

**MIS 637 B Final Exams**  
**Data Analytics & Machine Learning**

**December 12, 2019**  
**School of Business**  
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1. Describe the differences between clustering and classifications

**ANSWER:**

<b>SR. No.</b>	<b>Clustering</b>	<b>Classification</b>
<b>1</b>	It finds natural grouping of instances on given unlabeled data.	It learns a method to predict the instance class from pre labeled classified instances.
<b>2</b>	An unsupervised learning technique.	A supervised learning technique.
<b>3</b>	Works solely with unlabeled data.	Involves both labeled and unlabeled data.
<b>4</b>	Has a single phase. (Grouping)	Involves two phases. (Training and Testing)
<b>5</b>	Clustering does not poignantly employ training sets, which are groups of instances employed to generate the groupings.	Classification imperatively needs training sets to identify similar features.
<b>6</b>	Clustering groups objects with the aim to narrow down relations as well as learn novel information from hidden patterns.	Classification seeks to determine which explicit group a certain object belongs to.
<b>7</b>	Example of algorithms: K-Means, DBSCAN.	Example of algorithms: Decision trees, Random forest.

2. We have the following two-dimensional data points:

a (3,2), b (3,3), c (4,3), d (5,3), e (1,2), f (4,2), g (1,1), h (2,1).

Identify the cluster by applying the k-means algorithm, with k=2. Show that the ratio of the between-cluster variation to the within-cluster variation increases with each pass of the algorithm. Please show your work and how the algorithm works: **passes, steps, formulas, calculations, tables, plots, and final clusters.**

**ANSWER:**

**FIRST PASS:**

Given data: k = 2

a	b	c	d	e	f	g	h
(3,2)	(3,3)	(4,3)	(5,3)	(1,2)	(4,2)	(1,1)	(2,1)

**Step 1:** So, m1 = (4, 3) & m2 = (1, 1)

Calculate the distance of each point from m1 & m2 and divide them in to clusters C1 and C2.

**Step 2:**

Euclidean distance formula:  $d_{Euclidean}(x, y) = \sqrt{(x_2-x_1)^2 + (y_2-y_1)^2}$  where two points are (x1, y1) (x2, y2)

Points	Distance from Centre1 (4, 3)	Distance from Centre2 (1, 1)	Cluster
a (3,2)	1.414	2.236	C1
b (3,3)	1	2.828	C1
c (4,3)	0	3.605	C1
d (5,3)	1	4.472	C1
e (1,2)	3.162	1	C2
f (4,2)	1	3.162	C1
g (1,1)	3.605	0	C2
h (2,1)	2.828	1	C2

Points in cluster C1 are (a, b, c, d, f) and that in C2 are (e, g, h)

$$SSE = \sum_{i=1}^k \sum_{p \in C_i} d(p, m_i)^2$$

$$SSE = 1.414^2 + 1^2 + 0^2 + 1^2 + 1^2 + 1^2 + 0^2 + 1^2$$

Hence, SSE= 6.999

$$d(m_1, m_2) = 3.605$$

$$\frac{BCV}{WCV} = \frac{d(m_1, m_2)}{SSE} = 3.605/6.999 = 0.515$$

$$\text{New Centroid: C1} = \left( \frac{3+3+4+5+4}{5}, \frac{2+3+3+3+2}{5} \right) = (3.8, 2.6)$$

$$\text{New Centroid: C2} = \left( \frac{1+1+2}{3}, \frac{2+1+1}{3} \right) = (1.33, 1.33)$$

## SECOND PASS:

Points	Distance from Centre1 (3.8, 2.6)	Distance from Centre2 (1.33, 1.33)	Cluster
a (3,2)	1	1.799	C1
b (3,3)	0.894	2.361	C1
c (4,3)	0.447	3.149	C1
d (5,3)	1.264	4.032	C1
e (1,2)	2.863	0.746	C2
f (4,2)	0.632	2.752	C1
g (1,1)	3.224	0.466	C2
h (2,1)	2.408	0.746	C2

$$SSE = \sum_{i=1}^k \sum_{p \in C_i} d(p, m_i)^2$$

$$SSE = 1^2 + 0.894^2 + 0.447^2 + 1.264^2 + 0.746^2 + 0.632^2 + 0.466^2 + 0.746^2$$

$$SSE = 5.326$$

$$d(m_1, m_2) = 2.777$$

$$\frac{BCV}{WCV} = \frac{d(m_1, m_2)}{SSE} = 2.777/5.326 = 0.521$$

$$\text{New Centroid: C1} = \left( \frac{3+3+4+5+4}{5}, \frac{2+3+3+3+2}{5} \right) = (3.8, 2.6)$$

$$\text{New Centroid: C2} = \left( \frac{1+1+2}{3}, \frac{2+1+1}{3} \right) = (1.33, 1.33)$$

When the value of the centroid of two clusters doesn't change then K-means algorithm terminates.

Final Clusters:

**Cluster 1 = {a, b, c, d, f}**

**Cluster 2 = {e, g, h}**

**GRAPH PLOT:**

