# Newtonian gravitation for C++ programmers

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#### Abstract

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### 1 Numerical: integer field line count

Where r is the receiver radius, R is the distance from the centre of the emitter,  $\beta$  is the get intersecting line count function, and n is the field line count, the gradient is:

$$\alpha = \frac{\beta(R+\epsilon) - \beta(R)}{\epsilon}.$$
 (1)

The gradient strength is:

$$g = \frac{-\alpha}{r^2}. (2)$$

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```
int main(int argc, char** argv)
        // Field line count
        const size_t n = 10000000000;
        cout << "Allocating memory for field lines" << endl;</pre>
        vector<vector_3> unit_vectors(n);
        for (size_t i = 0; i < n; i++)
                unit_vectors[i] = RandomUnitVector();
                static const size_t output_mod = 10000;
                if (i % output_mod = 0)
                         cout << "Getting pseudorandom locations: "</pre>
                        << static_cast < float > (i) / n << endl;
        }
        string filename = "newton.txt";
        ofstream out_file(filename.c_str());
        out_file << setprecision (30);
        const real_type start_distance = 10.0;
        const real_type end_distance = 100.0;
        const size_t distance_res = 1000;
        const real_type distance_step_size =
                (end_distance - start_distance)
                / (distance_res - 1);
        for (size_t step_index = 0; step_index < distance_res; step_index++)
                const real_type r =
                         start_distance +
                         step_index * distance_step_size;
                const vector_3 receiver_pos(r, 0, 0);
                const real_type receiver_radius = 1.0;
                const real_type epsilon = 1.0;
                vector_3 receiver_pos_plus = receiver_pos;
                receiver_pos_plus.x += epsilon;
                const long long signed int collision_count_plus =
                         get_intersecting_line_count(
                                 unit_vectors,
                                 receiver_pos_plus,
                                 receiver_radius);
                const long long signed int collision_count =
                         get_intersecting_line_count(
                                 unit_vectors,
```

### 2 Analytical: real field line count

Where r is the receiver radius, R is the distance from the centre of the emitter,  $\beta$  is the get intersecting line count function, and n is the field line count, the gradient is:

$$\alpha = \frac{\beta(R+\epsilon) - \beta(R)}{\epsilon}.$$
 (3)

Here we assume that the maximum number of field lines is given by the holographic principle:

$$n = \frac{c^3 A}{4G\hbar \log 2}. (4)$$

The gradient strengths are:

$$g = \frac{-\alpha}{r^2} \approx \frac{n}{2R^3},\tag{5}$$

$$g_N = \frac{nc\hbar \log 2}{4\pi M R^2} = \frac{c^4 A}{16\pi G M R^2} = \frac{GM}{R^2}.$$
 (6)

```
pi * sphere_radius * sphere_radius;
        const real_type ratio =
                small_area / big_area;
        return n * ratio;
int main(int argc, char** argv)
        const real_type emitter_radius = 1.0;
        const real_type emitter_area =
                4.0 * pi * emitter_radius * emitter_radius;
        // Field line count
        // re: holographic principle:
        const real_type n =
                (c3 * emitter_area)
                / (\log (2.0) * 4.0 * G * hbar);
        const real_type emitter_mass = c2 * emitter_radius / (2.0 * G);
        // 1.73502e+70 is the 't Hooft-Susskind constant:
        // the number of field lines for a black hole of
        // unit Schwarzschild radius
        //const\ real_type\ G_- =
                (c3 * pi)
                / (log(2.0) * hbar * 1.73502e+70);
        const string filename = "newton.txt";
        ofstream out_file(filename.c_str());
        out_file << setprecision(30);
        const real_type start_distance = 10.0;
        const real_type end_distance = 100.0;
        const size_t distance_res = 1000;
        const real_type distance_step_size =
                (end_distance - start_distance)
                / (distance_res - 1);
        for (size_t step_index = 0; step_index < distance_res; step_index++)
                const real_type r =
                        start_distance + step_index * distance_step_size;
                const vector_3 receiver_pos(r, 0, 0);
                const real_type receiver_radius = 1.0;
                const real_type epsilon = 1.0;
                vector_3 receiver_pos_plus = receiver_pos;
```

```
receiver_pos_plus.x += epsilon;
        // https://en.wikipedia.org/wiki/Directional_derivative
        const real_type collision_count_plus =
                get_intersecting_line_count(
                         receiver_pos_plus,
                         receiver_radius);
        const real_type collision_count =
                get_intersecting_line_count(
                         receiver_pos,
                         receiver_radius);
        const real_type gradient =
                (collision_count_plus - collision_count)
                / epsilon;
        real_type gradient_strength =
                -gradient
                / (receiver_radius * receiver_radius);
        const real_type gradient_strength_ =
                n / (2.0 * pow(receiver_pos.x, 3.0));
        const real_type newton_strength =
                n * c * hbar * log(2.0)
                (pow(receiver_pos.x, 2.0)
                         * emitter_mass * 4.0 * pi);
        const real_type newton_strength_ =
                c4 * emitter_area
                / (16.0 * pi * G)
                         * pow(receiver_pos.x, 2.0) * emitter_mass);
        const real_type newton_strength__ =
                G * emitter_mass / pow(receiver_pos.x, 2.0);
        //cout \ll newton\_strength\_\_ / newton\_strength \ll endl;
        \operatorname{cout} << "r: " << r << " gradient strength: "
                << gradient_strength << endl;</pre>
        out_file << r << " " << gradient_strength << endl;
}
out_file.close();
return 0;
```

# 3 Newtonian gravitational integration

```
vector_3 Newtonian_acceleration(
        const real_type emitter_mass,
        const vector_3& pos, // Receiver pos
        const real_type G)
        vector_3 grav_dir = vector_3(0, 0, 0) - pos;
        const real_type distance = grav_dir.length();
        grav_dir.normalize();
        vector_3 accel = grav_dir * G * emitter_mass / pow(distance, 2.0);
        return accel;
void proceed_Euler(
        vector_3& pos,
        vector_3& vel,
        const real_type G,
        const real_type dt)
        vector_3 accel =
                Newtonian_acceleration (
                        emitter_mass,
                         pos,
                        G);
        vel += accel * dt;
        pos += vel * dt;
void idle_func(void)
        proceed_Euler(receiver_pos, receiver_vel, G, dt);
void proceed_symplectic4(
        vector_3& pos,
        vector_3& vel,
        real_type G,
        real_type dt)
        static real_type const cr2 =
                pow(2.0, 1.0 / 3.0);
        static const real_type c[4] =
                1.0 / (2.0 * (2.0 - cr2)),
                (1.0 - cr2) / (2.0 * (2.0 - cr2)),
                (1.0 - cr2) / (2.0 * (2.0 - cr2)),
                1.0 / (2.0 * (2.0 - cr2))
        };
```

```
static const real_type d[4] =
       0.0
};
pos += vel * c[0] * dt;
vel += Newtonian_acceleration(
               emitter_mass,
               pos,
               G) * d[0] * dt;
pos += vel * c[1] * dt;
vel += Newtonian_acceleration(
               emitter_mass,
               pos,
               G) * d[1] * dt;
pos += vel * c[2] * dt;
vel += Newtonian_acceleration(
               emitter_mass,
               pos,
               G) * d[2] * dt;
pos += vel * c[3] * dt;
// last element d[3] is always 0
```