t = 0)$, and $p_1 = p(x|t = 1)$, also known as the control and treated distributions. The IPM for p_0 and p_1 is defined as

$$\text{IPM}_{\mathcal{F}}(p_0, p_1) := \sup_{f \in \mathcal{F}} \left| \int_S f dp_0 - \int_S f dp_1 \right|,$$

where \mathcal{F} is a class of real-valued bounded measurable functions on S .

The choice of functions is the crucial distinction between IPMs [Sriperumbudur et al., 2009]. Two specific IPMs are used in our experiments: the Maximum Mean Discrepancy (MMD), and the Wasserstein distance. $\text{IPM}_{\mathcal{F}}$ is called MMD, when $\mathcal{F} = \{f : \|f\|_{\mathcal{H}} \leq 1\}$, where \mathcal{H} represents a reproducing kernel Hilbert space (RKHS) with k as its reproducing kernel. In other words, the family of norm-1 reproducing kernel Hilbert space (RKHS) functions lead to the MMD. The family of 1-Lipschitz functions $\mathcal{F} = \{f : \|f\|_L \leq 1\}$, where $\|f\|_L$ is the Lipschitz semi-norm of a bounded continuous real-valued function f , make IPM the Wasserstein distance. Both the Wasserstein and MMD metrics have consistent estimators which can be efficiently computed in the finite sample case [Sriperumbudur et al., 2012]. The important property of IPM is that

$$p_0 = p_1 \text{ iff } \text{IPM}_{\mathcal{F}}(p_0, p_1) = 0.$$

The representation with reduction of the discrepancy between the control and the treated populations helps the model to focus on balancing features across two populations when inferring the counterfactual outcomes. For instance, if in an experiment, almost no male student ever received intervention A, inferring how male students would react to intervention A is highly prone to error and a more conservative use of the gender feature might be warranted.

After obtaining the representation for subject \mathbf{x}_i , CFR concatenates the treatment assignment t_i to the representation $\Phi(\mathbf{x}_i)$ and feeds $[\Phi(\mathbf{x}_i), t_i]$ to another two fully connected layers to generate the predicted outcome.

4 Individualized Treatment Rules

An individual treatment rule (ITR) $d : \mathcal{X} \rightarrow \mathcal{T}$ is a deterministic decision rule from subject $\mathbf{x} \in \mathcal{X}$ into the intervention space \mathcal{T} . In experiments, we observe a triplet (\mathbf{x}, t, y) from each subject, where $\mathbf{x} = (x_1, x_2, \dots, x_n)^T \in \mathcal{X}$ denotes the participant's observed features, $t \in \mathcal{T} = -1, 1$ denotes the treatment assignment, and $y \in Y$ is the observed outcome, also called the "reward" in the literature on reinforcement learning. Note that $t = -1$ means that the subject is assigned to the control and $t = 1$ mean that the subject is assigned to the treatment in the context of ITR. Let $p(t|\mathbf{x})$ be the probability of assigning the subject with features \mathbf{x} to the intervention t . [Qian and Murphy, 2011] showed that the value of d satisfies

$$V(d) = E \left[\frac{y}{p(t|x)} \mathbb{I}_{t=d(\mathbf{x})} \right],$$

where $\mathbb{I}(\cdot)$ is an indicator function. The goal of the ITR is to find an optimal ITR, d^* , which is a rule that has the maximal value such that,

$$d^* \in \arg \max_d V(d).$$

[Qian and Murphy, 2011] also showed that finding d^* is equivalent to minimizing the following equation:

$$d^* \in \arg \min_d E \left[\frac{y}{p(t|x)} \mathbb{I}_{t \neq d(\mathbf{x})} \right] \quad (2)$$

Assume that the observed data $\{(\mathbf{x}_i, t_i, y_i), i = 1, \dots, n\}$ are collected independently. For any decision function $f(\mathbf{x})$, let $d_f(\mathbf{x}) = \text{sign}(f(\mathbf{x}))$ be the associated rule, where $\text{sign}(u) = 1$ for $u > 0$ and -1 otherwise. The particular choice of the value of $\text{sign}(0)$ is not important. With the observed data, the weighted classification error in Equation 2 can be approximated by the empirical risk

$$\frac{1}{n} \sum_{i=1}^n \frac{y_i}{p(t_i|x_i)} \mathbb{I}_{t_i \neq d_f(\mathbf{x}_i)}. \quad (3)$$

[Qian and Murphy, 2011] proposed a two-step procedure that first train a model using the observed data to estimate a conditional mean for the outcome $E(y|\mathbf{x}, t)$, and then determines the treatment rule by comparing the predicted value $E(y|\mathbf{x}, t = 1)$ between $E(y|\mathbf{x}, t = -1)$.

In contrast, [Zhao et al., 2012] proposed one-step procedure by showing that find an optimal ITR is equivalent to a classification task where we want

to classify t with \mathbf{x} as the input. Outcome weighted learning (OWL) proposed by [Zhao et al., 2012] use the hinge loss function and the regularization technique aiming to minimize

$$\frac{1}{n} \sum_{i=1}^n \frac{y_i}{p(t_i|x_i)} (1 - t_i f(\mathbf{x}_i))_+ + \lambda \|f\|^2, \quad (4)$$

where $(u)_+ = \max(u, 0)$ is the positive part of u , $\|f\|$ is some norm for f , and λ is a tuning parameter controlling the trade-off between empirical risk and complexity of the decision function f .

