

Homework 3

Song Jiecheng 13300180032

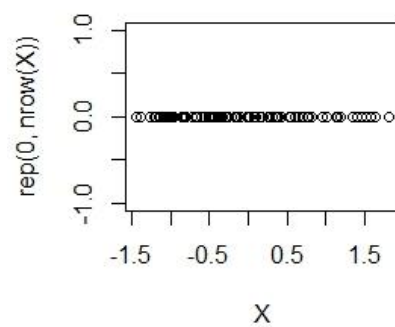
Question 1 : Do PCA (Principle Component Analysis) with assign31.csv

Demonstrates

Graph

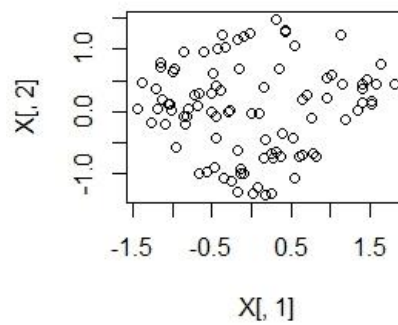
information reserve

1



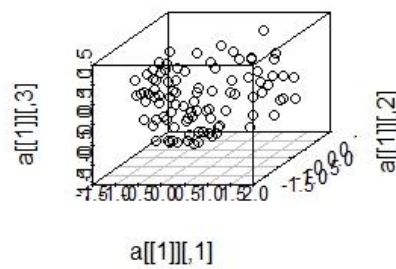
0.2139058

2



0.396026

3



0.5165856

4	0.595481
5	0.6697862
6	0.7381548
7	0.7905304
8	0.8367713
9	0.8798061
10	0.920202
11	0.9500036

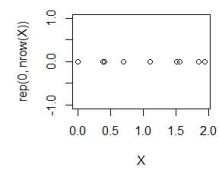
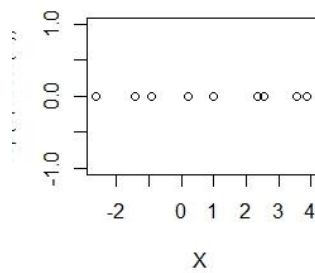
Question 2 : Do PCA and NMF with assign32.csv and explain the difference between them.

Demonstrates

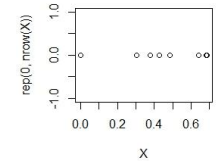
PCA

NMF

1



W

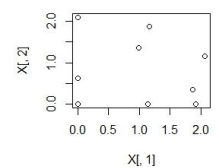
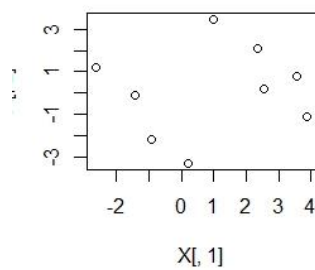


H

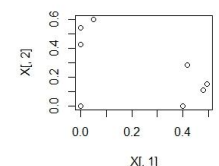
Information reserve 0.4326317

Error 0.4326317

2



W

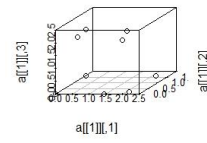
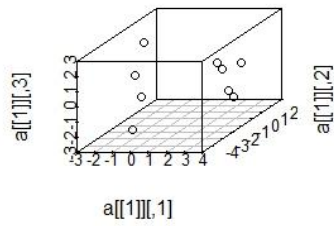


H

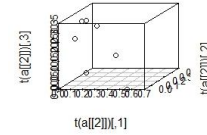
Information reserve 0.7648243

Error 0.1417607

3



W



H

Information reserve 0.9298461

Error 0.06324455

4

Information reserve 0.9918732

Error 0.009525376

5

Information reserve 0.9967265

Error 0.009675278

6

Information reserve 1

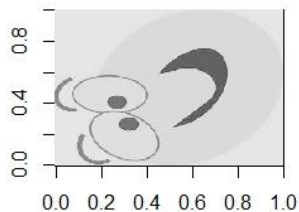
Error 0.008793702

We can find the capacity of reserving information of PCA and NMF are similar, over three demonstrates, we can save more than ninety-nine percent of the information.

