

# Computing the least commitment action models from observations of plan executions

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## Abstract

## 1 Introduction

## 2 Background

This section formalizes the models for *classical planning* and for the *observation* of the execution of a classical plan.

### 2.1 Classical planning with conditional effects

$F$  is the set of *fluents* or *state variables* (propositional variables). A *literal*  $l$  is a valuation of a fluent  $f \in F$ , i.e. either  $l = f$  or  $l = \neg f$ .  $L$  is a set of literals that represents a partial assignment of values to fluents, and  $\mathcal{L}(F)$  is the set of all literals sets on  $F$ , i.e. all partial assignments of values to fluents. A *state*  $s$  is a full assignment of values to fluents. We explicitly include negative literals  $\neg f$  in states and so  $|s| = |F|$  and the size of the state space is  $2^{|F|}$ .

A *planning frame* is a tuple  $\Phi = \langle F, A \rangle$ , where  $F$  is a set of fluents and  $A$  is a set of *actions*. An action  $a \in A$  is defined with *preconditions*,  $\text{pre}(a) \in \mathcal{L}(F)$ , *positive effects*,  $\text{eff}^+(a) \in \mathcal{L}(F)$ , and *negative effects*  $\text{eff}^-(a) \in \mathcal{L}(F)$ . The semantics of actions  $a \in A$  is specified with two functions:  $\rho(s, a)$  denotes whether action  $a$  is *applicable* in a state  $s$  and  $\theta(s, a)$  denotes the *successor state* that results of applying action  $a$  in a state  $s$ . Then,  $\rho(s, a)$  holds iff  $\text{pre}(a) \subseteq s$ . And the result of applying  $a$  in  $s$  is  $\theta(s, a) = \{s \setminus \text{eff}^-(a)\} \cup \text{eff}^+(a)$ .

A *planning problem* is defined as a tuple  $P = \langle F, A, I, G \rangle$ , where  $I$  is the initial state in which all the fluents of  $F$  are assigned a value true/false and  $G$  is the goal set. A *plan*  $\pi$  for  $P$  is an action sequence  $\pi = \langle a_1, \dots, a_n \rangle$ , and  $|\pi| = n$  denotes its *plan length*. The execution of  $\pi$  in the initial state  $I$  of  $P$  induces a *trajectory*  $\tau(\pi, P) = \langle s_0, a_1, s_1, \dots, a_n, s_n \rangle$  such that  $s_0 = I$  and, for each  $1 \leq i \leq n$ , it holds  $\rho(s_{i-1}, a_i)$  and  $s_i = \theta(s_{i-1}, a_i)$ . A trajectory  $\tau(\pi, P)$  that solves  $P$  is one in which  $G \subseteq s_n$ .

An action  $a_c \in A$  with conditional effects is defined as a set of preconditions  $\text{pre}(a_c) \in \mathcal{L}(F)$  and a set of *conditional effects*  $\text{cond}(a_c)$ . Each conditional effect  $C \triangleright E \in \text{cond}(a_c)$  is composed of two sets of literals:  $C \in \mathcal{L}(F)$ , the *condition*, and  $E \in \mathcal{L}(F)$ , the *effect*. An action  $a_c$  is applicable in a

state  $s$  if  $\rho(s, a_c)$  is true, and the *triggered effects* resulting from the action application are the effects whose conditions hold in  $s$ :

$$\text{triggered}(s, a_c) = \bigcup_{C \triangleright E \in \text{cond}(a_c), C \subseteq s} E,$$

The result of applying action  $a_c$  in state  $s$  is  $\theta(s, a_c) = \{s \setminus \text{eff}_c^-(s, a) \cup \text{eff}_c^+(s, a)\}$ , where  $\text{eff}_c^-(s, a) \subseteq \text{triggered}(s, a)$  and  $\text{eff}_c^+(s, a) \subseteq \text{triggered}(s, a)$  are, respectively, the triggered *negative* and *positive* effects.

### 2.2 The observation model

Given a planning problem  $P = \langle F, A, I, G \rangle$ , a plan  $\pi$  and a trajectory  $\tau(\pi, P)$ , we define the *observation of the trajectory* as an interleaved combination of actions and states that represents the observation from the execution of  $\pi$  in  $P$ . Formally,  $\mathcal{O}(\tau) = \langle s_0^o, a_1^o, s_1^o, \dots, a_l^o, s_m^o \rangle$ ,  $s_0^o = I$ , and:

- The **observed actions** are consistent with  $\pi$ , which means that  $\langle a_1^o, \dots, a_l^o \rangle$  is a sub-sequence of  $\pi$ . Specifically, the number of observed actions,  $l$ , can range from 0 (fully unobservable action sequence) to  $|\pi|$  (fully observable action sequence).
- The **observed states**  $\langle s_0^o, s_1^o, \dots, s_m^o \rangle$  is a sequence of possibly *partially observable states*, except for the initial state  $s_0^o$ , which is fully observable. A partially observable state  $s_i^o$  is one in which  $|s_i^o| < |F|$ ; i.e., a state in which at least a fluent of  $F$  is not observable. Note that this definition also comprises the case  $|s_i^o| = 0$ , when the state is fully unobservable. Whatever the sequence of observed states of  $\mathcal{O}(\tau)$  is, it must be consistent with the sequence of states of  $\tau(\pi, P)$ , meaning that  $\forall i, s_i^o \subseteq s_i$ . In practice, the number of observed states,  $m$ , range from 1 (the initial state, at least), to  $|\pi| + 1$ , and the observed intermediate states will comprise a number of fluents between  $[1, |F|]$ .

