

$$EX^k$$

$$E \left[ Z_{ij}^k \mathbb{1} \left[ \|Z\| > u^{1/2} n \right] \right]$$

$$Z = (H + u^{-1/2} P)$$

$$E[Z_{ij}]$$

$$EX^k \leq (EX)^k$$

Known

$$= E \left[ E[Z \dots | P] \right]$$

Known

$$= \mathbb{1} \left[ \sum_{ij} Z_{ij}^2 > u^{1/2} n \right]$$

$$\sum Z_{ij}^2 > u^{1/2} n$$

$$Z_{ij}^2 > \frac{u^{1/2} n}{D^2} \text{ some } ij$$

$$Z_{ij}^2 > \frac{u^{1/2} n}{D} \forall ij$$

So

$$\mathbb{1} \left[ Z_{ij}^2 > \frac{u^{1/2} n}{D} \forall ij \right] \leq \mathbb{1} \left[ \sum Z_{ij}^2 > u^{1/2} n \right]$$

$$\mathbb{1} \left[ Z_{ij}^2 > u^{1/2} n \right]$$