

Perceptron

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Abstract

The perceptron algorithm is one of the simplest machine learning algorithms. It is a form of supervised learning that takes a set of predictor variables and classifies observations into a binary class. This report takes an implementation of the Perceptron algorithm and measures its performance at classifying observations as either having diabetes or not. Investigations into model variability and optimal iteration values were conducted and the impact these have on the overall model performance are discussed.

1. Introduction

Perceptron is one of the simplest machine learning algorithms. Perceptron is a supervised learning algorithm that takes a combination of parameters to make a binary classification. Perceptron was initially developed in 1958 [1] however was not fully utilised until much later when it was used in machine learning as a part of multi layer neural networks. The single layer Perceptron is able to "learn" from a set of information and provide output based on the input information. Perceptron works by iteratively calculating a set of weights based on the dimension size of the features in the dataset, D . The output of which is a line or D dimension plane that separates the observations into two categories. Perceptron calculates the updated weights iteratively and in an ideal world will converge to a D dimension vector of values that separates all values into their correct groups. Where the data is not able to be separated cleanly into two groups the Perceptron algorithm will never converge. This requires a max iteration value to be set such that the problem is bounded. If a max iteration value is not set the Perceptron algorithm can keep moving back and forth trying to cleanly separate the training observations into the correct groups. Determining the optimal max iterations for the dataset will be investigated in the method section of the report.

In this project the Perceptron algorithm was implemented on the Pima Indians Diabetes Database open source dataset [3]. This dataset contains a set of eight medical predictor variables, the number of pregnancies the patient has had, their BMI, insulin level, plasma glucose concentration,

blood pressure, skin fold thickness, age and their diabetes pedigree. The dataset also contains an outcome variable which is either the patient has diabetes or they don't have diabetes. The predictor variables are each one of the D dimensions.

2. Method

As outlined in the introduction section the goal of the Perceptron algorithm is to separate the entries in the dataset into one of two binary groups. The data is read into a python array of dictionaries with the features being stored in a D dimensional array and the outcome stored as a signed integer. The data is then split into a training and testing set using the scikit learn train test function. An 80-20 training testing split was used [2].

The Perceptron algorithm takes an input layer which is the set of features in each observation, let the vector of features for observation i be defined as x_i . Let the collection of these observations be defined as X . Each of these observations have an outcome variable which is whether the patient has diabetes or not. Let the outcome for the i_{th} observation be defined as y_i . This outcome variable is either $+1$ if the patient has diabetes or -1 if the patient doesn't have diabetes. Let the collection of all the outcomes for each observation be defined as Y . The Perceptron algorithm starts by creating a D dimension vector of weights, defined as W . For this implementation the initial W is set as a D dimension zero vector. A bias value is also required which is defined as b initially set to 0. This bias shifts the intercept of the dimensions linear separator away from 0 and is required as it may not be possible to split the data points if this doesn't occur.

The Perceptron algorithm works by calculating the dot product of x_i and W and adding the bias, b . The sign function is then passed the result and this is our activation function corresponding to the possible values of the outcome variable mentioned above. The sign function is defined as

$$\text{sign}(x) = \begin{cases} -1 & \text{if } x < 0 \\ 0 & \text{if } x = 0 \\ +1 & \text{if } x > 0 \end{cases} \quad (1)$$

To determine if the perceptron has correctly classified

the observation, the result of the sign function corresponds to the outcome variable possibilities of whether a patient has diabetes or not. Therefore, the whole process of making a prediction on an observation is defined as.

$$f(x) = \text{sign}((x_i \cdot W) + b) \quad (2)$$

Using the predictions from equation (2) the weight vector, W can be updated during the training process. By multiplying the prediction by the actual class of the observation and checking the resulting value is > 0 the update logic can be simplified. If the result is > 0 then the perceptron has made a correct prediction and does not need to be updated. This can be seen in the logic table below showing if a correct prediction is made the result will always be > 0 and if an incorrect prediction is made the result will be ≤ 0

Truth	Prediction	Output
1	1	1
1	-1	-1
-1	1	-1
-1	-1	1

Table 1. Prediction vs truth logic table for predictions

If the perceptron makes an incorrect prediction during the training phase W is updated by multiplying y_i with x_i . Let W at the current time be defined as W_t . This update step is defined as

$$W_{t+1} = W_t + (y_i * x_i) \quad (3)$$

A learning rate value, α , can be used when updating W however in the case of the single layer Perceptron, it does not effect the final result as it will converge on a stable solution regardless. What it can be used for is altering the volatility of the updates to W and in some cases can speed up the rate at which the algorithm converges. The equation for updating W that includes the α value is defined as

$$W_{t+1} = W_t + \alpha(y_i * x_i) \quad (4)$$

Similarly, b needs to be updated in the case of an incorrect prediction. Let b at the current time be defined as b_t . The update step is defined as

$$b_{t+1} = b_t + y_i \quad (5)$$

This process is repeated for every observation in the training set. In an ideal scenario this process would be repeated until every element has been correctly classified, however this is most often not possible. Where the data is not linearly separable on a given dimension the Perceptron algorithm will not be able to converge on a solution. To address this a max iteration value must be set which will set a stop point for the algorithm if it fails to converge. This max

iteration value is the number of times the algorithm will iterate over the entire training dataset during the training phase. Different values will be investigated in the results section to examine the impact it has on the overall model performance.