We assume a bijective monotone mapping between actions/states of trajectories and observations [Ramírez and Geffner, 2009], thus also granting the inverse consistency relationship (the trajectory is a superset of the observation). Therefore, transiting between two consecutive observed states in  $\mathcal{O}(\tau)$  may require the execution of more than a single action ( $\theta(s_i^o, \langle a_1, \dots, a_k \rangle) = s_{i+1}^o$ , where  $k \geq 1$  is unknown but finite. In other words, having  $\mathcal{O}(\tau)$  does not imply knowing the actual length of  $\pi$ .

## 2.3 Conformant planning

## 3 Learning the least commitment action models from observations

### 3.1 The learning task

### 3.2 The hypothesis space

STRIPS action schemata provide a compact representation for specifying classical planning models. A STRIPS *action schema*  $\xi$  is defined by four lists: A list of *parameters*  $\text{pars}(\xi)$ , and three list of predicates (namely  $\text{pre}(\xi)$ ,  $\text{del}(\xi)$  and  $\text{add}(\xi)$ ) that shape the kind of fluents that can appear in the *preconditions*, *negative effects* and *positive effects* of the actions induced from that schema.

#### Definition 1 (Comparable STRIPS action schemata)

Two STRIPS schemata  $\xi$  and  $\xi'$  are **comparable** iff  $\text{pars}(\xi) = \text{pars}(\xi')$ , i.e. both share the same list of parameters.<sup>1</sup>

For instance, the `stack(?v1,?v2)` and `unstack(?v1,?v2)` schemata from a four operator *blocksworld* [Slaney and Thiébaux, 2001] are *comparable* while `stack(?v1,?v2)` and `pickup(?v1)` are not. Last but not least, we say that two STRIPS models  $\mathcal{M}$  and  $\mathcal{M}'$  are *comparable* iff there exists a bijective function  $\mathcal{M} \mapsto \mathcal{M}'$  that maps every action schema  $\xi \in \mathcal{M}$  to a comparable schemata  $\xi' \in \mathcal{M}'$  and vice versa.

Let be  $\Psi$  the set of *predicates* that shape the propositional state variables  $F$ , and a list of *parameters*  $\text{pars}(\xi)$ . The set of elements that can appear in  $\text{pre}(\xi)$ ,  $\text{del}(\xi)$  and  $\text{add}(\xi)$  of the STRIPS action schema  $\xi$  is given by FOL interpretations of  $\Psi$  over the parameters  $\text{pars}(\xi)$ . We denote this set of FOL interpretations as  $\mathcal{I}_{\Psi,\xi}$ .

Despite any element of  $\mathcal{I}_{\Psi,\xi}$  can *a priori* appear in the  $\text{pre}(\xi)$ ,  $\text{del}(\xi)$  and  $\text{add}(\xi)$  of schema  $\xi$ , the space of possible STRIPS schemata is constrained by a set  $\mathcal{C}$  that includes:

- *Syntactic constraints.* STRIPS constraints require  $\text{del}(\xi) \subseteq \text{pre}(\xi)$ ,  $\text{del}(\xi) \cap \text{add}(\xi) = \emptyset$  and  $\text{pre}(\xi) \cap \text{add}(\xi) = \emptyset$ . Considering exclusively these syntactic constraints, the size of the space of possible STRIPS schemata is given by  $2^{2 \times |\mathcal{I}_{\Psi,\xi}|}$ .
- *Domain-specific constraints.* One can introduce domain-specific knowledge to constrain further the space of possible schemata. For instance, in a *blocksworld* one can claim that `on( $v_1, v_1$ )` and `on( $v_2, v_2$ )` will not appear in any of these lists because of the semantic of the `on` predicate that codes which block is in top of other block.

#### Definition 2 (Well-defined STRIPS action schemata)

Given a set of predicates  $\Psi$ , a list of action parameters  $\text{pars}(\xi)$ , and set of FOL constraints  $\mathcal{C}$ ,  $\xi$  is a **well-defined STRIPS action schema** iff its three lists  $\text{pre}(\xi) \subseteq \mathcal{I}_{\Psi,\xi}$ ,  $\text{del}(\xi) \subseteq \mathcal{I}_{\Psi,\xi}$  and  $\text{add}(\xi) \subseteq \mathcal{I}_{\Psi,\xi}$  only contain elements in  $\mathcal{I}_{\Psi,\xi}$  and they satisfy all the constraints in  $\mathcal{C}$ .