[Zhou et al.,] showed that decision rule in Equation 8 is affected by a simple shift of the outcome y and proposed Residual weighted learning (RWL) to relieve this issue. The idea behind RWL is to introduce a function g to reduce the variance of $\frac{y-g(\mathbf{x})}{p(t|\mathbf{x})} \mathbb{I}_{t \neq d(\mathbf{x})}$ and a reasonable candidate of g is

$$g^*(\mathbf{x}) = \frac{\mathbb{E}(y|\mathbf{x}, t=1) + \mathbb{E}(y|\mathbf{x}, t=-1)}{2} = \mathbb{E}\left(\frac{y}{2p(t, \mathbf{x})} | \mathbf{x}\right). \quad (5)$$

RWL thus is to minimize the following empirical risk:

$$\frac{1}{n} \sum_{i=1}^n \frac{y_i - \hat{g}^*(\mathbf{x}_i)}{p(t_i|\mathbf{x}_i)} \mathbb{I}_{t_i \neq d_f(\mathbf{x}_i)} \quad (6)$$

where \hat{g}^* is an estimate of g^* . For simplicity, let $\hat{r}_i = y_i - \hat{g}^*(\mathbf{x}_i)$. As in OWL, [Zhou et al.,] consider a surrogate loss function T to replace the 0-1 loss in Equation 6. The non-convex loss T has the following form:

$$T(u) = \begin{cases} 0 & \text{if } u \geq 1, \\ (1-u)^2 & \text{if } 0 \leq u < 1, \\ 2 - (1+u)^2 & \text{if } -1 \leq u < 0, \\ 2 & \text{if } u < -1 \end{cases} \quad (7)$$

It is called the smoothed ramp loss in [Zhou et al.,]. By incorporating the regularization, RWL is eventually aimed to minimize the following empirical risk:

$$\frac{1}{n} \sum_{i=1}^n \frac{\hat{r}_i}{p(t_i|x_i)} T(t_i f(\mathbf{x}_i))_+ + \lambda \|f\|^2, \quad (8)$$

where $\|f\|$ is the norm for f , and λ is a tuning parameter.

5 Bayesian Optimization

Bayesian optimization is a sequential model-based approach for global optimization of an unknown objective function f . The problem can be mathematically expressed as:

$$\mathbf{x}^* = \arg \max_{\mathbf{x} \in \mathcal{X}} f(\mathbf{x}) \quad (9)$$

where \mathcal{X} is the design space of interest. Bayesian optimization is the combination of two main components: a surrogate probabilistic model which captures our beliefs about the behavior of the unknown objective function f and is updated once new observation is gathered, and an acquisition function $\alpha : \mathcal{X} \rightarrow \mathbb{R}$ which performs the selection of the optimal sequence of queries based on the previous model. Since the objective function f is unknown, the Bayesian strategy is to place a prior over it which captures our beliefs about the behavior of the function. After gathering the function evaluations, which are treated as data, the prior is updated to form the posterior distribution over the objective function. Equipped with the posterior distribution, an acquisition function α is induced to determine what the next query point should be. The trade-off between the exploration and the exploitation is determined by the acquisition function leveraging the uncertainty in the posterior. Examples of acquisition functions includes probability of improvement, expected improvement, Bayesian expected losses, upper confidence bounds (UCB), and mixtures of these. The purpose of the trade-off is to minimize the number of function evaluations. As such, Bayesian optimization is well suited for functions that are very expensive to evaluate. The details of Bayesian Optimization is shown in Algorithm 3.

The Gaussian process (GP) is the most popular surrogate model. The objective function is modeled as a sample from the GP distribution. Attributes of the GP such as mean and variance are used by the acquisition function to decide the successive query points. More information about GP in the bandit setting can be found in Section 10.

Algorithm 3: Bayesian optimization

Input: n observations $\mathcal{D} = \{(\mathbf{x}_i, y_i)\}_{i=1}^n$ from objective function f
for $t = n + 1, n + 2, \dots$ **do**
 select new \mathbf{x}_t by maximizing acquisition function α

$$\mathbf{x}_t = \arg \max_{\mathbf{x}} \alpha(\mathbf{x}; \mathcal{D})$$

 query objective function to observe $y_t = f(\mathbf{x}_t)$
 augment data $\mathcal{D} = \{\mathcal{D}, (\mathbf{x}_t, y_t)\}$
 update statistical model
end

5.1 Thompson Sampling

Thompson sampling for Beta-Bernoulli bandit perhaps is the simplest non-trivial multi-armed bandit strategy in Bayesian optimization [Shahriari et al., 2016]. Bernoulli bandit problem is the bandit problem when the rewards are either 0 or 1, and for arm i the probability of success (reward=1) is μ_i . The Thompson sampling maintains Bayesian priors on the Bernoulli means μ_i 's. Beta distribution turns out to be a very convenient choice of priors for Bernoulli

rewards. The pdf of $\text{Beta}(\alpha, \beta)$ with parameters $\alpha > 0, \beta > 0$ is given by

$$f(x; \alpha, \beta) = \frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha)\Gamma(\beta)} x^{\alpha-1} (1-x)^{\beta-1}. \quad (10)$$

The mean of $\text{Beta}(\alpha, \beta)$ is $\alpha/(\alpha + \beta)$; and higher the α, β , tighter is the concentration of $\text{Beta}(\alpha, \beta)$ around the mean. If the prior for each arm is a $\text{Beta}(\alpha, \beta)$ distribution, then after observing a Bernoulli trial, the posterior distribution is simply $\text{Beta}(\alpha + 1, \beta)$ or $\text{Beta}(\alpha, \beta + 1)$, depending on whether the trial resulted in a success or failure, respectively. Thompson sampling then samples from these posterior distributions across all arms and chooses the arm with largest sample value. This procedure is summarized in Algorithm 4.

Algorithm 4: Thompson sampling for Beta-Bernoulli bandit

Input: α, β : hyperparameters of the beta prior

Initialize $n_{a,0} = n_{a,1} = i = 0$ for all K arms a

repeat

for $a = 1, \dots, K$ **do**

$w_a \sim \text{Beta}(\alpha + n_{a,1}, \beta + n_{a,0})$

end

$a_i = \arg \max_a w_a$

 Observe y_i by pulling arm a_i

if $y_i = 0$ **then**

$n_{a_i,0} = n_{a_i,0} + 1$

else

$n_{a_i,1} = n_{a_i,1} + 1$

end

$i = i + 1$

until *stopping criterion reached*;

In summary, Thompson sampling is the simplest non-trivial multi-armed bandit strategy in Bayesian Optimization. Since the Thompson sampling models the arms as independent, Thompson sampling must try every arm at least once. It will be an issue if the number of arms becomes large. In this case, Bayesian optimization with GP is an alternative to the Thompson sampling and alleviate this issue.

