

$$\mathbb{P}(\mu_n^S(\varepsilon) \geq 1)$$

$$\leq \frac{\mathbb{P}(\mu_{\leq \delta}(\varepsilon) \geq 1)}{\mathbb{P}(\mu_{\geq \delta}(\varepsilon) \geq 1)}$$

$$\lim_{\varepsilon \rightarrow 0} \frac{\mathbb{P}(\mu^u(\varepsilon) \geq 1)}{\mathbb{P}(\mu(\varepsilon) \geq 1)}$$

could show that ratio $\rightarrow 0$ as $\varepsilon \rightarrow 0$ for small δ

concentrate on a nearby point outside the open ball $B_\delta(x)$ having

$$\mathbb{P}(\mu_{\geq \delta}^u(\varepsilon) \geq 1) + \mathbb{P}(\mu_{\leq \delta}^u(\varepsilon) \geq 1)$$

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A

$$\mathbb{P}(\mu_{\geq \delta}^u(\varepsilon) \geq 1) + \mathbb{P}(\mu_{\leq \delta}^u(\varepsilon) \geq 1)$$

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$$\mathbb{P}(\mu_{\geq \delta}(\varepsilon) \geq 1)$$