3. Results

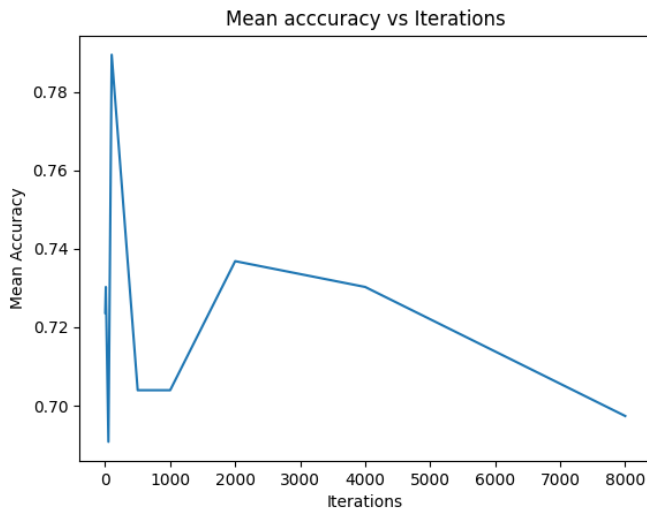
3.1. Max Iteration Investigation

As discussed above the max iteration value used during the training phase can have a big impact on the overall model performance. Allowing the model time to converge on an optimal or near optimal solution is paramount. To determine the appropriate magnitude of the max iteration value, various values were set during the training phase. A set seed was passed to the function that splits the data into the training and testing set to ensure each value of max iterations was being tested on the same data. To reduce the variance in the results, which will be investigated later, each max iteration value was run 10 times and the mean of the model accuracy was calculated.

Iterations	Mean Accuracy
1	0.723
10	0.730
50	0.753
100	0.789
500	0.703
1000	0.703
2000	0.736
4000	0.730
8000	0.697

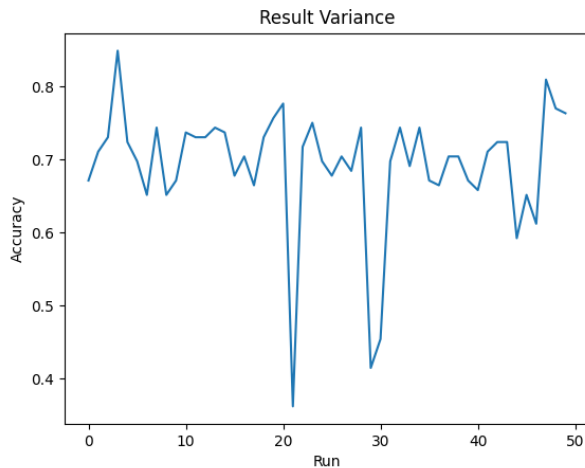
Table 2. Iterations vs mean accuracy

Plotting the results from the table above it can be observed that as the number of max iterations increases, the corresponding mean accuracy of the Perceptron algorithm also increases before reaching an equilibrium. For the highest magnitude max iterations the accuracy begins to drop off. This will be investigated in the discussion section. There is also a spike at the iteration value of 100 and this will be investigated in the discussion section.



3.2. Result Variance Investigation

The variance of the final model accuracy result is highly dependent on the data selected for the training set. Since the data is randomly selected, the final model W vector and b can vary greatly. The impact of this was investigated by running the Perceptron algorithm 50 times with an iteration value of 2000 which was found to provide the best, stable results.



From the plot above it can be observed that the variance of the Perceptron algorithm can vary greatly depending on the initial split. This can possibly be mitigated and approaches for this will be investigated in the discussion section

4. Discussion

The Perceptron algorithm can be very effective at predicting diabetes using the Pima Indian dataset. Depending on the number of iterations and the data chosen for the training set accuracy as high as approximately 0.83 has been ob-

served. It can be highly variable in its performance due to the datasets small size and the lack of a solution that splits all the observations into the correct groups. With the dataset only containing 768 observations, when it is split into the training and testing sets the training set only contains 614 observations. This small set of observations leads to variability in the models performance depending on the sample selected. To address this a bigger dataset could be used which would result in a reduced impact on the final results caused by the small number of observations.

For this report, outlier data was not accounted for. This could have compounded with the small dataset size to increase the variability of the final results. If the training dataset contained a high proportion of observations with outlier data the final W would not result in optimal results when run against the testing set. Where there is missing data in the observation, the value is set to -1 which does impact the updating of the W vector. Imputing these values will be discussed in the future work section of this report.

5. Future Work

For future work on this problem building a system that trains multiple W vectors and uses the mean of them as the final value will be investigated. This would reduce the highly variable results caused by the differences in the training set chosen. It is possible that this could result in the Perceptron overfitting the data as given enough iterations of the model training it is likely the vast majority of the observations would be included in one or multiple iterations. The impact of this should be reduced since the weights of a given observation on the trained model would only be included in a subset of the training iterations. Other future work would be to address the outlier data through omitting observations that contain outlier values or devising a method of keeping them out of the training set which would likely increase the models average performance. Another approach would be to replace the missing values in any given observation with the mean value of the dataset.

6. Conclusion

The Perceptron algorithm performs well at predicting diabetes based on the available variables from the Pima Indians dataset. With the small dataset available the Perceptron algorithm is able to make predictions with an average accuracy of approximately 0.75. This result is highly dependant on the subset of the data used for the training set and an investigation was completed to investigate this. It was found that using this dataset, the Perceptron was never able to converge on a solution that separated all of the observations into their correct groups. The impact on model performance from different max iterations was investigated and it was found that a good balance of variability and performance occurred at approximately 2000 iterations. Strate-

gies were outlined in the future work section of this report for addressing variability present in the model training process and handling of missing data from some of the observations.

References

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7. Appendix

Github repository link: https://github.com/sjg546/COMPSCI7318_Assignment1