5.2 Choice between function predictor and multi-armed bandit algorithm

In many experiments, the designs space available to the designers have components that can be varied independently. For example, in designing an advertisement, one has choices such as artwork, font style, and size. If there are five choices for each, the total number of possible configurations is 125.

In general, this number grows combinatorially in the number of components. This presents challenges for approaches such as the Thompson sampling, since

the Thompson sampling models the arms as independent, which will lead to strategies that must try every arm at least once. This rapidly becomes infeasible in the large design spaces.

Even if the total number of possible design configuration is relatively small, it is still challenging for multi-armed bandit algorithms, such as Thompson sampling, when the number of available subjects is limited for these algorithms to figure out the optimal arm.

To alleviate this issue, a commonly used approach is to learn a function, whose input is a feature vector of the arm and output is associated reward of the arm, capturing dependence between the arms. Assume that each possible arm a has an associated feature vector $\mathbf{x}_a \in \mathbb{R}^d$. The expected reward of each arm can be expressed as a function of this feature vector, such as $f(a) = f(\mathbf{x}_a)$. The goal is to learn this function $f : \mathbb{R}^d \rightarrow \mathbb{R}$ from the experiment data in order to choose the arm with the highest reward among all possible arms.

6 Online Learning vs. Batch Learning

In machine learning, online machine learning is a method of machine learning in which data becomes available in a sequential order and is used to update our best predictor for future data at each step, as opposed to batch learning techniques which generate the best predictor by learning on the entire training data set at once.

6.1 Sequential method

The sequential approach is independent of the choice of prior and of the likelihood function and depends only on the assumption of i.i.d data. Sequential methods make use of observations one at a time, or in small batches, and then discard them before the next observations are used. They can be used, for example, in real-time learning scenarios where a steady stream of data is arriving, and predictions must be made before all of the data is seen. Because they do not require the whole data set to be stored or loaded into memory, sequential methods are also useful for large data sets.

7 Semi-Supervised Learning

In the setting of semi-supervised learning, the training data consists of l labeled instances $\{(\mathbf{x}_i, y_i)\}_{i=1}^l$ and u unlabeled instances $\{(\mathbf{x}_j)\}_{j=l+1}^{l+u}$, often with $l \ll u$. The goal of semi-supervised learning is to learn a model with better performance from the combination of labeled data and unlabeled data than from labeled data alone. The benefit of semi-supervised learning is that the labeled data can be hard and expensive to obtain since labels may require human experts, and the unlabeled data is often cheap in large quantity. Figure 2 illustrates how unlabeled data help models achieve a better performance.

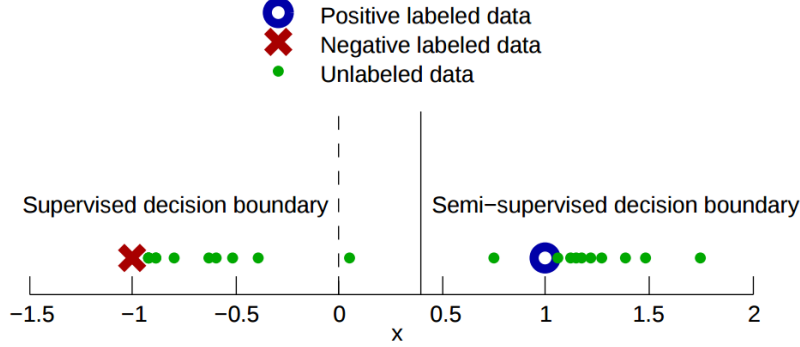


Figure 2: An illustrative example on how semi-supervised learning helps the model have a better performance.

7.1 Co-training

Co-training [Blum and Mitchell, 1998] is a technique in semi-supervised learning that requires two views of the data. It assumes that each example is described using two different feature sets that provide different, complementary information about the example. Co-training first learns a separate classifier for each view using any labeled examples. The most confident predictions of each classifier on the unlabeled data are then used to iteratively construct additional labeled training data. The details of co-training algorithm is described in Algorithm 5.

Algorithm 5: Co-training Algorithm for Semi-Supervised Learning

Input: labeled data $\{(\mathbf{x}_i, y_i)\}_{i=1}^l$, unlabeled data $\{\mathbf{x}_j\}_{j=l+1}^{l+u}$
each instance has two views $\mathbf{x}_i = [\mathbf{x}_i^{(1)}, \mathbf{x}_i^{(2)}]$
and a learning speed k
Let $L_1 = L_2 = \{(\mathbf{x}_1, y_1), \dots, (\mathbf{x}_l, y_l)\}$.
repeat
 Train view-1 $f^{(1)}$ from L_1 , view-2 $f^{(2)}$ from L_2
 Classify unlabeled data with $f^{(1)}$ and $f^{(2)}$ separately.
 Add $f^{(1)}$'s top k most-confident predictions $(\mathbf{x}, f^{(1)}(\mathbf{x}))$ to L_2
 Add $f^{(2)}$'s top k most-confident predictions $(\mathbf{x}, f^{(2)}(\mathbf{x}))$ to L_1
 Remove these from the unlabeled data.
until unlabeled data is used up;

There are three important assumptions which guarantee the performance of co-training algorithm: 1). feature split $x = [x^{(1)}; x^{(2)}]$ exists; 2). $x^{(1)}$ or $x^{(2)}$ alone is sufficient to train a good classifier; 3). $x^{(1)}$ and $x^{(2)}$ are conditionally

independent given the class.

7.2 Application in PeerASSIST

Semi-supervised learning approaches come in handy in PeerASSIST when we try to learn a function to predict the effectiveness of peer explanations. In the setting of PeerASSIST, not every peer explanation will be received by students, and thus, some of the explanations have no observed data on their effectiveness (e.g., the popularity, next problem correctness). When learning the function, these peer explanations without observed data are discarded, which is a waste of the data. Moreover, if there are not enough observed data, it becomes difficult to accurately learn the function. Semi-supervised learning approaches can be applied in this scenario to learn a better function.

