

$$\frac{Y_i - \hat{\mu}}{\hat{\sigma}}$$

$$| | + | |$$

$$|\hat{\mu} - \mu| < \varepsilon, \quad |\hat{\sigma} - \sigma| < \varepsilon$$

$$\left\| \frac{Y_i - \hat{\mu}}{\hat{\sigma}} \right\|^2$$

$$|a+b| \leq |a| + |b|.$$

$$\left| \frac{\hat{\sigma}}{\sigma} \right|$$

$$\left\| \frac{Y_i - \hat{\mu}}{\hat{\sigma}} \right\| = \left\| \frac{Y_i - \mu}{\hat{\sigma}} + \frac{\mu - \hat{\mu}}{\hat{\sigma}} \right\| \leq \left\| \frac{Y_i - \mu}{\hat{\sigma}} \right\| + \left\| \frac{\mu - \hat{\mu}}{\hat{\sigma}} \right\|$$

$$= \left[ \frac{\sigma}{\hat{\sigma}} \right] \left( \left\| \frac{Y_i - \mu}{\sigma} \right\| + \left\| \frac{\mu - \hat{\mu}}{\sigma} \right\| \right)$$

maybe need  $\sigma$  bounded below?

$$\leq \frac{\sigma}{\hat{\sigma}} \left( \left\| \frac{Y_i - \mu}{\sigma} \right\| + \varepsilon \right) = X_i$$