

$$\text{Sym}(T_0^2(M)) = \bigcup_{t \in M} \text{Sym}(T_0^2(T_t(M)),$$

so at each

~~so for each~~

~~$g_t \in \text{Sym}$~~

$$g_t \in \text{Sym}(T_0^2(T_t(M)))$$

\bigcup_t section takes to $g_t \in \text{Sym}(T_0^2(T_t(M)))$

so g_t lives in X_t, X_t as. Done

Bilinear metric for Λ is $\boxed{x^T \Lambda y}$

$$\boxed{f: M \rightarrow \mathbb{R}} \quad \boxed{X_t f} \quad X_t f: M \rightarrow \mathbb{R}$$

vector fields are derivatives!

Take basis vectors in \mathbb{R}^2 then

$$g_t(X_1, X_2) = g_t\left(\frac{\partial}{\partial x_1}, \frac{\partial}{\partial x_2}\right)$$