

$$\text{cov}(\nabla f(t)) = 0$$

$$\Rightarrow \mathbb{E}[\nabla^T f(t) \nabla f(t)] = 0$$

$$\nabla^2 f(h, h) = h^T \nabla^2 f h$$

$$(a \nabla f(t))$$

$$= \mathbb{E}[\text{vec}(\nabla^T(t) \nabla f(t))] = \mathbf{I}$$

$$\mathbb{E}[\nabla f_i(t) \nabla f_j(t)] = 0$$

$$\frac{\partial}{\partial t_i} \mathbb{E} \left[\frac{\partial}{\partial t_i} f(t) \frac{\partial}{\partial t_j} f(t) \right] = 0 \mathbf{I}$$

$$= \mathbb{E} \left[\frac{\partial^2}{\partial t_i^2} f(t) \frac{\partial}{\partial t_j} f(t) + \frac{\partial}{\partial t_i} f(t) \frac{\partial^2}{\partial t_i \partial t_j} f(t) \right] = 0$$

$$\frac{\partial}{\partial t_i} = \mathbb{E} \left[\frac{\partial^2 f}{\partial t_i \partial t_j} \frac{\partial}{\partial t_j} f + \frac{\partial}{\partial t_j} \frac{\partial^2 f}{\partial t_i \partial t_j} \right]$$

AX

$$\mathbb{E} \left[\frac{\partial^2 f}{\partial t_i \partial t_j} \frac{\partial}{\partial t_j} f \right] = - \mathbb{E} \left[\frac{\partial^2 f}{\partial t_j \partial t_i} \frac{\partial}{\partial t_i} f \right]$$

$$\begin{bmatrix} \square & \square \end{bmatrix}$$