

$$E[z_j^k] \mathbb{1}[\|z\| > u^{1/2} \eta]$$

$$\int_{x^2+y^2 > u} x e^{-(x^2+y^2)} dx dy$$

discuss this issue with Dan!

$$= \int x e^{-x^2} dx \int e^{-y^2} dy$$

$$x^2+y^2 > \|y\|^2 \text{ to } y^2-x^2 \leq x^2+y^2$$

$$= \int x e^{-x^2}$$

change of var  
so the limits are independent

$$\leq \int x e^{-x^2}$$

$$\int_{y^2 \geq x^2} x^2 u^{1/2} \eta$$

$$\begin{aligned} Ax &= A \\ \text{and } A^{1/2} z &= I \end{aligned}$$

$$\int x^2 e^{-x^2}$$

$$x^2+y^2 > u^{1/2} \eta$$

$$\Leftrightarrow y^2 > u^{1/2} \eta - x^2$$

$$\mathbb{1}[x^2 < u^{1/2} \eta / 2], \quad \mathbb{1}[x^2 > u^{1/2} \eta / 2] \quad \text{integrate over.}$$

$$y^2 > u^{1/2} \eta / 2$$

$$y^2 > 0, \quad x^2 > u^{1/2} \eta / 2$$