8 Natural Language Processing for Enhancing Learning

8.1 Confusion Detector

Given the enormous student/instructor ratio in a MOOC’s discussion forums, it is difficult for an instructor to read all posts in a MOOC’s discussion forums. To address this issue, [Agrawal et al., 2015] collected and created the Stanford MOOCPosts dataset: a corpus composed of 29,604 anonymized learner forum posts from eleven Stanford University public online classes. Each post in the MOOCPosts dataset was scored across six dimensions – confusion, sentiment, urgency, question, answer, and opinion – and subsequently augmented with additional metadata. Then the authors built a confusion classifier from the Stanford MOOCPost dataset to automatically detect confusion from students posts and proposed a recommendation algorithm, which takes the student confusion as input, to automatically recommended a video lecture from a collection of several video lectures related to the course.

8.2 Automated Essay Scoring

Automated grading is a critical part of Massive Open Online Courses (MOOCs) system and any intelligent tutoring systems (ITS) at scale. Essay writing is usually a common student assessment process in schools and universities. In this task, students are required to write essays of various length, given a prompt or essay topic. Some standard tests, such as Test of English as a Foreign Language (TOEFL) and Graduate Record Examination (GRE), assess student writing skills. Manually grading these essay will be time-consuming. Thus automated essay scoring (AES) systems has been used in these tests to reduce the time and cost of grading essays. Moreover, as massive open online courses (MOOCs) become widespread and the number of students enrolled in one course increases,

the need for grading and providing feedback on written assignments are ever critical.

AES has employed numerous efforts to improving its performance. AES uses statistical and Natural Language Processing (NLP) techniques to automatically predict a score for an essay based on the essay prompt and rubric. Most existing AES systems are built on the basis of predefined features, e.g. number of words, average word length, and number of spelling errors, and a machine learning algorithm [Chen and He, 2013]. It is normally a heavy burden to find out effective features for AES. Moreover, the performance of the AES systems is constrained by the effectiveness of the predefined features. Recently another kind of approach has emerged, employing neural network models to learn the features automatically in an end-to-end manner [Taghipour and Ng, 2016]. By this means, a direct prediction of essay scores can be achieved without performing any feature extraction. The model based on long short-term memory (LSTM) networks in [Taghipour and Ng, 2016] has demonstrated promise in accomplishing multiple types of automated grading tasks.

8.3 NLP in PeerASSIST

The goal of PeerASSIST is to crowdsource the explanation (in the format of texts) of how to solve a given problem from students and apply multi-armed bandit algorithm to efficiently select the most helpful and useful peer explanation from all collected peer explanations for a given problem. The effectiveness of each peer explanations is measured in three dimensions: teacher’s rating (thumb up or thumb down), student’s rating (thumb up or thumb down), and the student next problem correctness after receiving the peer explanation.

A potential application of NLP techniques to PeerASSIST is to build a classifier to predict the probability of a peer explanation being an effective one based on the content of the explanation. As mentioned above, NLP techniques, especially deep learning approaches for NLP, have achieved promising results on text classification tasks. The predicted probabilities can potentially used to select the optimal explanation when one is needed to be delivered to the students. In this scenario, we can deliver the explanation with the highest probability to students. Another possible use of the predicted probabilities is to treat these values as a part of the contextual information for the explanations and incorporate this contextual information into contextual multi-armed bandit algorithms.

The explanations collected from students are not always of good quality. Since the classifier can automatically detect explanations with bad quality (i.e., the explanations with low probability values), one can quickly filter out these potential bad explanations, which saves multi-armed bandit algorithm from wasting attempts trying these explanations. When the explanations that students type in are detected as bad ones by the classifier, we can also build an intervention by telling students that the algorithm thinks that their explanations need some improvement. Then the students have a second chance to submitting new explanations. We hope that there will be observable improvement on the quality

of peer explanations for these students.

9 Reliable Crowdsourcing

During this process of asking students to rate the learning artifacts, we might gather noisy rating from students due to the fact that students may have a wide ranging level of rating expertise which are unknown, and in some cases may be adversarial. To learn the ground truth of these learning artifacts, we need to aggregate their opinions to recover the true, unknown label of each learning artifacts.

9.1 Majority Voting

Given each item is labeled by different workers, it is a straightforward approach to take the majority label as the true label. From reported experimental results on real crowdsourcing data [Snow et al., 2008], majority voting performs significantly better on average than individual workers. However, majority voting considers each item independently and gives the same weight across all workers who label the item when aggregating true label.

9.2 Dawid-Skene Model

[Dawid and Skene, 1979] were among the first to consider such a problem setup. They assume each workers are conditionally independent given the true labels and each worker is associated with a probabilistic confusion matrix that generates her labels. Each entry of the matrix indicates the probability that items in one class are labeled as another. Given the observed responses, the true labels for each items and the confusion matrices for each worker can be jointly estimated by a maximum likelihood method. The optimization can be implemented by the expectation-maximization (EM) algorithm.

9.3 GLAD

[Whitehill et al., 2009] proposed a richer graphic model which includes item difficulty and the expertise of the worker. The difficulty of item is modeled by the parameter $1/\beta_j \in [0, \infty)$. Here $1/\beta_j = \infty$ means the image is very ambiguous and hence the most proficient worker has a random chance of labeling it correctly. $1/\beta_j = 0$ means the item is so easy that even the most obtuse worker will always label it correctly.

The expertise of each worker i is modeled using the parameter $\alpha_i \in (-\infty, +\infty)$. Here $\alpha = +\infty$ means the worker always labels items correctly; $-\infty$ means the worker always labels items incorrectly.

The labels given by worker i to item j are denoted as L_{ij} and are generated as follows:

$$p(L_{ij} = Z_j | \alpha_i, \beta_j) = \frac{1}{1 + e^{-\alpha_i \beta_j}} \quad (11)$$

As the difficulty $1/\beta_j$ of an item increases, the probability of the label being correct moves toward 0.5. Similarly, as the worker's expertise decreases (lower α_i), the chance of correctly labeling drops to 0.5. Figure 3 shows the structure of the graphical model.

