Learning action models from *state-invariants*

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Abstract

This paper addresses the learning of STRIPS action models from *state-invariants* (i.e logic formulae that specify constraints about the possible states of a given domain). The benefit of exploiting *state-invariants* is two-fold, they constrain the space of possible action models and they can complete learning examples that are only partially observed. Our approach for learning STRIPS action from *state-invariants* is a *classical planning* compilation that is flexible to different sources of input knowledge including partial observations of plan executions and *state-invariants*. The experimental results demonstrate that, even at unfavorable scenarios where input observations are minimal (a single learning example that comprises just a full initial state and a partially observed state), *state-invariant* are helpful to learn good quality STRIPS action models.

1 Introduction

The specification of action models is a complex process that limits, too often, the application of *model-based planning* to real-world tasks [Kambhampati, 2007]. The *machine learning* of action models relieves this *knowledge acquisition bottleneck* of *model-based planning* and nowadays, there exists a wide range of effective approaches for learning action models [Arora *et al.*, 2018]. Many of the most successful approaches for learning planning action models are however purely *inductive* [Yang *et al.*, 2007; Pasula *et al.*, 2007; Mourao *et al.*, 2010; Zhuo and Kambhampati, 2013], linking learning performance exclusively to the *amount* and *quality* of the input learning examples (which typically are observation of plan executions).

This paper addresses the learning of action models exploiting a different source of knowledge, *deductive* knowledge. Our approach leverages *state-invariants* (i.e. logic formulae that specify constraints about the possible states of a given domain) to cushion the negative impact of insufficient learning examples. Given an action model, state-of-the-art planners infer *state-invariants* from that model to reduce the search space and make the planning process more efficient [Helmert, 2009]. In this paper we follow the opposite direction and leverage *state-invariants* to learn the planning action model. The benefit of learning action models from *state-invariants* is two-fold, *state-invariants* constrain the space of possible action models and can complete learning examples that are only partially observed.

Our approach for learning STRIPS action models from *state-invariants* is to compile the learning task into a classical planning task. Our compilation is built on top of the classical planning compilation for the learning of STRIPS action models [Aineto *et al.*, 2018] and it is flexible to different kinds of input knowledge including both partial observations of plan executions and *state-invariants*. The compilation outputs an STRIPS action model that is *consistent* with all the given input knowledge. The experimental results demonstrate that, even at unfavorable scenarios where input observations are minimal (a single learning example that comprises just a full initial state and a partially observed state), *state-invariant* are helpful to learn good quality STRIPS action models.

2 Background

This section formalizes the *planning model* we follow in this work and introduces the classical planning compilation for the learning of STRIPS action models [Aineto *et al.*, 2018]. Finally, the section formalizes *state-invariants*.

2.1 Classical planning with conditional effects

Let F be the set of propositional state variables (*fluents*) describing a state. A *literal* l is a valuation of a fluent $f \in F$; i.e. either $l = f$ or $l = \neg f$. A set of literals L represents a partial assignment of values to fluents (without loss of generality, we will assume that L does not contain conflicting values). Given L, let $\neg L = \{\neg l : l \in L\}$ be its complement. We use $\mathcal{L}(F)$ to denote the set of all literal sets on F; i.e. all partial assignments of values to fluents. A *state* s is a full assignment of values to fluents; $|s| = |F|$.

A *classical planning action* $a \in A$ has: a precondition $\mathsf{pre}(a) \in \mathcal{L}(F)$, a set of effects $\mathsf{eff}(a) \in \mathcal{L}(F)$, and a positive action cost $cost(a)$. The semantics of actions $a \in A$ is specified with two functions: $\rho(s, a)$ denotes whether action a is *applicable* in a state s and $\theta(s, a)$ denotes the *successor state* that results of applying action a in a state s. Then, $\rho(s, a)$ holds iff $\mathsf{pre}(a) \subseteq s$, i.e. if its precondition holds in s. The result of executing an applicable action $a \in A$ in a state s is a new state $\theta(s, a) = (s \setminus \neg\mathsf{eff}(a)) \cup \mathsf{eff}(a)$. Subtracting

the complement of $\mathsf{eff}(a)$ from s ensures that $\theta(s, a)$ remains a well-defined state. The subset of action effects that assign a positive value to a state fluent is called *positive effects* and denoted by $\mathsf{eff}^+(a) \in \mathsf{eff}(a)$ while $\mathsf{eff}^-(a) \in \mathsf{eff}(a)$ denotes the *negative effects* of an action $a \in A$.

