

ITEM #191 — Strand Decomposition for Horizontal Bridging

Conversation: Feasible Path Trimming

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From $X \rightarrow Y$ Rope to Minimal Computation-Disjoint Fibers

1. Motivation

After obtaining a **Feasible Horizontal Bridging Subgraph** and trimming it into an **Exact Path** (ITEM #188), a deeper engineering problem emerges:

A feasible $X \rightarrow Y$ structure is rarely a single path;
it is a *rope* composed of multiple intertwined, partially shared computation strands.

Treating this rope as a monolithic path leads to:

- Poor reuse across different targets
- Path oscillation in multi-goal bridging
- Weak coverage in “sufficient” horizontal bridging
- Inefficient caching and explanation

To enable **sufficient, stable, and reusable Horizontal Bridging**,
we must **decompose a feasible $X \rightarrow Y$ rope into multiple independent computation strands**.

2. Problem Definition

Given:

- A feasible or trimmed horizontal bridging subgraph
 $G = (V, E)$ connecting X to Y
- Y may contain multiple targets
- Shared prefixes, branches, joins, and cycles may exist

Goal:

Decompose G into a set of **computation-disjoint strands**:

$$S = \{ (X_1 \rightarrow Y_1), (X_2 \rightarrow Y_2), \dots, (X_k \rightarrow Y_k) \}$$

such that:

- $\bigcup Y_i = Y$ (target coverage)
- Each strand is internally executable
- Strands are mutually **computation-independent**
- Each strand can be **stored, reused, and recomposed** for future Horizontal Bridging

3. Core Insight

The key realization is:

**Horizontal Bridging requires not just paths,
but minimal independent bridging units.**

A strand is defined as:

The minimal Y -anchored executable subgraph whose computation does not interfere with other strands under a chosen independence criterion.

This transforms Horizontal Bridging from *path finding* into *strand assembly*.

4. Algorithm Overview

The algorithm consists of three composable stages:

A. Target-Side Partitioning (Y-Partition)

Partition the target set \mathcal{Y} into sub-targets $\{\mathcal{Y}_1, \mathcal{Y}_2, \dots\}$ such that:

- Targets in the same group share substantial computation structure
- Targets across groups are weakly coupled or independent

Engineering-friendly strategies:

- **Signature-based clustering (MVP)**
Group targets by route signatures extracted from \mathcal{G}
 - **Structural cut / dominator-like partitioning**
Separate targets that require different critical intermediates
 - **Domain-driven partitioning**
Package / module / CCC-region-based grouping
-

B. Strand Extraction via Reverse Trimming (ITEM #188 Reuse)

For each target group \mathcal{Y}_i :

$\mathcal{G}_i = \text{Trim}(\mathcal{G}, \mathcal{X}, \mathcal{Y}_i)$

where Trim is the **Y-anchored reverse pruning algorithm** from ITEM #188.

This yields a **minimal Y-sufficient subgraph** for each strand candidate.

C. Computation-Disjoint Packing

The extracted strand graphs $\{\mathcal{G}_i\}$ may still share computation.

Define a **computation-independence policy**, such as:

- **Strict disjointness**: no shared nodes or edges
- **Cost-disjointness**: no shared high-cost or non-idempotent nodes
- **Policy-aware disjointness**: conflict determined by execution semantics

Apply a greedy or policy-guided packing process to produce:

$\{\mathcal{G}_1^*, \mathcal{G}_2^*, \dots\}$

where each strand is mutually non-interfering under the chosen policy.

5. Result: Strand Set

Each resulting strand G_i^* represents:

- A self-contained computation from x_i to y_i
- Minimal and exact with respect to its targets
- Independent from other strands

Conceptually:

$$\begin{array}{c} X \rightarrow Y \text{ rope} \\ \downarrow \\ (X_1 \rightarrow Y_1), (X_2 \rightarrow Y_2), \dots, (X_k \rightarrow Y_k) \end{array}$$

6. Knowledge HashMap Construction

Each strand is canonicalized and stored as a reusable knowledge unit:

Key (example):

```
(operationKey,  
goalSignature,  
policySignature,  
contextSignature)
```

Value:

- Canonical path or minimal subgraph
- Cost profile
- Evidence / explanation chain
- Constraints and applicability conditions

This transforms bridging results into **persistent Horizontal Bridging knowledge**.

7. Role in Sufficient Horizontal Bridging

Strand decomposition enables:

- **Coverage-oriented bridging** instead of single-path optimization
- Reduced oscillation in multi-target planning
- Incremental assembly of solutions using cached strands

- Self-reinforcing improvement of the bridging system

Operationally:

```
Strand HashMap
  ↓
Direct assembly (Phase-0)
  ↓
Feasible bridging for gaps
  ↓
New strand extraction and caching
```

8. Engineering Properties

- Composable with ITEM #188
 - Linear to near-linear complexity per stage
 - Deterministic under fixed policies
 - Strongly explainable
 - Naturally supports constructive evolution
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9. Summary

ITEM #191 elevates Horizontal Bridging from path discovery to structural decomposition.

It establishes the principle that:

The power of Horizontal Bridging lies in discovering, isolating, and reusing minimal computation-independent strands.

Together with ITEM #188, this forms a closed engineering loop:

- Feasible → Exact → Independent → Reusable → Sufficient
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ITEM #191 — 水平桥接的计算股分解算法 (中文版)

从 $X \rightarrow Y$ 绳索到最小计算不相干独立股

1. 动机

在获得一条 可行或已裁剪的 $X \rightarrow Y$ 水平桥接结构 后，一个更深层的工程问题随之出现：

这条路径通常不是一根线，
而是一根由多条计算链相互缠绕形成的“绳子”。

将其当作单一路径会导致：

- 知识难以复用
 - 多目标桥接时产生震荡
 - 覆盖不足，难以做到“充分桥接”
 - 缓存与解释效率低下
-

2. 问题定义

给定：

- 一条 $X \rightarrow Y$ 的可行/精确桥接子图 G
- 目标集合 Y ，可能包含多个目标

目标：

将 G 分解为若干条 计算互不相干的独立股：

$(X_1 \rightarrow Y_1), (X_2 \rightarrow Y_2), \dots$

并保证：

- 覆盖全部目标
 - 每一股可独立执行
 - 股与股之间不存在关键计算冲突
 - 每一股都可被缓存与复用
-

3. 核心思想

水平桥接真正需要的不是“一条最优路径”，
而是：

一组最小、独立、可复用的计算股。

4. 算法结构

A. 目标端分组 (Y-Partition)

按结构、签名或领域约束，将 Y 拆成若干子目标集合。

B. 反向裁剪提取股 (复用 ITEM #188)

对每个 Y_i ，执行：

$G_i = \text{Trim}(G, X, Y_i)$

得到仅支撑该目标组的最小子图。

C. 计算不相干装箱

在定义好的冲突策略下，将 G_i 组合成互不干扰的独立股集合。

5. 结果

最终得到：

- 多条 $X_i \rightarrow Y_i$ 的独立计算股
 - 可直接执行、解释、缓存
 - 可像积木一样组合用于未来桥接
-

6. 知识化与 HashMap

每一股被规范化并存入 HashMap，
成为 **Horizontal Bridging** 的长期资产。

7. 对充分 Horizontal Bridging 的意义

该机制使系统具备：

- 覆盖导向而非路径导向的能力
 - 稳定、多目标的组合式桥接
 - 持续自我增强的知识积累闭环
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8. 总结

ITEM #191 将水平桥接从“找路”提升为“解绳”。