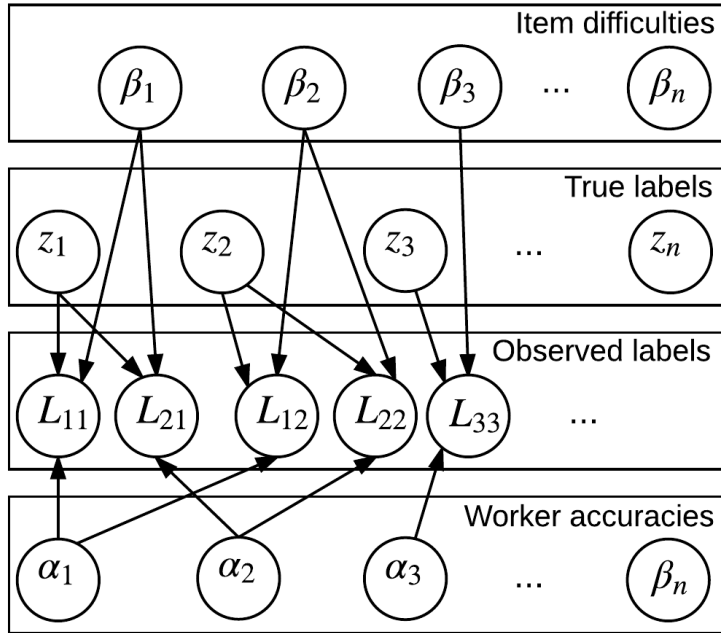


Figure 3: An illustrative example on how semi-supervised learning helps the model have a better performance.

9.4 Deep Learning Approach

[Shaham et al., 2016] showed that the Dawid and Skene model is equivalent to a Restricted Boltzmann Machine (RBM) with a single hidden node under the assumption that all workers are conditionally independent. Thus the posterior probabilities of the true labels can be estimated via a trained RBM.

A RBM is an undirected bipartite graphical model, consisting of a visible layer X and a hidden layer H . The visible layer consists of d binary random

variables and the hidden layer m binary random variables. These two layers are fully connected to each other. A RBM is parametrized by $\lambda = (W, a, b)$, where W is the weight matrix of the connections between the visible and hidden units, and a, b are the bias vectors of the visible and hidden layers, respectively. An illustration of a RBM is depicted in Figure 4.

A RBM implies the conditional probabilities

$$p_{\lambda}(X_i = 1|H) = \sigma(a_i + W_{i \cdot} H)$$

$$p_{\lambda}(H_j = 1|X) = \sigma(b_j + X^T W_{\cdot j}),$$

where $\sigma(z)$ is the sigmoid function, $W_{i \cdot}$ is the i -th row of W and $W_{\cdot j}$ is its j -th column.

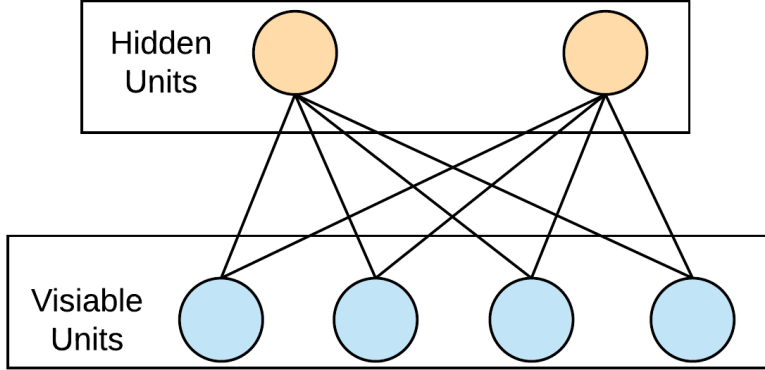


Figure 4: Diagram of a restricted Boltzmann machine with four visible units and three hidden units (no bias units)

To relax the assumption on the conditional independence of the variables X_1, \dots, X_d , a RBM-based Deep Neural Net (DNN) is proposed to estimate the posterior probabilities $p_{\theta}(Y|X)$. The mechanism to stack multiple RBMs is that the hidden layer of each RBM is the input for the successive RBM. The RBMs are trained one at a time from bottom to top. Specifically, given training data $x^{(1)}, \dots, x^{(n)} \in \{0, 1\}^d$, the bottom RBM is trained first, and then obtain the hidden representation of the first layer by sampling $h^{(i)}$ from the conditional RBM distribution $p_{\lambda}(H|X = x^{(i)})$. The vector $h^{(1)}, \dots, h^{(n)}$ are then used as a training set for the second RBM and so on. An illustration of a RBM is depicted in Figure 5.

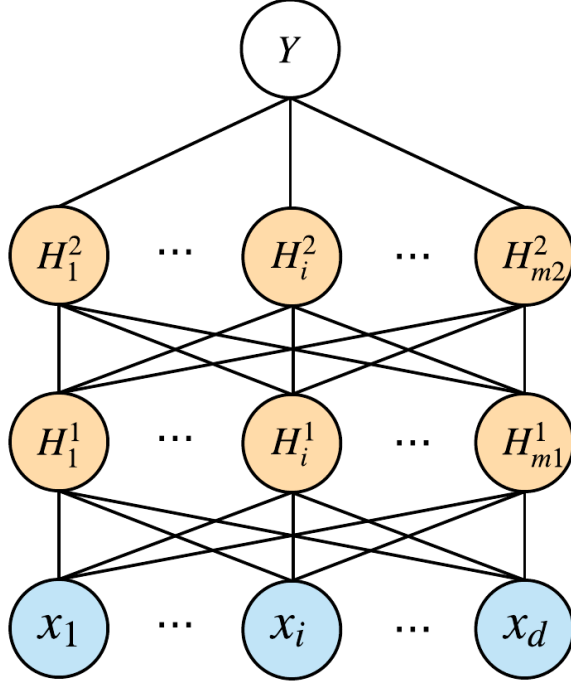


Figure 5: Diagram of RBM-based DNN with two hidden layers.