A *classical planning problem* is a tuple $P = \langle F, A, I, G \rangle$, where I is the initial state and $G \in \mathcal{L}(F)$ is the set of goal conditions over the state variables. A *plan* π is an action sequence $\pi = \langle a_1, \ldots, a_n \rangle$, with $|\pi| = n$ denoting its *plan length* and $cost(\pi) = \sum_{a \in \pi} cost(a)$ its *plan cost*. The execution of π on the initial state of P induces a *trajectory* $\tau(\pi, P) = \langle s_0, a_1, s_1, \ldots, a_n, s_n \rangle$ such that $s_0 = I$ and, for each $1 \leq i \leq n$, it holds $\rho(s_{i-1}, a_i)$ and $s_i = \theta(s_{i-1}, a_i)$. A plan π solves P iff the induced *trajectory* $\tau(\pi, P)$ reaches a final state $G \subseteq s_n$, where all goal conditions are met. A solution plan is *optimal* iff its cost is minimal.

We also define *actions with conditional effects* because they are useful to compactly formulate our approach for *goal recognition with unknown domain models*. An action $a_c \in A$ with conditional effects is a set of preconditions $\mathsf{pre}(a_c) \in \mathcal{L}(F)$ and a set of *conditional effects* $\mathsf{cond}(a_c)$. Each conditional effect $C \rhd E \in \mathsf{cond}(a_c)$ is composed of two sets of literals: $C \in \mathcal{L}(F)$, the *condition*, and $E \in \mathcal{L}(F)$, the *effect*. An action a_c is applicable in a state s if $\rho(s, a_c)$ is true, and the result of applying action a_c in state s is $\theta(s, a_c) = \{s \setminus \neg\mathsf{eff}_c(s, a) \cup \mathsf{eff}_c(s, a)\}$ where $\mathsf{eff}_c(s, a)$ are the *triggered effects* resulting from the action application (conditional effects whose conditions hold in s):

$$\mathsf{eff}_c(s, a) = \bigcup_{C \rhd E \in \mathsf{cond}(a_c), C \subseteq s} E,$$

2.2 Learning action models with classical planning

The *classical planning compilation* for the learning STRIPS action models [Aineto *et al.*, 2018] receives as input an empty model $\mathcal{M}$ (which contains just the action headers), and an observation of a set of observations of plan executions. The compilation outputs a model $\mathcal{M}'$ that specifies the preconditions and effects of each action schema included in $\mathcal{M}$ such that the validation of the observations following $\mathcal{M}'$ is successful; i.e., it holds $\rho(s^o_{i-1}, a_i)$ for every observed action and $s^o_i = \theta(s^o_{i-1}, a_i)$ for every observed state.

A solution plan to the classical planning problem that results from the compialtion is a sequence of: (a) *insert actions*, that insert preconditions and effects on a schemata of $\mathcal{M}$ to build $\mathcal{M}'$ and (b) *apply actions* that validate the application of the $\mathcal{M}'$ model in the input observations. Figure 1 shows a solution to a classical planning problem resulting from the Aineto *et al.* 2018 compilation corresponding to the *blocksworld* [Slaney and Thiébaux, 2001]. In the initial state of that problem the robot hand is empty and three blocks (namely `blockA`, `blockB` and `blockC`) are clear and on top of the table. The problem goal is having the three-block tower `blockA` on top of `blockB` and `blockB` on top of `blockC`. The plan shows the *insert* actions for the `stack` scheme (steps $00-01$ insert the preconditions, steps $05-10$ insert the effects), the plan steps $02-04$ that insert the preconditions of the `pickup` scheme and steps $10-13$ that insert the effects of this scheme. Finally, steps $14-17$ is a plan postfix with actions that apply the programmed model to achieve the goals starting from the given initial state.

```
00: (insert_pre_stack_holding_v1)
01: (insert_pre_stack_clear_v2)
02: (insert_pre_pickup_handempty)
03: (insert_pre_pickup_clear_v1)
04: (insert_pre_pickup_ontable_v1)
05: (insert_eff_stack_clear_v1)
06: (insert_eff_stack_clear_v2)
07: (insert_eff_stack_handempty)
08: (insert_eff_stack_holding_v1)
09: (insert_eff_stack_on_v1_v2)
10: (insert_eff_pickup_clear_v1)
11: (insert_eff_pickup_ontable_v1)
12: (insert_eff_pickup_handempty)
13: (insert_eff_pickup_holding_v1)
14: (apply_pickup blockB)
15: (apply_stack blockB blockC)
16: (apply_pickup blockA)
17: (apply_stack blockA blockB)
18: (validate_1)
```

Figure 1: Example of a solution to a problem output by the classical planning compilation for the learning STRIPS action models.

2.3 State-invariants

The notion of *state-constraint* is very general and has been used in different areas of AI and for different purposes. If we restrict ourselves to planning, *state-constraints* are abstractions for compactly specifying sets of states. For example, *state-constraints* in planning allow to specify the set of states where a given action is applicable, the set of states where a given *derived predicate* holds or the set of states that are considered goal states.

