

$$\frac{d}{dt_j} R(t)$$

~~to~~

$$\frac{d}{dt_j} R(t, s) = \frac{d}{dt_j} \mathbb{E} [(X(t) - \mu)(X(s) - \mu)]$$

$$= \mathbb{E} [X_j(t) (X(s) - \mu)]$$

at $t=0$ get $\mathbb{E} [X_j(0) (X(s) - \mu)]$

so cov

$$\text{cov}(X_j(0), X(t)) = \mathbb{E} [X_j(0) (X(t) - \mu)]$$

$$= \mathbb{E} \left[\left(\frac{d}{ds} X_j(s) \right) \Big|_{s=0} (X(t) - \mu) \right]$$

$$\mathbb{E} [X_j(t) (X(s) - \mu)]$$