

STAT 2857A – Lecture 1 Examples and Exercises

Example 1.1: Happy Birthmonth!

Consider the month of birth for three students selected randomly from the class (call them Alexandria, Braden, and Chen).

- a) Describe the outcomes.
- b) How many outcomes are in the sample space?
- c) Identify one simple event?
- d) Identify one compound event?

Example 1.1 part 2

Let A_i denote the event that Alexandria is born in month i . Let B_i denote the event that Braden is born in month i . Let C_i denote the event that Chen is born in month i .

Describe each of the following events in words?

- a) $E_1 = A_1 \cap B_1 \cap C_1$
- b) $E_2 = \bigcup_{i=1}^{12} (A_i \cap B_i \cap C_i)$
- c) $E_3 = \bigcup_{i=1}^{12} (A_i \cap B_i \cap C'_i)$

Example 1.1 part 3

- a) Identify two events that are disjoint/mutually exclusive.
- b) Identify two events that are *not* disjoint/mutually exclusive.

Example 1.1 part 4

Consider the events E_1 , E_2 , and E_3 from part 2.

- a) What is the probability of each event?
- b) What do these probabilities mean?

Exercise 1.1

An unfortunate student has tests in biology, chemistry, and statistics all in one day (a cruel experiment). Thankfully, each test is graded on a pass/fail basis.

- a) List all of the outcomes in the sample space.
- b) Write the sample space in set builder notation.
- c) Identify i) two events that are mutually exclusive and ii) two events that are not mutually exclusive.
- d) Let E_1 be the event the student passes one test and E_2 the event they pass two test. List the outcomes in and describe the event $(E_1 \cup E_2)'$.