

ITEM #227 - Motion Trajectory as Time-Series IR: Minimal Differential Primitives for Physical and Biological Movement

Conversation : 运动轨迹 Time-Series IR

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DBM-COT ITEM #227 (EN)

Motion Trajectory as Time-Series IR: Minimal Differential Primitives for Physical and Biological Movement

Abstract

This item formalizes the minimal and sufficient raw input representation for modeling physical and biological motion trajectories as Time-Series IR (Information Representation). By decomposing motion into discrete time samples, local geometric direction, and differential changes in position and direction, we establish a coordinate-agnostic, structure-centric IR foundation applicable to aircraft flight, animal locomotion, and other embodied systems. Absolute positions and orientations are explicitly excluded from IR signals and retained only for interpretation and alignment.

1. Discrete Time Sampling

Given a motion process, we sample the trajectory at fixed or variable time intervals:

$$t[k], \quad k = 0, 1, 2, \dots, n$$

The index k defines a strictly ordered temporal sequence, serving as the fundamental axis of the Time-Series IR. Continuity is assumed only locally between adjacent samples.

2. Spatial Observation (Interpretation Layer)

At each time point, the observed spatial position is recorded as:

$$p[k] = (x[k], y[k], z[k])$$

These absolute coordinates **do not directly constitute IR signals**. They serve as raw observations and are retained for visualization, physical grounding, and post-hoc interpretation.

3. Local Motion Geometry: Directional Normal

At each sampled point, a plane orthogonal to the instantaneous motion direction is defined. Its normal vector represents the local direction of motion:

$$n[k] = (\alpha[k], \beta[k], \gamma[k])$$

This normal captures the first-order geometric structure of the trajectory at time k , independent of global coordinate frames.

4. Differential Primitives Between Adjacent Samples

For each adjacent time pair $(k, k+1)$, two and only two differential quantities are extracted as **raw Time-Series IR primitives**:

4.1 Positional Change (Magnitude)

$$\Delta pos[k] = || p[k+1] - p[k] ||$$

This represents displacement magnitude, corresponding to speed, effort, or kinetic intensity.

4.2 Directional Change (Structure)

$$\Delta dir[k] = \text{angle}(n[k], n[k+1])$$

This represents turning, curvature, hesitation, or maneuvering behavior.

Together, $(\Delta pos, \Delta dir)$ form the minimal sufficient IR describing motion dynamics.

5. Exclusion of Absolute State from IR

For motion trajectory IR:

- Absolute coordinates (x, y, z)
- Absolute directions (α, β, γ)

must not be treated as IR signals.

They are invariant-breaking, context-dependent, and system-specific. Instead, only *differential changes* carry structural information suitable for metric comparison, clustering, and reasoning.

Absolute values may be retained solely as **explanatory or alignment metadata**.

6. Relation to Time-Series Structural Intelligence

This representation directly parallels financial Time-Series IR:

Financial Series Motion Trajectory

Price	Absolute position
Price delta	Δ_{pos}
Trend change	Δ_{dir}

The IR captures **decision structure**, not raw state.

7. Scope and Applicability

This primitive IR applies uniformly to:

- Aircraft and UAV flight trajectories
- Animal locomotion and migration
- Human motion and behavior tracking
- Autonomous robotic navigation

Higher-order constructs (curvature, maneuver patterns, intent inference) must be derived **above** this layer, preserving the minimality and purity of the raw IR.

8. Core Principle

Motion Time-Series IR should encode how movement changes, not where it is.

This principle anchors motion modeling within the broader DBM Structural Intelligence framework.

DBM-COT ITEM #227 (中文)

运动轨迹的 Time-Series IR：物理与生物运动的最小差分原语

摘要

本文正式定义了将物理与生物运动轨迹建模为 Time-Series IR（信息表征）的最小且充分的原始输入形式。通过离散时间采样、局部运动几何结构以及位置与方向的差分变化，建立了一套与坐标系无关、以结构为中心的 IR 基础，适用于飞行器、动物运动及其他具身系统。绝对坐标与绝对方向被明确排除在 IR 信号之外，仅作为解释与对齐数据保留。

1. 离散时间采样

对任意运动过程，在固定或可变时间间隔下采样：

$t[k], \quad k = 0, 1, 2, \dots, n$

索引 k 构成严格有序的时间序列，是 Time-Series IR 的基本轴线，仅假设相邻采样点之间具有局部连续性。

2. 空间观测（解释层）

在每个时间点，记录空间位置：

$$\mathbf{p}[k] = (x[k], y[k], z[k])$$

这些绝对坐标不直接作为 IR 信号，仅作为原始观测数据，用于可视化、物理语义解释与后续对齐。

3. 局部运动几何：方向法线

在每个采样点，构造一垂直于瞬时运动方向的平面，其法线表示该点的运动方向：

$$\mathbf{n}[k] = (\alpha[k], \beta[k], \gamma[k])$$

该法线刻画了轨迹在时间 k 的一阶几何结构，与全局坐标系无关。

4. 相邻采样点之间的差分原语

对任意相邻时间点 $(k, k+1)$ ，仅提取以下两个差分量作为 Time-Series IR 的最基本原始输入：

4.1 位置变化（尺度）

$$\Delta_{\text{pos}}[k] = || \mathbf{p}[k+1] - \mathbf{p}[k] ||$$

表示位移大小，对应速度、能量投入或行为强度。

4.2 方向变化（结构）

$$\Delta_{\text{dir}}[k] = \text{angle}(\mathbf{n}[k], \mathbf{n}[k+1])$$

表示转向、曲率、犹豫、规避或机动行为。

$(\Delta_{\text{pos}}, \Delta_{\text{dir}})$ 构成描述运动动力学的最小充分 IR 对。

5. 绝对状态不应进入 IR

在运动轨迹 IR 中：

- 绝对位置 (x, y, z)
- 绝对方向 (α, β, γ)

不应作为 IR 信号使用。

它们破坏不变性，强依赖上下文与系统设定，仅适合作为解释数据或对齐元数据存在。

6. 与时间序列结构智能的对应关系

该建模方式与金融时间序列 IR 完全同构：

金融时间序列 运动轨迹

价格 绝对位置

价格变动 Δpos

趋势变化 Δdir

IR 关注的是决策与行为结构，而非状态本身。

7. 适用范围

该最小 IR 原语统一适用于：

- 飞行器与无人机轨迹
- 动物运动与迁徙
- 人体行为与动作序列
- 自主机器人导航

更高阶结构（曲率、机动模式、意图推断）必须在此之上派生，而不污染原始 IR 层。

8. 核心原则

运动的 Time-Series IR 应描述“如何变化”，而非“位于何处”。

该原则是 DBM 结构智能体系中运动建模的基石。
