

$$f' = \frac{y'}{\hat{\sigma}_1 / \sqrt{n}} \quad f' \approx \frac{y''}{\hat{\sigma}_1 / \sqrt{n}}$$

$$\text{Var}(y'') = \hat{\sigma}_2^2 / n$$

$$\Rightarrow \text{Var}(f') = \hat{\sigma}_2^2 / \hat{\sigma}_1^2$$


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So it follows that  $E[\hat{\varepsilon}_i(u) \hat{\varepsilon}_i(v)]$

$$\xrightarrow{n \rightarrow \infty} C(u, v)$$


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Also  $E[X_i X_i^T] = \Sigma_X$ !

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So the expectation of the inner parts of

$$\frac{1}{n} \sum_{i=1}^n \hat{\varepsilon}_i(u) \hat{\varepsilon}_i(v) X_i X_i^T \text{ converge.}$$

So triangular LLN applies

$$\Rightarrow \text{this converges to } C(u, v) \Sigma_X$$

still need to check  
translatability  
 under  $f^{\text{th}}$  moments  
on  $\varepsilon_i, X_i$ !