And in PCA we need calculate the eigenvalues and eigenvectors of the covariance matrix, and in NMF we find how to make the norm of $WH-X$ minimum.

Question 2 : Do PCA and NMF with test2.csv and explain the difference between them.

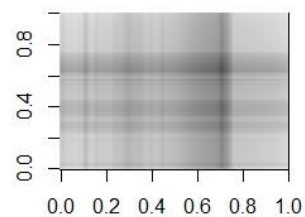
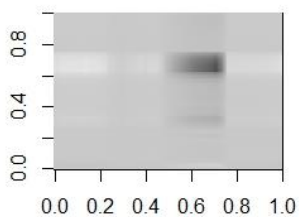
Original Photo



Demonstrates
1

PCA

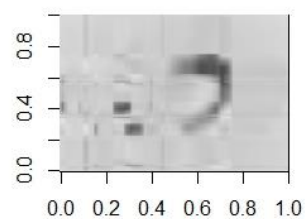
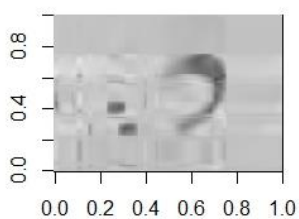
NMF



5

Information reserve 0.3474913

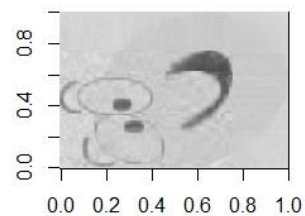
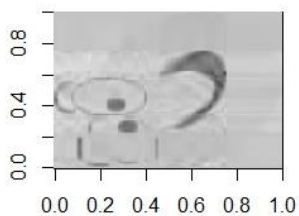
Error 0.05002276



10

Information reserve 0.6676473

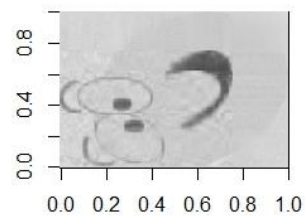
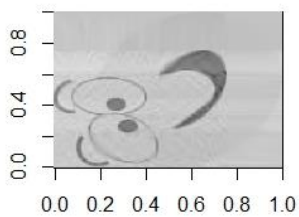
Error 0.02084154



20

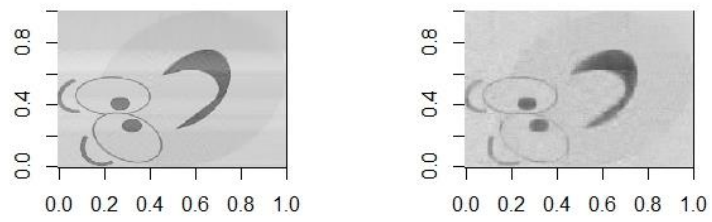
Information reserve 0.8050326

Error 0.01257145



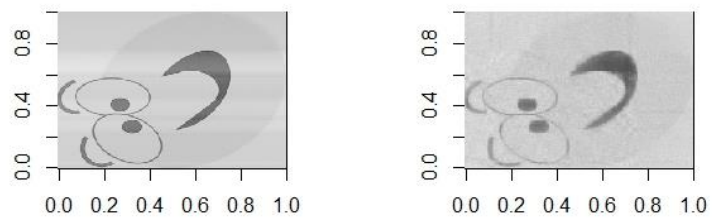
50

Information reserve 0.9041759 Error 0.009992646



100

Information reserve 0.9782281 Error 0.00998637



Information reserve 0.9977143 Error 0.009870262

We can find in this case, the ability of information reservation of NMF are better than PCA, however, the consequence are similar, we can see, over twenty demonstrate, we can see clearly the picture.