State-invariants is a kind of state-constraints useful for computing more compact state representations [Helmert, 2009] or making *satisfiability planning* and *backward search* more efficient [Rintanen, 2014; Alcázar and Torralba, 2015]. Given a classical planning problem $P = \langle F, A, I, G \rangle$, a *state-invariant* is a formula ϕ that holds at the initial state of a given classical planning problem, $I \models \phi$, and at every state s, built from F, that is reachable from I by applying actions in A. For instance, Figure 2 shows five clauses that define *state-invariants* for the *blocksworld* planning domain.

$\forall x_1, x_2\ ontable(x_1) \leftrightarrow \neg on(x_1, x_2)$.
$\forall x_1, x_2\ clear(x_1) \leftrightarrow \neg on(x_2, x_1)$.
$\forall x_1, x_2, x_3\ \neg on(x_1, x_2) \vee \neg on(x_1, x_3)\ such\ that\ x_2 \neq x_3$.
$\forall x_1, x_2, x_3\ \neg on(x_2, x_1) \vee \neg on(x_3, x_1)\ such\ that\ x_2 \neq x_3$.
$\forall x_1, \ldots, x_n\ \neg(on(x_1, x_2) \wedge on(x_2, x_3) \wedge \ldots \wedge on(x_{n-1}, x_n) \wedge on(x_n, x_1))$.

Figure 2: Example of *state-invariants* for the *blocksworld* domain.

A *mutex* (mutually exclusive) is a *state-invariant* that takes the form of a binary clause and indicates a pair of different properties that cannot be simultaneously true [Kautz and Selman, 1999]. For instance in a three-block *blocksworld*, $\neg on(block_A, block_B) \vee \neg on(block_A, block_C)$ is a *mutex* because $block_A$ can only be on top of a single block.

A *domain invariant* is an instance-independent state-invariant, i.e. holds for any possible initial state and any possible set of objects. Therefore, if a given state s holds $s \not\models \phi$ such that ϕ is a *domain invariant*, it means that s is not a valid state. Domain invariants are often compactly defined as *lifted invariants* (also called schematic invariants [Rintanen, 2017]).

3 Learning STRIPS action models from *state-invariants*

First, this section defines the sampling space and the space of possible action models. Then, the section formalizes the task of learning STRIPS action models from *state-invariants*.

3.1 The sampling space

We define a *learning example* as a sequence $\mathcal{O} = \langle s_0^o, s_1^o \ldots, s_m^o \rangle$ of partial states, except for the initial state s_0^o which is fully observed. Intermediate states can be missing meaning that are *unobserved*, so transiting between two consecutive observed states in $\mathcal{O}$ may require the execution of more than a single action ($\theta(s_i^o, \langle a_1, \ldots, a_k \rangle) = s_{i+1}^o$, where $k \geq 1$ is unknown but finite. A partially observed state s_i^o, $1 \leq i \leq m$, is one in which $|s_i^o| < |F|$; i.e., a state in which at least a fluent of F is not observable. Note that this definition also comprises the case $|s_i^o| = 0$, when the state is fully unobservable.

3.2 The space of STRIPS action models

A STRIPS *action schema* ξ is defined by: A list of *parameters* $pars(\xi)$, and three sets of predicates (namely $pre(\xi)$, $del(\xi)$ and $add(\xi)$) that shape the kind of fluents that can appear in the *preconditions*, *negative effects* and *positive effects* of the actions induced from that schema. Let be Ψ the set of *predicates* that shape the propositional state variables F, and a list of *parameters*, $pars(\xi)$. The set of elements that can appear in $pre(\xi)$, $del(\xi)$ and $add(\xi)$ of the STRIPS action schema ξ is the set of FOL interpretations of Ψ over the parameters $pars(\xi)$ and is denoted as $\mathcal{I}_{\Psi,\xi}$.

For instance in a four-operator *blocksworld* [Slaney and Thiébaux, 2001], the $\mathcal{I}_{\Psi,\xi}$ set contains only five elements for the `pickup(`v_1`)` schemata, $\mathcal{I}_{\Psi,pickup}$={`handempty`, `holding(`$v_1$`)`, `clear(`$v_1$`)`, `ontable(`$v_1$`)`, `on(`$v_1, v_1$`)`} while it contains eleven elements for the `stack(`v_1`,`v_2`)` schemata, $\mathcal{I}_{\Psi,stack}$={`handempty`, `holding(`v_1`)`, `holding(`v_2`)`, `clear(`v_1`)`, `clear(`v_2`)`, `ontable(`v_1`)`, `ontable(`v_2`)`, `on(`v_1, v_1`)`, `on(`v_1, v_2`)`, `on(`v_2, v_1`)`, `on(`v_2, v_2`)`}.

