To show the integrals bit,

have

$$\chi(f(c_r')) = \{f \in B(h\}: \chi$$