```
function [stage2_total_mass, stage2_height] = get_stage2_mass(second_stage, M_p, M_0, num_engines, init)
   % Sophie, Sara, Ben
   % Set density constants
   rho_LH2 = 71;
   rho_LOX = 1140;
   rho_RP1 = 820;
   rho_LCH4 = 423;
   rho_solid = 1680;
   rho_N204 = 1442;
   rho\_UDMH = 791;
   % Set tank constants
   M 1 = 26000; \% kg
   radius = 6.4; % m
   cap_height = 1; % m
   payload_cone_height = 10; % m
   payload_cyl_height = 10; % m
   engine_space = 3; % m
   \ensuremath{\mbox{\%}} Constants that depend on propellant choice
   if second_stage == "LCH4"
       stage2_ratio = 3.6;
       stage2_oxidizer_rho = rho_LOX;
       stage2_fuel_rho = rho_LCH4;
       stage2_thrust_single = 0.745e6; % N
       stage2_nozzle_exp = 45;
       chamber_pressure_2 = 10.1e6; % Pa
   elseif second_stage == "LH2"
       stage2 ratio = 6.03;
       stage2_oxidizer_rho = rho_LOX;
       stage2_fuel_rho = rho_LH2;
       stage2_thrust_single = 0.099e6; % N
       stage2_nozzle_exp = 84;
       chamber_pressure_2 = 4.2e6; % Pa
   elseif second_stage == "RP1"
       stage2_ratio = 2.72;
       stage2_oxidizer_rho = rho_LOX;
       stage2_fuel_rho = rho_RP1;
       stage2_thrust_single = 0.061e6; % N
       stage2_nozzle_exp = 14.5;
   chamber_pressure_2 = 6.77e6; % Pa
elseif second_stage == "solid"
       stage2_thrust_single = 2.94e6; % N
       stage2_nozzle_exp = 56;
       chamber_pressure_2 = 5e6; % Pa
   elseif second_stage == "storables"
       stage2_ratio = 2.67;
       stage2_oxidizer_rho = rho_N2O4;
       stage2_fuel_rho = rho_UDMH;
       stage2_thrust_single = 0.067e6; % N
       stage2_nozzle_exp = 81.3;
       chamber\_pressure\_2 = 14.7e6; \ \% \ Pa
   end
   % Set thrust according to number of engines
   if init
       stage2 thrust = stage2 thrust single;
   else
       stage2_thrust = stage2_thrust_single*num_engines;
   % Compute stage2 tank mass
   if second_stage == "solid"
       solid_volume = M_p/rho_solid;
       stage2_tank_mass = 12.16*solid_volume;
   else
       mass_split = M_p/(stage2_ratio+1);
       mass_oxidizer = stage2_ratio*mass_split;
       mass_fuel = mass_split;
       volume_oxidizer = mass_oxidizer/stage2_oxidizer_rho;
       volume_fuel = mass_fuel/stage2_fuel_rho;
       if second_stage == "LH2"
           stage2_tank_mass = 12.16*volume_oxidizer + 9.09*volume_fuel;
       else
           stage2_tank_mass = 12.16*(volume_oxidizer + volume_fuel);
   \% Compute stage2 tank volume assuming cylinder and two sphere caps 1\mbox{m}
   % tall each
   if second_stage ~= "solid"
       ox_cap_vol = 2*(pi*cap_height)*(3*radius^2 + cap_height^2)/6;
       ox_cyl_vol = volume_oxidizer - ox_cap_vol;
       ox_cyl_height = ox_cyl_vol/(pi*radius^2);
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ox_cap_surf_area = 2*(pi*(radius^2 + cap_height^2));
        ox_cyl_surf_area = 2*pi*radius*ox_cyl_height;
        fuel_cap_vol = 2*(pi*cap_height)*(3*radius^2 + cap_height^2)/6;
        fuel_cyl_vol = volume_fuel - fuel_cap_vol;
        fuel_cyl_height = fuel_cyl_vol/(pi*radius^2);
        fuel_cap_surf_area = 2*(pi*(radius^2 + cap_height^2));
        fuel_cyl_surf_area = 2*pi*radius*fuel_cyl_height;
   \ensuremath{\mathrm{\%}} Compute insulation from tank volume, edge cases for storables and
   % solids
    if second_stage ~= "solid" && second_stage ~= "storables"