<sup>1</sup>In STRIPS models,  $\text{pars}(\xi) = \text{pars}(\xi')$  implies the number of parameters must be the same. For other planning models that allow object typing, the equality implies that parameters share the same type

```
(:action editable_inc-x
:parameters (?v1 ?v2)
:precondition
  (and (or (not (pre_xcoord_v1_inc-x)) (xcoord ?v1))
        (or (not (pre_xcoord_v2_inc-x)) (xcoord ?v2))
        (or (not (pre_ycoord_v1_inc-x)) (xcoord ?v1))
        (or (not (pre_ycoord_v2_inc-x)) (xcoord ?v2))
        (or (not (pre_q0_inc-x)) (q0))
        (or (not (pre_q1_inc-x)) (q1)))
        (or (not (pre_next_v1_v1_inc-x)) (next ?v1 ?v1)))
        (or (not (pre_next_v1_v2_inc-x)) (next ?v1 ?v2)))
        (or (not (pre_next_v2_v1_inc-x)) (next ?v2 ?v1)))
        (or (not (pre_next_v2_v2_inc-x)) (next ?v2 ?v2))))
:effect (and
  (when (del_xcoord_v1_inc-x) (not (xcoord ?v1)))
  (when (del_xcoord_v2_inc-x) (not (xcoord ?v2)))
  (when (del_ycoord_v1_inc-x) (not (xcoord ?v1)))
  (when (del_ycoord_v2_inc-x) (not (xcoord ?v2)))
  (when (del_q0_inc-x) (not (q0)))
  (when (del_q1_inc-x) (not (q1)))
  (when (del_next_v1_v1_inc-x) (not (next ?v1 ?v1)))
  (when (del_next_v1_v2_inc-x) (not (next ?v1 ?v2)))
  (when (del_next_v2_v1_inc-x) (not (next ?v2 ?v1)))
  (when (del_next_v2_v2_inc-x) (not (next ?v2 ?v2)))

  (when (add_xcoord_v1_inc-x) (xcoord ?v1))
  (when (add_xcoord_v2_inc-x) (xcoord ?v2))
  (when (add_ycoord_v1_inc-x) (xcoord ?v1))
  (when (add_ycoord_v2_inc-x) (xcoord ?v2))
  (when (add_q0_inc-x) (q0))
  (when (add_q1_inc-x) (q1))
  (when (add_next_v1_v1_inc-x) (next ?v1 ?v1))
  (when (add_next_v1_v2_inc-x) (next ?v1 ?v2))
  (when (add_next_v2_v1_inc-x) (next ?v2 ?v1))
  (when (add_next_v2_v2_inc-x) (next ?v2 ?v2)))
```

Figure 1: Editable version of the `inc-x(?v1,?v2)` schema for robot navigation in a  $n \times n$  grid.

We say a planning model  $\mathcal{M}$  is *well-defined* if all its STRIPS action schemata are *well-defined*.

### 3.3 A propositional encoding for STRIPS action schema

Given a STRIPS action schema  $\xi$ , a propositional encoding for the *preconditions*, *negative* and *positive* effects of that schema can be represented with fluents of the kind  $[\text{pre}|\text{del}|\text{add}]_e.\xi$  such that  $e \in \mathcal{I}_{\Psi,\xi}$  is a single element from the set of interpretations of predicates  $\Psi$  over the corresponding variable names  $\Omega_\xi$ . Figure ?? shows the propositional encoding for the six action schema defined in Figure ??.

The interest of having a propositional encoding for STRIPS action schema is that, using *conditional effects*, it allows to compactly define *editable actions*. Actions whose semantics is given by the value of the  $[\text{pre}|\text{del}|\text{add}]_e.\xi$  fluents at the current state. Given an operator schema  $\xi \in \mathcal{M}$  its *editable* version is formalized as:

$$\begin{aligned} \text{pre}(\text{editable}_\xi) &= \{\text{pre}_e.\xi \implies e\}_{\forall e \in \mathcal{I}_{\Psi,\xi}} \\ \text{cond}(\text{editable}_\xi) &= \{\text{del}_e.\xi\} \triangleright \{\neg e\}_{\forall e \in \mathcal{I}_{\Psi,\xi}}, \\ &\quad \{\text{add}_e.\xi\} \triangleright \{e\}_{\forall e \in \mathcal{I}_{\Psi,\xi}}. \end{aligned}$$

Figure 1 shows the PDDL encoding of the *editable inc-x(?v1,?v2)* schema for robot navigation in a  $n \times n$  grid (Figure ??). Note that this editable schema, when the fluents of Figure ?? hold, behaves exactly as defined in Figure ??.

### **3.4 Learning the least commitment models with conformant planning**

## **4 Evaluation**

## **5 Conclusions**

### **References**

- [Ramírez and Geffner, 2009] Miquel Ramírez and Hector Geffner. Plan recognition as planning. In *International Joint conference on Artificial Intelligence, (IJCAI-09)*, pages 1778–1783. AAAI Press, 2009.
- [Slaney and Thiébaux, 2001] John Slaney and Sylvie Thiébaux. Blocks world revisited. *Artificial Intelligence*, 125(1-2):119–153, 2001.