9.5 Minimax Entropy

[Zhou et al., 2012] proposed a minimax entropy principle to estimate the ground truth given the observed labels by workers. The model is illustrated in Figure 6. Each row corresponds to a works indexed by i (from 1 to m). Each column corresponds to an item to be labeled, indexed by j (from 1 to n). Each item has an unobserved label represented as a vector y_{jl} , which is 1 when item j is in class l (from 1 to c), and 0 otherwise. Observed data is a tensor of labels z_{ijk} , which is 1 when the item i is labeled as class j by the worker i , and 0 otherwise. We assume that z_{ij} are drawn from π_{ij} . π_{ij} can be represented as a tensor π_{ijk} , which is the probability that worker i labels item j as class k . The proposed model will estimate y_{jl} from the observed z_{ij} .

The maximum entropy model for π_{ij} given y_{jl} is as follow:

	item 1	item 2	...	item n
worker 1	z_{11}	z_{12}	...	z_{1n}
worker 2	z_{21}	z_{22}	...	z_{2n}
...
worker m	z_{m1}	z_{m2}	...	z_{mn}

	item 1	item 2	...	item n
worker 1	π_{11}	π_{12}	...	π_{1n}
worker 2	π_{21}	π_{22}	...	π_{2n}
...
worker m	π_{m1}	π_{m2}	...	π_{mn}

Figure 6: Left: observed labels. Right: underlying distributions. Highlights on both tables indicate that rows and columns of the distributions are constrained by sums over observations.

$$\begin{aligned}
& \max_{\pi} - \sum_{i=1}^m \sum_{j=1}^n \sum_{k=1}^c \pi_{ijk} \ln \pi_{ijk} \\
& \text{s.t.} \sum_{i=1}^m \pi_{ijk} = \sum_{i=1}^m z_{ijk}, \forall j, k, \quad \sum_{j=1}^n y_{jl} \pi_{ijk} = \sum_{j=1}^n y_{jl} z_{ijk}, \forall i, k, l, \\
& \sum_{k=1}^c \pi_{ijk} = 1, \forall i, j, \pi_{ijk} \geq 0, \forall i, j, k.
\end{aligned} \tag{12}$$

To infer y_{jl} , they proposed to choose y_{jl} to minimize the entropy in Equation 12.

$$\begin{aligned}
& \min_y \max_{\pi} - \sum_{i=1}^m \sum_{j=1}^n \sum_{k=1}^c \pi_{ijk} \ln \pi_{ijk} \\
& \text{s.t.} \sum_{i=1}^m \pi_{ijk} = \sum_{i=1}^m z_{ijk}, \forall j, k, \quad \sum_{j=1}^n y_{jl} \pi_{ijk} = \sum_{j=1}^n y_{jl} z_{ijk}, \forall i, k, l, \\
& \sum_{k=1}^c \pi_{ijk} = 1, \forall i, j, \pi_{ijk} \geq 0, \forall i, j, k, \quad \sum_{l=1}^c y_{jl} = 1, \forall j, y_{jl} \geq 0, \forall j, l.
\end{aligned} \tag{13}$$

9.6 Control Items

Control items with known answers can be used to evaluation workers' reliability and bias, and hence weight their answers accordingly on target items with unknown answers. There is a trade-off in this scenario: we can better estimate workers' reliability and bias by letting them answer more control items, but there are fewer opportunities left for the target items. On the other hand, using fewer control items produces poor estimates of worker's reliability and bias, which leads to a bad result when aggregating workers' answers. [Liu et al., 2013] examined the effectiveness of control items and provided insights on how many control items are enough under different scenarios, which can help crowdsourcing practitioners make their own decisions. Aforementioned methods (except

for majority voting) evaluate workers' reliability by comparing their agreement with other workers and control items can be incorporated into these methods.

10 Gaussian Processes in Bandit Setting

The Gaussian process is the extension of multivariate Gaussian to infinite-sized collections of real-valued variables. In particular, this extension will allow us to think of Gaussian processes as distributions not just over random vectors but in fact distributions over random functions.

The Gaussian process $\text{GP}(\mu_0, k)$ is a non-parametric model that is fully characterized by its prior mean function $\mu_0 : \mathcal{X} \rightarrow \mathbb{R}$ and its positive-definite kernel, or covariance function, $k : \mathcal{X} \times \mathcal{X} \rightarrow \mathbb{R}$.

Let $\mathcal{D}_n = \{(\mathbf{x}_i, y_i)\}$ denote a set of n observations and \mathbf{x} denote the arbitrary test point. The random variable $f(\mathbf{x})$ is also a GP distribution conditioned on observations \mathcal{D}_n with following mean $\mu_n(\mathbf{x})$ and variance $\sigma_n^2(\mathbf{x})$:

$$\mu_n(\mathbf{x}) = \mu_0(\mathbf{x}) + \mathbf{k}(\mathbf{x})^T (\mathbf{K} + \sigma^2 \mathbf{I})^{-1} (\mathbf{y} - \mathbf{m}) \quad (14)$$

$$\sigma_n^2(\mathbf{x}) = k(\mathbf{x}, \mathbf{x}) - \mathbf{k}(\mathbf{x})^T (\mathbf{K} + \sigma^2 \mathbf{I})^{-1} \mathbf{k}(\mathbf{x}) \quad (15)$$

where $m_i := \mu_0(\mathbf{x}_i)$, $K_{i,j} := k(\mathbf{x}_i, \mathbf{x}_j)$, and $\mathbf{k}(\mathbf{x})$ is a vector of covariance terms between \mathbf{x} and $\mathbf{x}_{1:n}$.

The posterior mean and variance evaluated at any point \mathbf{x} represent the model's prediction and uncertainty in the objective function at the point \mathbf{x} . In order to apply GP under the setting of multi-armed bandit, we need an acquisition function to select the next query point given the posterior model. The acquisition function should be carefully designed to trade off exploration of the search area and exploitation of current promising areas.

