

$$\mathbb{P}(X_I \in D \mid I, X_j = x)$$

$$= \mathbb{P}(X_I \in D \mid X_i \leq c \ i \notin I, X_i > c \ i \in I, X_j = x)$$

$$= \int \mathbb{P}(X_I \in D \mid X_i > c \ i \in I, X_i = x_i \ i \notin I, X_j = x)$$

$$\mathbb{P}(X \in D \mid X > c, X_i = x_i) \rightarrow \text{for } x_i > c$$



$$= \frac{\mathbb{P}(X \in D, X > c \mid X_i = x_i)}{\mathbb{P}(X > c \mid X_i = x_i)} = \mathbb{P}(X_j > c \ j \neq i \mid X_i = x_i)$$

↗ this is increasing

$$\int_{x > c} p(x \mid X_i = x_i) dx$$