

# Assignment #3

April 2020

Part 1)

1)  $67 + 4 + 1 = 72$  number of observations

2)  $H_0: B_1 = 0$

$H_a: B_1 \neq 0$

3)  $2.186/0.4104 = 5.3265$ .  $\alpha = .01 = 2.6524 < t_1$  which means we reject  $H_0$ , and the null hypothesis of  $B_1 = 0$ .  $X$  is then stated as a valid indicator for  $Y$ .

4)  $R^2 = SSR/SSt = SSR/SSR + SSE = (1974.53 + 118.8642 + 32.4701 + .4356) / (1974.53 + 118.8642 + 32.4701 + .4356 + 630.36) = .7713$ . Variation is 77.13%.

5)  $.7713 - (1 - .7713) * 4/(72-4-1) = .7577$ . Here, adjusted R-squared is different from R-squared values because R-squared assumes that all independent variables are necessary for explaining variation in dependent variables, while adjusted R-squared penalizes and lowers the score for adding independent variables that do not help in predicting dependent variables.

6)  $H_0: B_1 = B_2 = B_3 = B_4 = 0$

$H_a: B_i \neq 0$  (not equal to zero), for  $i \in 1, 2, 3, 4$

7)  $((1974.53 + 118.8642 + 32.4701 + .4356)/4) / ((630.36/72-4-1)) = 56.5003$

When  $p=4$  and freedom  $=67$ ,  $p$  value  $<.0001$ . This means that at least one of the slope parameters is zero and we can reject the null hypothesis.

Part 2)

8) Model 1 nests Model 2 because there are far more explanatory variables in model 2 that are not in Model 1, whilst all of the variables in Model 1 are in Model 2.

9)  $H_0: B_5 = B_6 = 0$

$H_a: B_i \neq 0$  (not equal to) 0, for  $i \in 5, 6$

10)  $F = ((630.36 - 572.6091)/(7 - 5)) / ((572.6091 / (72 - 6 - 1)) = 3.2778$

$F_{95,2,65} = 3.1381$

Again the null hypothesis is rejected as model 1 is still more powerful than model 2.

11) The 10 continuous variables:

Sales Price, Year Sold, Sub Class, Lot Area, Neighborhood, Building Type, House Style, Overall Condition, Year Built, and Garage cars.

It is interesting to put these into different sets as on the surface they variables seem very disparate. However I chose to break it into: Main House characteristics: Lot Area, Building type, House Style, Garage Cars, Overall Condition, and Year Built. The other is Ancillary Housing conditions: Sales Price, Year Sold, Sub Class, Neighborhood. The reason I broke them into these two sets was the actual

structure and bones of the homes which are main house characteristics, while ancillary characteristics are variables like neighborhood that describe the are of the house and not the structure itself.

12)

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Call:
lm(formula = SalePrice ~ LotArea + BldgType + HouseStyle + GarageCars +
    overallCond + YearBuilt, data = new)

Residuals:
    Min       1Q   Median       3Q      Max
-224786  -33046   -7862    20073   466456

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) -2.176e+06  9.172e+04 -23.729  < 2e-16 ***
LotArea      1.654e+00  1.328e-01  12.459  < 2e-16 ***
BldgType2fmCon -4.067e+03  7.009e+03  -0.580   0.5618
BldgTypeDuplex -2.630e+04  5.346e+03  -4.919  9.17e-07 ***
BldgTypeTwnhs -3.862e+04  5.662e+03  -6.821  1.09e-11 ***
BldgTypeTwnhsE -1.082e+04  3.893e+03  -2.778   0.0055 **
HouseStyle1.5Unf -1.563e+04  1.256e+04  -1.245   0.2134
HouseStyle1Story -1.819e+04  3.624e+03  -5.019  5.50e-07 ***
HouseStyle2.5Fin  9.032e+04  1.906e+04   4.737  2.27e-06 ***
HouseStyle2.5Unf  5.057e+04  1.131e+04   4.471  8.08e-06 ***
HouseStyle2Story -1.932e+03  3.888e+03  -0.497   0.6192
HouseStyleSFoyer -4.126e+04  6.882e+03  -5.994  2.29e-09 ***
HouseStyleSLvl  -3.623e+04  5.790e+03  -6.258  4.48e-10 ***
GarageCars     4.219e+04  1.599e+03  26.391  < 2e-16 ***
OverallCond     8.116e+03  9.651e+02   8.410  < 2e-16 ***
YearBuilt      1.134e+03  4.683e+01  24.222  < 2e-16 ***
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Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 53110 on 2913 degrees of freedom
(1 observation deleted due to missingness)
Multiple R-squared:  0.5605,    Adjusted R-squared:  0.5582
F-statistic: 247.7 on 15 and 2913 DF,  p-value: < 2.2e-16
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B1 is Lot Area

$H_0: B1 = 0$

$H_a: B1 \neq 0$

$T1 = 1.654 / 1.328 = 1.2455$

t-test with  $\alpha = .05$

$t_a = 69.708 > |t1|$ , reject the null

B2 is GarageCars

$T1 = 4.219 / 1.599 = 2.6385$

$T_a = 125.72 > |t_1|$ , reject the null

B3 is Overall Condition

$T_1 = 8.116/9.651 = .8409$

$T_a = 270.91 > |t_1|$ , reject the null

B4 is YearBuilt

$T_1 = 1.134/4.683 = .2421$

$T_a = 3528.1 > |t_1|$ , reject the null

b)

$H_0: \beta_1 = \beta_2 = \beta_3 = \beta_4 = 0$  versus  $H_a: \beta_1 \neq 0$  for  $E_1, 2, 3, 4$

