

Numerator

$$\underline{\text{Abs min}} = \left( \int_v^\infty p(y) \int \mathbf{1}[\|z\| > y\eta] \sum_{k=1}^D b_k(z) y^k p(z) dz dy \right)$$

$$\leq \int_v^\infty y^D p(y) \overset{\text{here since}}{b_D} \times P(\|z\| > y\eta) dy$$

$b_D = \frac{\det(\Lambda(t))}{\sigma^2}$

$$+ \sum_{k=0}^{D-1} \int_v^\infty |y|^k p(y) \int |b_k(z)| p(z) dz dy$$

$$\mathbb{E} \leq \int_v^\infty y^D p(y) |b_D| dy \times P(\|z\| > y\eta) \quad \text{①}$$

(as  $y \geq v \Rightarrow P(\|z\| > y\eta) \leq P(\|z\| > v\eta)$ )

$$+ \sum_{k=0}^{D-1} \int_v^\infty |y|^k p(y) \int |b_k(z)| p(z) dz dy. \quad \text{②}$$

$$\text{①} = |b_D|$$

$$+ (\text{poly of degree } \leq D-2) \times e^{-u^2/2\sigma^2} + \text{Constant}$$