

So can consider -

$$E[|f'(t)| \mathbb{1}[|f'(t)| < 0] \mid f(t) = u]$$

$$= -E[X_1(t) \ddot{X}_1(t) + \dot{X}_1(t) \mathbb{1}[\ddot{X}_1(t) < 0] \mid X_1 \dot{X}_1 = u]$$

$$= -E\left[E\left(X_1(t) \ddot{X}_1(t) + \frac{u}{X_1}\right) \mathbb{1}\left[\ddot{X}_1 < \frac{u}{X_1} - \dot{X}_1^2\right] \mid X_1 \dot{X}_1 = u, X_1\right]\right]$$

$$= -E\left[\frac{\omega - \lambda^2 \sigma^{-2}}{M(\lambda)}\right]$$

$$\ddot{X}_1 \mid X_1 \sim N(-\lambda \sigma^{-2} X_1, \omega - \lambda^2 \sigma^{-2})$$

$$\Rightarrow X_1 \ddot{X}_1 + \frac{u}{X_1} \sim N\left(-\lambda \sigma^{-2} X_1^2, X_1^2 (\omega - \lambda^2 \sigma^{-2})\right)$$