10.1 GP-UCB

To decrease uncertainty globally, one strategy could be to pick the point which maximizes the variance $\mathbf{x}_{n+1} = \arg \max_{\mathbf{x} \in D} \sigma_n(\mathbf{x})$. However, this strategy is not well suited for multi-armed bandit problem since it can be wasteful. Another idea is to select the point which maximizes the expected reward given the posterior model $\mathbf{x}_{n+1} = \arg \max_{\mathbf{x} \in D} \mu_n(\mathbf{x})$. However, this idea is too greedy and tends to end up with a local optima. To balance exploration and exploitation, a combined strategy is to choose

$$\mathbf{x}_{n+1} = \arg \max_{\mathbf{x} \in D} \mu_n(\mathbf{x}) + \beta_n \sigma_n(\mathbf{x}), \quad (16)$$

where β_n are constants. There are theoretically motivated guidelines for setting and scheduling the hyperparameter β_n to achieve optimal regret.

Since Equation 10.1 is an upper confidence bound of the marginal posterior $P(f(\mathbf{x})|\mathbf{y}_n)$, a natural interpretation of this strategy is that it selects the point

\mathbf{x} such that $f(\mathbf{x})$ is a reasonable upper bound on $f(\mathbf{x})$. This algorithm is called Gaussian process upper confidence bound (GP-UCB), introduced by [Srinivas et al., 2010]. The GP-UCB selection rule is motivated by the UCB algorithm for the classical multi-armed bandit problem.

10.2 Contextual GP-UCB

Motivated by GP-UCB algorithm mentioned above, [Krause and Ong, 2011] extended the generalization of this algorithm by incorporating contextual information

$$\mathbf{x}_{n+1} = \arg \max_{\mathbf{x} \in D} \mu_n(\mathbf{x}, \mathbf{z}_n) + \beta_n \sigma_n(\mathbf{x}, \mathbf{z}_n), \quad (17)$$

where $z_n \in Z$ is the contextual information from a set Z of contexts, $\mu_n(\cdot)$ and $\sigma_n^2(\cdot)$ are the posterior mean and variance of the GP conditioned on observations $\mathcal{D}_n = \{(\mathbf{x}_i, \mathbf{z}_i, y_i)\}$. The authors called the selection rule the contextual Gaussian process UCB algorithm (GCP-UCB).

To derive the kernel k on the product space $Z \times X$ of contexts and actions, a natural approach to start with kernel functions $k_Z : Z \times Z \rightarrow \mathbb{R}$ and $k_X : X \times X \rightarrow \mathbb{R}$ on the space of contexts and actions. [Krause and Ong, 2011] proposed two possibilities of constructing composite kernel k from context kernel k_Z and action kernel k_X . One is to calculate a product kernel $k = k_Z \otimes k_X$, by setting

$$(k_Z \otimes k_X)((\mathbf{z}, \mathbf{x}), (\mathbf{z}', \mathbf{x}')) = k_Z(\mathbf{z}, \mathbf{z}') k_X(\mathbf{x}, \mathbf{x}'). \quad (18)$$

An alternative is to calculate the additive kernel $k = k_Z \oplus k_X$, by setting

$$(k_Z \oplus k_X)((\mathbf{z}, \mathbf{x}), (\mathbf{z}', \mathbf{x}')) = k_Z(\mathbf{z}, \mathbf{z}') + k_X(\mathbf{x}, \mathbf{x}'). \quad (19)$$

11 Propensity Score Matching

A propensity score [Rosenbaum and Rubin, 1983] is the probability of a unit (e.g., student, classroom, school) being assigned to a particular treatment given a set of observed features. Propensity scores are used to reduce selection bias by equating groups based on these features.

Suppose that we have a binary treatment $T = \{0, 1\}$, an outcome Y , and observed features X . The propensity score is defined as the conditional probability of treatment given background variables:

$$p(x) := \Pr(T = 1 \mid X = x)$$

Let $Y(0)$ and $Y(1)$ denote the potential outcomes under the control and the treatment, respectively.

Due to random treatment assignment in RCT, the propensity score is known. However, the actual propensity score in observational experiments is unknown and it can be estimated using statistical or machine learning models from the experiment data. The most commonly used model is a logistic regression model,

in which treatment assignment T is the dependent variable and features X are independent variables. Beyond logistic regression, the use of bagging or boosting [Lee et al., 2010], tree-based model (Propensity trees) and causal random forests [Wager and Athey, 2015], and neural networks [Setoguchi et al., 2008] have been proposed to estimate the propensity score.

The purpose of Propensity score matching (PSM) [Austin, 2011] is to form matched sets of the treated and the control subjects who share a similar value of the predicted propensity score. PSM allows one to estimate the average treatment effect for the treated (ATT) [Imbens, 2004b]. The ATT is the average effect of treatment on those subjects who ultimately receive the treatment. The most common implementation of PSM is one-to-one or pair matching, in which pairs of the control and the treated subjects are formed, such that matched subjects have similar values of the propensity score. Once a matched sample has been formed, the treatment effect can be estimated by directly comparing outcomes between treated and untreated subjects in the matched sample. In summary, the analysis of a propensity score matched sample can mimic that of an RCT: one can directly compare outcomes between the treated and the control subjects within the propensity score matched sample.

The possibility of bias arises because the apparent difference in outcome between these two groups of units may depend on characteristics that affected whether or not a unit received a given treatment instead of due to the effect of the treatment per se. In randomized experiments, the randomization enables unbiased estimation of treatment effects; for each covariate, randomization implies that treatment-groups will be balanced on average, by the law of large numbers. Unfortunately, for observational studies, the assignment of treatments to research subjects is typically not random. Matching attempts to mimic randomization by creating a sample of units that received the treatment that is comparable on all observed covariates to a sample of units that did not receive the treatment.

12 Peer Review

After going through Chris Schunn’s publications, I find these three papers [Patchan and Schunn, 2016, Kaufman and Schunn, 2011, Patchan and Schunn, 2015] related to my dissertation. The summary of research findings from these paper is listed below.

