

On the quantum decomposition of the planet Mercury's orbit path

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Monday 3rd June, 2024 10:49

Abstract

By quantizing the gravitational time dilation using various step sizes, one obtains a set of weighted paths. The precession associated with each weighted path combines to provide the same answer as the classical analytical solution.

1 Time dilation

The kinematic time dilation is:

$$\frac{d\tau}{dt} = \frac{\sqrt{c^2 - ||\vec{v}||^2}}{c} = \sqrt{1 - \frac{||\vec{v}||^2}{c^2}}. \quad (1)$$

The gravitational time dilation is:

$$\frac{d\tau}{dt} = \sqrt{1 - \frac{R_s}{r}}. \quad (2)$$

In this paper we will be quantizing the kinematic and gravitational time dilation by casting them to a smaller floating point number. The quantized step size (e.g. epsilon) in general is $\epsilon = 2^{-m}$ where m is the number of mantissa bits in the floating point number.

2 Steps in spacetime

Where ℓ_s denotes the Sun's location at the origin, ℓ_o denotes the orbiter's location, and \vec{d} denotes the direction vector that points from the orbiter toward the Sun:

$$\vec{d} = \ell_s - \ell_o, \quad (3)$$

$$\hat{d} = \frac{\vec{d}}{||\vec{d}||}, \quad (4)$$

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the Newtonian acceleration vector is:

$$\vec{g}_n = \frac{\hat{d}GM}{||\vec{d}||^2}. \quad (5)$$

One parameter is closely related to the kinematic time dilation:

$$\alpha = 2 - \sqrt{1 - \frac{||\vec{v}_o||^2}{c^2}}. \quad (6)$$

Another parameter is the gravitational time dilation:

$$\beta = \sqrt{1 - \frac{R_s}{||\vec{d}||}}. \quad (7)$$

Finally, the semi-implicit Euler integration for velocity and then location is:

$$\vec{v}_o(t + \delta_t) = \vec{v}_o(t) + \delta_t \alpha \vec{g}_n, \quad (8)$$

$$\ell_o(t + \delta_t) = \ell_o(t) + \delta_t \beta \vec{v}_o(t + \delta_t). \quad (9)$$

Note that Newtonian gravity is the result where $\alpha = \beta = 1$.

3 Precession

$$\delta_p = \frac{6\pi GM}{c^2(1 - e^2)a} \left(\frac{1}{\pi \times 180 \times 3600} \right) \left(\frac{365}{88} \times 100 \right) = 42.937 \quad (10)$$

Where initial speed is 25000 metres per second, and the analytical solution is 103.7:

| Bits | Angle |
|------|--------|
| 20 | 17..04 |
| 21 | 17.04 |
| 22 | 17.04 |
| 23 | 47.8 |
| 24 | 38.95 |
| 25 | 34.8 |
| 26 | 34.96 |
| 27 | 34.9 |
| 28 | 35.07 |
| 29 | 35.08 |
| 30 | 35.06 |

If you add bit counts 22, 23, and 24 together (e.g. $17.04 + 47.8 + 38.95$) you get 103.79 arcseconds per Earth century. All of the other bit counts have a weight of zero.

Where initial speed is 20000 metres per second, and the analytical solution is 162.09:

| Bits | Angle |
|------|-------|
| 21 | 27.86 |
| 22 | 76.62 |
| 23 | 52.9 |

If you add bit counts 21, 22, and 23 together, you get 157.38.

Where initial speed is 30000 metres per second, and the analytical solution is 72.04:

| Bits | Angle |
|------|-------|
| 23 | 46.45 |
| 24 | 27.8 |

If you add bit counts 23 and 24 together, you get 74.25.

Where initial speed is 38858.47 metres per second, and the analytical solution is 42.9:

| Bits | Angle |
|------|-------|
| 24 | 46.8 |

The numerical solution is 46.8.

Where initial speed is 42500 metres per second, and the analytical solution is 35.8:

| Bits | Angle |
|------|-------|
| 26 | 51.7 |

The numerical solution is 51.7. Obviously, this solution's weight is less than 1 (e.g. $(35.8/51.7) < 1$).

References

- [1] Halayka. On simulating the four Solar System tests of general relativity using two-parameter post-Newtonian gravitation with Euler integration. (2024)

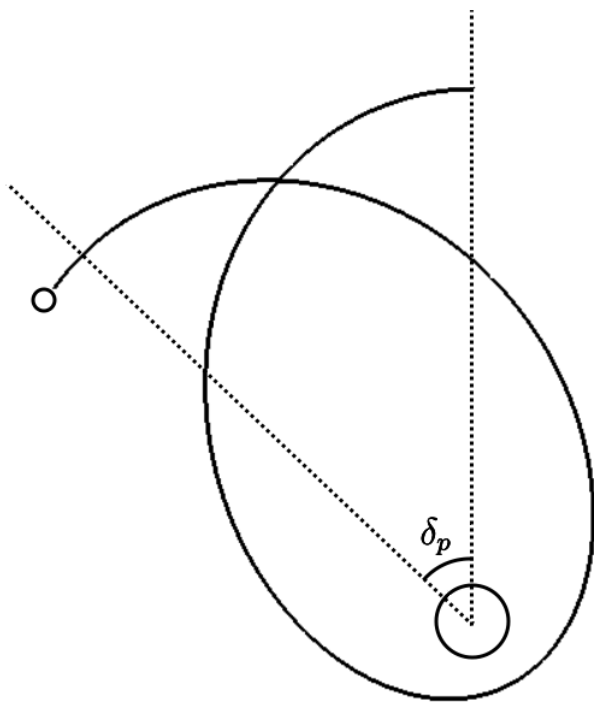


Figure 1: A diagram showing precession, where the orbit does not quite form a closed ellipse.