F-statistic = 247.7, reject the null

Part 4)

13)

a)

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Call:
lm(formula = SalePrice ~ LotArea + BldgType + HouseStyle + GarageCars +
    overallCond + YearBuilt + YrSold + SubClass + Neighborhood,
    data = new)
```

Residuals:

Min	1Q	Median	3Q	Max
-184578	-23443	-3146	16341	401435

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	-5.251e+05	1.223e+06	-0.429	0.667761	
LotArea	1.340e+00	1.139e-01	11.762	< 2e-16	***
BldgType2fmCon	1.532e+04	1.320e+04	1.161	0.245862	
BldgTypeDuplex	-8.055e+03	6.049e+03	-1.332	0.183107	
BldgTypeTwnhs	-4.832e+04	1.058e+04	-4.566	5.17e-06	***
BldgTypeTwnhse	-2.724e+04	9.330e+03	-2.920	0.003529	**
HouseStyle1.5Unf	-1.761e+04	1.020e+04	-1.726	0.084460	.
HouseStyle1story	-1.564e+04	3.716e+03	-4.207	2.66e-05	***
HouseStyle2.5Fin	8.210e+04	1.575e+04	5.213	1.99e-07	***
HouseStyle2.5Unf	4.175e+04	9.230e+03	4.523	6.35e-06	***
HouseStyle2story	5.318e+03	3.501e+03	1.519	0.128831	
HouseStyleSFoyer	-1.289e+04	6.205e+03	-2.078	0.037778	*
HouseStyleSLvl	-9.941e+03	5.609e+03	-1.772	0.076419	.
GarageCars	2.747e+04	1.396e+03	19.679	< 2e-16	***
OverallCond	8.107e+03	7.912e+02	10.246	< 2e-16	***
YearBuilt	9.609e+02	6.102e+01	15.748	< 2e-16	***
YrSold	-6.262e+02	6.052e+02	-1.035	0.300876	
SubClass	-1.522e+02	8.813e+01	-1.727	0.084309	.
NeighborhoodBlueste	-2.234e+04	1.611e+04	-1.387	0.165585	
NeighborhoodBrDale	-2.127e+04	1.242e+04	-1.711	0.087100	.
NeighborhoodBrkside	-3.054e+04	1.043e+04	-2.927	0.003452	**
NeighborhoodClearCr	-8.642e+03	1.116e+04	-0.775	0.438599	
NeighborhoodCollgCr	-3.262e+04	9.077e+03	-3.593	0.000332	***
NeighborhoodCrawfor	2.200e+04	1.003e+04	2.192	0.028450	*
NeighborhoodEdwards	-3.862e+04	9.584e+03	-4.029	5.74e-05	***
NeighborhoodGilbert	-5.227e+04	9.461e+03	-5.525	3.59e-08	***
NeighborhoodGreens	4.281e+04	1.744e+04	2.455	0.014139	*
NeighborhoodGrnHill	1.286e+05	3.136e+04	4.101	4.22e-05	***
NeighborhoodIDOTRR	-4.024e+04	1.065e+04	-3.780	0.000160	***
NeighborhoodLandmrk	-2.969e+04	4.392e+04	-0.676	0.499144	
NeighborhoodMeadowv	-2.207e+04	1.150e+04	-1.920	0.054983	.
NeighborhoodMitchel	-4.844e+04	9.673e+03	-5.007	5.85e-07	***
NeighborhoodNames	-3.862e+04	9.251e+03	-4.174	3.08e-05	***
NeighborhoodNoRidge	6.752e+04	1.020e+04	6.623	4.19e-11	***
NeighborhoodNPkVill	-1.133e+04	1.248e+04	-0.908	0.363964	
NeighborhoodNridght	7.462e+04	9.094e+03	8.206	3.41e-16	***
NeighborhoodNWames	-3.200e+04	9.603e+03	-3.332	0.000873	***
NeighborhoodOldTown	-3.181e+04	1.013e+04	-3.142	0.001698	**
NeighborhoodSawyerw	-4.867e+04	9.672e+03	-5.031	5.17e-07	***
NeighborhoodSawyerw	-3.745e+04	9.504e+03	-3.941	8.32e-05	***
NeighborhoodSomerst	1.166e+03	9.025e+03	0.129	0.897229	
NeighborhoodStoneBr	9.792e+04	1.023e+04	9.572	< 2e-16	***
NeighborhoodSWISU	-1.647e+04	1.153e+04	-1.428	0.153387	
NeighborhoodTimber	-2.664e+03	1.010e+04	-0.264	0.791965	
NeighborhoodVeenker	2.517e+04	1.225e+04	2.054	0.040034	*

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signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

B1 is Year Sold

H0:B1 = 0

$H_a: B1 \neq 0$

$$T1 = -6.262 / 6.052 = 1.0347$$

t-test with  $\alpha = .05$

$t_{\alpha} = 82456 > |t1|$ , reject the null

B2 is Subclass

$$T1 = -1.522 / 8.813 = -.1727$$

t-test with  $\alpha = .05$

$t_{\alpha} = 72.84 > |t1|$ , reject the null

b)

F-statistic = 166.9, reject the null

$H_0: \beta_1 = \beta_2 = \beta_3 = \beta_4 = \beta_5 = \beta_6 = 0$  versus  $H_a: B1$  for E 1,2,3,4, 5, 6

14)

$H_0: \beta_5 = \beta_6 = \beta_7 = \beta_8 = \beta_9 = \beta_{10} = 0$  versus  $H_a: B1$  for E 5,6,7,8,9,10

F-statistic = 127.62, reject the null