        LOX_stage2_insulation_mass = 1.123*(ox_cap_surf_area + ox_cyl_surf_area);
        if second stage == "LH2"
            LH2_stage2_insulation_mass = 2.88*(fuel_cap_surf_area + fuel_cyl_surf_area);
            stage2_insulation_mass = LOX_stage2_insulation_mass + LH2_stage2_insulation_mass;
        elseif second stage == "LCH4"
            LCH4_stage2_insulation_mass = 1.123*(fuel_cap_surf_area + fuel_cyl_surf_area);
            stage2_insulation_mass = LOX_stage2_insulation_mass + LCH4_stage2_insulation_mass;
           stage2_insulation_mass = LOX_stage2_insulation_mass;
        end
    elseif second stage == "solid"
        stage2 insulation mass = 0;
        solid_cap_vol = 2*(pi*cap_height)*(3*radius^2 + cap_height^2)/6;
        solid_cyl_vol = solid_volume - solid_cap_vol;
        solid_cyl_height = solid_cyl_vol/(pi*radius^2);
        stage2 insulation mass = 0;
    % Set engine and casing mass, dependent on propellant
    if second_stage ~= "solid"
        stage2 engine mass = 7.81e-4*stage2 thrust + 3.37e-5*stage2 thrust*sqrt(stage2 nozzle exp) + 59;
        stage2_casing_mass = 0;
        stage2_engine_mass = 0;
        stage2_casing_mass = 0.135*M_p;
    end
   % Compute payload and aft fairing areas
    payload_fairing_area = pi*radius*sqrt(radius^2 + payload_cone_height^2) + 2*pi*radius*payload_cyl_height;
   aft2_fairing_area = 2*pi*radius*(engine_space + cap_height);
   payload fairing mass = 4.95*payload fairing area^(1.15);
   stage2_aft_fairing_mass = 4.95*aft2_fairing_area^(1.15);
   \% Compute intertank fairing mass and overall height dependent on propellant
   if second_stage ~= "solid"
       intertank2_fairing_area = 2*pi*radius*(2*cap_height);
        stage2_intertank2_fairing_mass = 4.95*intertank2_fairing_area^(1.15);
        stage2_height = payload_cone_height + payload_cyl_height + 4*cap_height + ox_cyl_height + fuel_cyl_height + engine_space;
    else
        stage2_intertank2_fairing_mass = 0;
        stage2\_height = payload\_cone\_height + payload\_cyl\_height + 2*cap\_height + solid\_cyl\_height + engine\_space;
   % Compute wiring, thrust structure, and gimbals masses
    stage2_mass_wiring = 1.058*sqrt(M_0)*stage2_height^(0.25);
   stage2_mass_thrust_struct = 2.25e-4*stage2_thrust;
   stage2\_mass\_gimbals = 237.8*(stage2\_thrust/chamber\_pressure\_2)^(0.9375);
   % Compute total mass
   stage2_total_mass = M_p + stage2_mass_wiring + stage2_tank_mass + stage2_insulation_mass + stage2_engine_mass + stage2_mass_thrust_struct + stage2_casing_mass +
   % Assign workspace variables
    assignin('base', 'stage2_propellant_mass', M_p);
    assignin('base', 'stage2_tank_mass', stage2_tank_mass);
    assignin('base', 'stage2_mass_wiring', stage2_mass_wiring);
    assignin('base', 'stage2_insulation_mass', stage2_insulation_mass);
    assignin('base', 'stage2_engine_mass', stage2_engine_mass);
    assignin('base', 'stage2_mass_thrust_struct', stage2_mass_thrust_struct);
    assignin('base', 'stage2_casing_mass', stage2_casing_mass);
   assignin('base', 'stage2_mass_gimbals', stage2_mass_gimbals);
assignin('base', 'payload_fairing_mass', payload_fairing_mass);
   assignin('base', 'stage2_intertank2_fairing_mass', stage2_intertank2_fairing_mass);
    assignin('base', 'stage2_aft_fairing_mass', stage2_aft_fairing_mass);
end
```



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