[Patchan and Schunn, 2016] pointed out that research on such peer assessments has found that, in general, peers are capable of providing valid ratings, and their feedback is usually just as effective as an instructor’s feedback in help students improve their draft and sometimes more effective. Further, participating in peer assessment improves writing ability.

[Kaufman and Schunn, 2011] found that students sometimes regard peer assessment as unfair and often believe that peers are unqualified to review and assess students’ work. Furthermore, students’ perceptions about the fairness of peer assessment drop significantly following students’ experience in doing

peer assessment. Students’ fairness perceptions—and drops in those perceptions—are most significantly associated with their perceptions about the extent to which peers’ feedback is useful and positive. However, students’ perceptions appear to be unrelated to the extent of their revision work.

[Patchan and Schunn, 2015] found that reviewer ability and text quality did not affect the amount of feedback provided (i.e., number of comments and length of comments). Low reviewer provided more praise than high reviewers whereas high reviewers provided more criticism than low reviewers. This criticism described more problems and offered more solutions. There was one interesting interaction between reviewer ability and text quality – high reviewers described more problems in the low-quality texts than in the high-quality texts, whereas low reviewers did not make this distinction.

[Patchan and Schunn, 2016] found several interesting interactions between two factors. Often lower-ability writers benefited more from receiving feedback from lower-ability reviewers, while higher-ability writers benefited equally from receiving feedback from lower-ability and higher-ability reviewers.

13 Learnersourcing Subgoal Labels

[Weir et al., 2015] presented a three-stage workflow for learners to generate subgoal labels for how-to video while they are learning from the videos. The goal of the first stage (Generation) is to let learners submit the subgoal labels after a certain interval during watching the videos. The goal of the second stage (Evaluation) is to let learners select the most relevant answer for the video section, as well as discard potential spam answers. The goal of the third stage (Proofreading) is to let learners evaluate the most popular subgoal labels from stage 2 for quality and eventually agree on a final label for that subgoal. During stage 2 and stage 3, learners always have a option to refine the label.

In PeerAssist, only students who receive 0 on a problem are prompted with a peer explanation from one of students who answer the same problem correctly. Then these students have a option to give a rating (thumb up or thumb down) to the peer explanation that they receive. The students, who answer the problem correctly in the first attempt, do not have a chance seeing and rating the peer explanations. If a certain problem is relatively easy, there will be few students who receive 0 and it is difficult to find the optimal peer explanations based on students’ ratings. Even if the problem is relatively difficult, we miss the contribution from the students with correct answer in the first attempt when deciding the optimal peer explanations. Motivated by [Weir et al., 2015], we can apply two-stage workflow to collect ratings from students in terms of the quality of the peer explanations after they submit an answer. Assume that there are several peer explanations available for a given problem and the ranking of these peer explanations are already decided by some algorithm (e.g., multi-armed bandit algorithm) based on the history data.

On stage 1, students are prompted with several (i.e., 3) peer explanations and have a option to rate these explanations after they submit an answer. The

goal of this stage is to collect students’ opinions on these explanations and use these data as one of the indicators to determine the most effective explanation and discard spam explanations. In terms of which explanations should be prompted to students on this stage, several simple approaches can be applied: random selection from all available explanations or newly added explanations. Exploration strategy can be applied in this scenario. For the purpose of exploration, explanations with high uncertainty are prompted with students. This strategy can potentially reduce the uncertainty of these explanations and help multi-armed bandit algorithm efficiently find the optimal explanations.

On stage 2, student are prompted with the currently optimal peer explanation from the ranking algorithm and asked to evaluate whether this peer explanation is highly effective. The goal of this stage is to let students to evaluate the optimal explanation for quality and analog to the goal of exploration strategy in multi-armed bandit algorithm.

14 HCOMP & CSCW

[Glassman et al., 2016] Personalized support for students is a gold standard in education, but it scales poorly with the number of students. Prior work on learnersourcing presented an approach for learners to engage in human computation tasks while trying to learn a new skill. Our key insight is that students, through their own experience struggling with a particular problem, can become experts on the particular optimizations they implement or bugs they resolve. These students can then generate hints for fellow students based on their new expertise. We present workflows that harvest and organize students’ collective knowledge and advice for helping fellow novices through design problems in engineering. Systems embodying each workflow were evaluated in the context of a college-level computer architecture class with an enrollment of more than two hundred students each semester. We show that, given our design choices, students can create helpful hints for their peers that augment or even replace teachers’ personalized assistance, when that assistance is not available.

[Yim et al., 2017] Group activities that use Google Docs for simultaneous collaborative writing and editing are increasingly common in higher education. Although studies show that synchronous collaboration can bring multiple benefits, such as enhanced productivity and writing quality, little is known about these writing practices in classrooms and their impact on students’ writing. Using a mixed method approach, we conducted an empirical study that explores the different styles of synchronous collaboration in 45 Google Docs documents produced by 82 undergraduate students, and how students’ practices affect the specific dimensions of the final text including quality. The results suggest that (a) out of four styles, Divide and Conquer style tended to produce better quality text whereas Main Writer had the lowest quality scores, and that (b) balanced participation and amount of peer editing led to longer texts with higher quality scores for content, evidence, but not organization or mechanics. Given these results, we suggest several design features for collaborative writing systems and

propose guidelines for instructional practices.

[Yoon et al., 2016] New multi-modal annotation tools hold the promise of bringing the benefits of face-to-face contact to remote, asynchronous interactions. One such system, RichReview++, incorporates new techniques to improve access to the embedded multimedia commentary and allows users to annotate with new modalities, like deictic gestures. We conducted a series of field deployments of RichReview++ to characterize how these features benefit students using them for activities in the university classroom. Our first deployment investigated the use of multi-modal annotations as a way for instructors to provide feedback on student term papers. Our second deployment used annotations to support peer discussion about assigned readings in a graduate-level course. We found that presenting voice comments as interactive waveforms seems to facilitate students’ consumption of the instructor’s voice comments. We also found that gestural annotations clarify voice and give annotators a quick and lightweight way to alter the scope of their voice comments. Based on these results, we suggest ways to best leverage multi-modal annotation tools in education environments.

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