

# On the quantum decomposition of the planet Mercury's orbit path

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## Abstract

By quantizing the kinematic and gravitational time dilation using various step sizes, one obtains a set of weighted paths. The precession associated with each weighted path combines to provide the same answer as the classical analytical solution.

## 1 Introduction

In a previous paper [1], we introduced a method of numerical simulation for the four Solar System tests of general relativity. There was a catch: one had to quantize the kinematic and gravitational time dilation by casting the relevant floating point variables from double-precision to single-precision. A first, this was taken to be a bug, but after careful consideration, it turns out to be a feature of reality. This paper will demonstrate how to decompose the orbit path of Mercury, to numerically obtain the relativistic orbit precession.

## 2 Time dilation

The kinematic time dilation is:

$$\frac{d\tau}{dt} = \frac{\sqrt{c^2 - ||\vec{v}||^2}}{c} = \sqrt{1 - \frac{||\vec{v}||^2}{c^2}}. \quad (1)$$

The gravitational time dilation in the Schwarzschild solution is:

$$\frac{d\tau}{dt} = \sqrt{1 - \frac{R_s}{r}}, \quad (2)$$

where the Schwarzschild radius is  $R_s = 2GM/c^2$ .

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### 3 Quantization of time dilation

In this paper, we will be quantizing the kinematic and gravitational time dilation by casting them to a lesser-precision floating point number.

The non-exponent bit count  $n$  includes the number of mantissa bits  $m$ , plus one sign bit. We generally used  $n = 100$ , except for the kinematic and gravitational time dilation, which uses a lesser, various precision (e.g.  $n = 24$ ).

For subnormal numbers such as those used here, the smallest step size that can be represented is  $\epsilon = 2 \times 2^{-b}$ , where  $b$  is the largest exponent value (e.g.  $2^7 - 1 = 127$  in single-precision floating point numbers,  $2^{10} - 1 = 1023$  for doubles). For instance, we use 1023 where  $n = 100$ , and 127 otherwise (e.g. where  $n = 24$ ).

### 4 Steps in spacetime

Where  $\ell_s$  denotes the Sun's location at the origin,  $\ell_o$  denotes the orbiter Mercury's location, and  $\vec{d}$  denotes the direction vector that points from the orbiter toward the Sun:

$$\vec{d} = \ell_s - \ell_o, \quad (3)$$

$$\hat{d} = \frac{\vec{d}}{||\vec{d}||}, \quad (4)$$

the Newtonian acceleration vector is:

$$\vec{g}_n = \frac{\hat{d}GM}{||\vec{d}||^2}. \quad (5)$$

One parameter is closely related to the kinematic time dilation:

$$\alpha = 2 - \sqrt{1 - \frac{||\vec{v}_o||^2}{c^2}}. \quad (6)$$

Another parameter is the gravitational time dilation:

$$\beta = \sqrt{1 - \frac{R_s}{||\vec{d}||}}. \quad (7)$$

Finally, the semi-implicit Euler integration for velocity and then location is:

$$\vec{v}_o(t + \delta_t) = \vec{v}_o(t) + \delta_t \alpha \vec{g}_n, \quad (8)$$

$$\ell_o(t + \delta_t) = \ell_o(t) + \delta_t \beta \vec{v}_o(t + \delta_t). \quad (9)$$

Note that Newtonian gravity is the result where  $\alpha = \beta = 1$ .

### 5 Classical analytical calculation of Mercury's orbit precession

The classical orbit precession is:

$$\delta_p = \frac{6\pi GM}{c^2(1 - e^2)a} \left( \frac{1}{\pi \times 180 \times 3600} \right) \left( \frac{365}{88} \times 100 \right) = 42.937 \quad (10)$$

where  $e = 0.2056$  is the eccentricity and  $a = 5.7909 \times 10^{10}$  is the semi-major axis.

## 6 Quantum path decomposition

There is a pattern.

We use an initial location that is  $6.9817079 \times 10^{10}$  metres from the Sun (e.g. the aphelion).

Where initial speed is 25000 metres per second, and the analytical solution is 103.7:

Bits $n$	Angle $\delta_p$
20	17..04
21	17.04
22	17.04
23	47.8
24	38.95
25	34.8
26	34.96
27	34.9
28	35.07
29	35.08
30	35.06

If you add bit counts 22, 23, and 24 together (e.g.  $17.04 + 47.8 + 38.95$ ) you get 103.79 arcseconds per Earth century. All of the other bit counts have a weight of zero.

Where initial speed is 20000 metres per second, and the analytical solution is 162.09:

Bits $n$	Angle $\delta_p$
21	27.86
22	76.62
23	52.9

If you add bit counts 21, 22, and 23 together, you get 157.38.

Where initial speed is 30000 metres per second, and the analytical solution is 72.04:

Bits $n$	Angle $\delta_p$
23	46.45
24	27.8

If you add bit counts 23 and 24 together, you get 74.25.

Where initial speed is 38858.47 metres per second (e.g. the actual speed at aphelion), and the analytical solution is 42.9:

Bits $n$	Angle $\delta_p$
24	46.8

Where initial speed is 42500 metres per second, and the analytical solution is 35.8:

Bits $n$	Angle $\delta_p$
26	51.7

Obviously, this solution's weight is less than 1 (e.g.  $(35.8/51.7) < 1$ ).

## References

- [1] Halayka. On simulating the four Solar System tests of general relativity using two-parameter post-Newtonian gravitation with Euler integration. (2024)

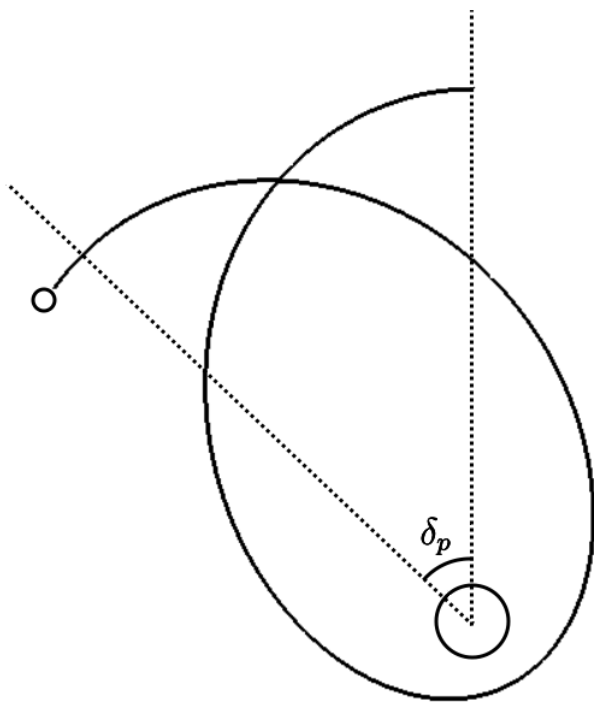


Figure 1: A diagram showing precession, where the orbit does not quite form a closed ellipse.