

Fix  $h > 0$ , Then want to show that

①

$$P\left(\sup_{t \in B_{t_0}(h)} |Y(t) - Y(t_0)|\right)$$

20:20:200 | bootstrap  
non-bootstrap

Wlog  $t_0 = 0$ , want to show that:

$$\textcircled{4} P\left(\sup_{t \in B_{\sqrt{v}}(0)} |Y(t/\sqrt{v}(0)) - Y(0) + \frac{1}{2}t^T \Lambda t| \sqrt{v}(0)\right)$$

$\rightarrow 0$  as  $v \rightarrow \infty$

Proof:

$$\textcircled{4} \leq P\left(\sup_{t \in B_{\sqrt{v}}(0)} |Y(t/\sqrt{v}(0)) - Y(0) - \frac{t^T \nabla Y(0)}{\sqrt{v}(0)} - \frac{1}{2}t^T \frac{\nabla^2 Y(0)}{Y(0)} t| \sqrt{v}(0)\right) \textcircled{1}$$

$$+ P\left(\sup_{t \in B_{\sqrt{v}}(0)} \left| \frac{t^T \nabla Y(0)}{\sqrt{v}(0)} \right| \sqrt{v}(0)\right) \textcircled{2}$$

$$+ P\left(\sup_{t \in B_{\sqrt{v}}(0)} \left| \frac{1}{2}t^T \Lambda t - \frac{1}{2}t^T \frac{\nabla^2 Y(0)}{Y(0)} t \right| \sqrt{v}(0)\right) \textcircled{3}$$

$\rightarrow 0!$