Real dimension in numerical Newtonian gravitation

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Abstract

This paper contains a short introduction to Newtonian gravitation. The main focus is on some C++ code.

1 Brute force: integer field line count

Regarding the holographic principle, where n is the gravitational field line count, and A_s is the Schwarzschild black hole event horizon area:

$$n = \frac{A_s k c^3}{4G\hbar \log 2},\tag{1}$$

the Schwarzschild radius is:

$$r_s = \sqrt{\frac{A_s}{4\pi}} = \sqrt{\frac{nG\hbar \log 2}{kc^3\pi}},\tag{2}$$

and the mass is:

$$M = \frac{c^2 r_s}{2G} = \sqrt{\frac{nc\hbar \log 2}{4Gk\pi}}.$$
 (3)

Where R is some far distance from the centre of the gravitating body (e.g, $R \gg r_s$), β is the get intersecting line length function and ϵ is some small value (e.g 10^{-5}), the gradient is:

$$\gamma = \frac{\beta(R+\epsilon) - \beta(R)}{\epsilon}.\tag{4}$$

The gradient strength is:

$$g = -\gamma \pi = \frac{n}{2R^3}. (5)$$

From this we can get the Newtonian acceleration a for a flat rotation curve of speed v:

$$a = \frac{v^2}{R} = \frac{gRc\hbar \log 2}{k2\pi M},\tag{6}$$

$$v = \sqrt{\frac{gR^2c\hbar\log 2}{k2\pi M}}. (7)$$

The ratio of $a_{2.001}/a_3$ is equal to R.

The code for this section can be downloaded from:

https://github.com/sjhalayka/ellipsoid_emitter

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References

- [1] Misner et al. Gravitation. (1970)
- [2] 't Hooft. Dimensional reduction in quantum gravity. (1993)
- [3] Susskind. The World as a Hologram. (1994)
- [4] Fiedler. Fix Your Timestep! (2004)
- [5] Fiedler. Integration Basics. (2004)