

$\mathcal{F} := \{$

$$f \in \mathcal{F} \stackrel{C_b(\mathbb{R})}{\Rightarrow} f^+ = f \vee 0 \in \mathcal{F}$$

$$g \in C_b(\mathbb{R}^k) \Rightarrow g \vee 0 \in C_b(\mathbb{R}^k)$$

$$(f \vee 0)(z) = (g \vee 0)(z(t), \dots, z(k))$$

and clearly a vector space so ✓.

$g = \text{constant}$ gives constant f^n s.

given $x \neq y$

$$\text{need } \boxed{f(x) \neq f(y)}$$

$$\text{ie } z_1 \neq z_2 \in C^\infty(\tau)$$

$$\text{and } f(z_1) \neq f(z_2)$$

$$\text{let } g: \mathbb{R} \rightarrow \mathbb{R} \\ x \mapsto x$$

$$z_1 \neq z_2 \Rightarrow \exists t \text{ s.t. } z_1(t) \neq z_2(t)$$

$$\text{let } g = \text{id}; \mathbb{R} \rightarrow \mathbb{R} \text{ and let } f(z) = g(z(t))$$

$$\text{then } f(z_1) = z_1(t) \neq z_2(t) = f(z_2)!$$