# On numerical quantum Schwarzschild gravity

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#### Abstract

This paper contains a short introduction to isotropic Schwarzschild gravitation.

### 1 Introduction

First see [1] for a short tutorial for C++ programmers on isotropic Newtonian gravitation. In [1] we build an isotropic gravitational field through the use of pseudorandomly generated field lines. In [1] we use a sphere as the receiver.

In this paper, we find a match between the numerical gravitation and the gravitational time dilation from Schwarzschild's general relativity [2–4]. Here, we use an axis-aligned bounding box (AABB) as the receiver.

In this paper we use Planck units, where  $c = G = \hbar = k = 1$ , which simplifies the equations. Note that a length of 1 means 1 Planck length, not 1 metre.

## 2 Method

Where  $r_e$  is the emitter's Schwarzschild radius,  $r_r$  is the receiver AABB radius (e.g. half of the AABB side length),  $\beta$  is the get intersecting line density function, and 1e12 and 0.01 are arbitrary constants:

$$r_e = \sqrt{\frac{1e12\log(2)}{\pi}}\tag{1}$$

$$r_r = r_e \times 0.01 \tag{2}$$

$$A_e = 4\pi r_e^2 \tag{3}$$

$$n_e = \frac{A_e}{4\log(2)} = 1e12 \tag{4}$$

$$M_e = \frac{r_e}{2} \tag{5}$$

Where R is the distance from the emitter's centre:

$$\alpha = \frac{\beta(R+\epsilon) - \beta(R)}{\epsilon}.$$
 (6)

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The gradient strength is:

$$g = \frac{-\alpha}{r_r^2} \approx \frac{n_e}{2R^3}. (7)$$

From this we can get the Newtonian acceleration  $a_N$ :

$$a_N = \frac{gR\log 2}{8M_e} = \sqrt{\frac{n_e \log 2}{4\pi R^4}} = \frac{M_e}{R^2}.$$
 (8)

We can also get a general relativistic acceleration  $a_S$ , where  $r_e < R$ :

