let have prime factorization

let

let M represent the set of all multiplicative functions

let represent the set of all prime numbers

consider

the divisors of are

therefore,

we will now establish that

when ,

assume that

for some arbitrary integer,

consider the next term,

consider the expression

the next term

we have established by mathematical induction that

therefore,