$$t = \sqrt{1 - \frac{r_e}{R}},\tag{9}$$

$$a_S \approx \frac{r_e}{t\pi R^2}. (10)$$

```
real_type intersect_AABB(
        const vector_3 min_location,
        const vector_3 max_location ,
        const vector_3 ray_origin,
        const vector_3 ray_dir ,
        real_type& tmin,
        real_type& tmax)
        tmin = (min_location.x - ray_origin.x) / ray_dir.x;
        tmax = (max\_location.x - ray\_origin.x) / ray\_dir.x;
        if (tmin > tmax) swap(tmin, tmax);
        real_type tymin = (min_location.y - ray_origin.y) / ray_dir.y;
        real_type tymax = (max_location.y - ray_origin.y) / ray_dir.y;
        if (tymin > tymax) swap(tymin, tymax);
        if ((tmin > tymax) | | (tymin > tmax)) return 0;
        if (tymin > tmin) tmin = tymin;
        if (tymax < tmax) tmax = tymax;
        real_type tzmin = (min_location.z - ray_origin.z) / ray_dir.z;
        real_type tzmax = (max_location.z - ray_origin.z) / ray_dir.z;
        if (tzmin > tzmax) swap(tzmin, tzmax);
        if ((tmin > tzmax) \mid | (tzmin > tmax)) return 0;
        if (tzmin > tmin) tmin = tzmin;
        if (tzmax < tmax) tmax = tzmax;
        if (tmin < 0 \mid | tmax < 0) return 0;
        vector_3 ray_hit_start = ray_origin;
        ray_hit_start.x += ray_dir.x * tmin;
        ray_hit_start.y += ray_dir.y * tmin;
        ray_hit_start.z += ray_dir.z * tmin;
        vector_3 ray_hit_end = ray_origin;
        ray_hit_end.x += ray_dir.x * tmax;
        ray_hit_end.y += ray_dir.y * tmax;
        ray_hit_end.z += ray_dir.z * tmax;
```

```
real_type l = (ray_hit_end - ray_hit_start).length();
        return 1;
vector_3 random_cosine_weighted_hemisphere(const vector_3& normal)
        // Generate two random numbers
        real_type u1 = dis(generator);
        real_type u2 = dis(generator);
        // Malley 's method
        // (cosine-weighted hemisphere sampling)
        // Sample uniformly on a disk,
        // then project up to hemisphere
        real_type r = sqrt(u1);
        real_type theta = 2.0 * pi * u2;
        // Point on unit disk
        real_type x = r * cos(theta);
        real_type y = r * sin(theta);
        // Height above disk
        real_type z = sqrt(1.0 - u1);
        // Create orthonormal basis around normal
        vector_3 n = normal;
        n.normalize();
        // Choose an arbitrary vector
        // not parallel to normal
        vector_3 arbitrary;
        if (fabs(n.x) > 0.9)
                arbitrary = vector_3(0, 1, 0);
        else
                arbitrary = vector_3(1, 0, 0);
        // Create tangent and bitangent
        vector_3 tangent = n.cross(arbitrary);
        tangent.normalize();
        vector_3 bitangent = n.cross(tangent);
        bitangent.normalize();
        // Transform from local coordinates
        // to world coordinates
        vector_3 result;
        result.x = tangent.x * x +
                bitangent.x * y + n.x * z;
        result.y = tangent.y * x +
                bitangent.y * y + n.y * z;
        result.z = tangent.z * x +
                bitangent.z * y + n.z * z;
```

```
return result.normalize();
std::optional<real_type> intersect(
        const vector_3 location ,
        const vector_3 normal,
        const real_type receiver_distance,
        const real_type receiver_radius)
        const vector_3 circle_origin(receiver_distance, 0, 0);
        if (normal.dot(circle_origin) <= 0)</pre>
                return std::nullopt;
        vector_3 min_location(
                -receiver_radius + receiver_distance,
                -receiver_radius,
                -receiver_radius);
        vector_3 max_location(
                receiver_radius + receiver_distance,
                 receiver_radius,
                receiver_radius);
        real_type tmin = 0, tmax = 0;
        real_type AABB_hit = intersect_AABB(
                 min_location,
                max_location,
                location,
                normal,
                tmin,
                tmax);
        if (AABB_hit > 0)
                return AABB_hit;
        return std::nullopt;
// Beta function, for Newtonian gravitation
real_type get_intersecting_line_density(
        const long long unsigned int n,
        const real_type emitter_radius ,
        const real_type receiver_distance ,
        const real_type receiver_radius)
        real_type count = 0;
        generator. seed (static\_cast < unsigned > (0));
        for (long long unsigned int i = 0; i < n; i++)
                 if (i \% 100000000 == 0)
                         cout \ll float(i) / float(n) \ll endl;
```

```
const vector_3 p = random_unit_vector();
                vector_3 normal = p;
                vector_3 location = normal;
                location.x *= emitter_radius;
                location.y *= emitter_radius;
                location.z *= emitter_radius;
                std::optional<real_type> i_hit = intersect(
                        location,
                        normal,
                        receiver_distance,
                        receiver_radius);
                if (i_hit)
                        count += *i_hit / (2.0 * receiver_radius);
        }
        return count;
// Beta function, for Schwarzschild gravitation
real_type get_intersecting_line_density(
        const long long unsigned int n,
        const real_type emitter_radius ,
        const real_type receiver_distance,
        const real_type receiver_radius)
        real_type count = 0;
        generator.seed(static\_cast < unsigned > (0));
        for (long long unsigned int i = 0; i < n; i++)
                if (i \% 100000000 == 0)
                        cout << float(i) / float(n) << endl;</pre>
                // Random hemisphere outward
                vector_3 location = random_unit_vector();
                location.x *= emitter_radius;
                location.y *= emitter_radius;
                location.z *= emitter_radius;
                vector_3 surface_normal = location;
                surface_normal.normalize();
                vector_3 normal =
                        random_cosine_weighted_hemisphere(
                                 surface_normal);
                std::optional<real_type> i_hit = intersect(
                         location, normal,
                         receiver_distance, receiver_radius);
```

Experimentation with the receiver size is necessary to understand the intricacies of the code. For instance, where  $r_r = r_e \times 0.01$ , it can be found that gravitation is repulsive at close range. Also, where  $r_r = r_e$ , it can be found that gravitation is attractive at close range.

The full code can be found at:

https://github.com/sjhalayka/non-newtonian\_falloff

### References

- [1] Halayka. Newtonian gravitation from scratch, for C++ programmers. (2024)
- [2] 't Hooft. Dimensional reduction in quantum gravity. (1993)
- [3] Susskind. The World as a Hologram. (1994)
- [4] Misner et al. Gravitation. (1970)



Figure 1: This figure shows an axis-aligned bounding box and an isotropic emitter, looking from slightly above. An example field line (red) and intersecting line segment (green) are given. The bounding box is filled with these green intersecting line segments. It is the gradient of the density of these line segments that forms the gravitational acceleration.