Despite any element of $\mathcal{I}_{\Psi,\xi}$ can *a priori* appear in the $pre(\xi)$, $del(\xi)$ and $add(\xi)$ of schema ξ, in practice the actual space of possible STRIPS schemata is bounded by:

1. **Syntactic constraints**. STRIPS constraints require $del(\xi) \subseteq pre(\xi)$, $del(\xi) \cap add(\xi) = \emptyset$ and $pre(\xi) \cap add(\xi) = \emptyset$. Considering exclusively these syntactic constraints, the size of the space of possible STRIPS schemata is given by $2^{2 \times |\mathcal{I}_{\Psi,\xi}|}$. *Typing constraints* are also of this kind [McDermott *et al.*, 1998].
2. **Observation constraints**. The *learning examples*, that are observations of plan executions, depict *semantic knowledge* that constraints further the space of possible action schemata.

In this work we introduce a novel propositional encoding of the *preconditions*, *negative*, and *positive* effects of a STRIPS action schema ξ that uses only fluents of two kinds `pre_e_`ξ and `eff_e_`ξ (where $e \in \mathcal{I}_{\Psi,\xi}$). This encoding exploits the syntactic constraints of STRIPS so it is more compact that the one previously proposed by Aineto *et al.* 2018

```
(:action stack
   :parameters (?v1 ?v2)
   :precondition (and (holding ?v1) (clear ?v2))
   :effect (and (not (holding ?v1)) (not (clear ?v2))
                (clear ?v1) (handempty) (on ?v1 ?v2)))


(pre_holding_v1_stack) (pre_clear_v2_stack)
(eff_holding_v1_stack) (eff_clear_v2_stack)
(eff_clear_v1_stack) (eff_handempty_stack) (eff_on_v1_v2_stack)
```

Figure 3: PDDL encoding of the `stack(?v1,?v2)` schema and our propositional representation for this same schema.

for learning STRIPS action models with classical planning. In more detail, if `pre_e_`ξ holds it means that $e \in \mathcal{I}_{\Psi,\xi}$ is a *precondition* in ξ. If `pre_e_`ξ and `eff_e_`ξ holds it means that $e \in \mathcal{I}_{\Psi,\xi}$ is a *negative effect* in ξ while if pre_e_ξ does not hold but `eff_e_`ξ holds, it means that $e \in \mathcal{I}_{\Psi,\xi}$ is a *positive effect* in ξ. Figure 3 shows the PDDL encoding of the `stack(?v1,?v2)` schema and our propositional representation for this same schema using the `pre_e_stack` and `eff_e_stack` fluents ($e \in \mathcal{I}_{\Psi,stack}$).

One can also introduce *domain-specific knowledge* to constrain further the space of possible schemata. For instance, in the *blocksworld* one can argue that `on(`v_1`,`v_1`)` and `on(`v_2`,`v_2`)` will not appear in the $pre(\xi)$, $del(\xi)$ and $add(\xi)$ lists of an action schema ξ because, in this specific domain, a block cannot be on top of itself. *State-invariants* are *domain-specific knowledge* that can be used to define new *syntactic* and *semantic* constraints over the space of possible action schemata.

3.3 The learning task

We define the task of learning a planning action model from *state-invariants* as a tuple $\Lambda = \langle \mathcal{M}, \mathcal{O}, \Phi \rangle$, where:

- $\mathcal{M}$ is the *initial empty model* that contains only the name, $name(\xi)$, and parameters, $pars(\xi)$, of each action model ξ to be learned.
- $\mathcal{O} = \langle s_0^o, s_1^o \ldots, s_m^o \rangle$ is a single learning example. This example can be reduced to its minimal expression $\mathcal{O}^* = \langle s_0^o, s_m^o \rangle$ comprissing at least two state observations, a full initial state s_0^o and a partially observed state s_m^o. The set of predicates Ψ and objects Ω that shape the set of fluents F is deducible from $\mathcal{O}$ since s_0^o is a fully observed state.
- Φ is a set of *state-invariants* that define constraints about the set of possible states.

A *solution* to a learning task $\Lambda = \langle \mathcal{M}, \mathcal{O}, \Phi \rangle$ is a model $\mathcal{M}'$ that is consistent with the the *initial empty model* $\mathcal{M}$, the learning example $\mathcal{O}$ and the set of *state invariants* in Φ.

4 Learning action models from *state-invariants* with classical planning

This section shows how to exploit our compact encoding of STRIPS action models to solve a $\Lambda = \langle \mathcal{M}, \mathcal{O}, \Phi \rangle$ learning task with an off-the-shelf classical planner.

4.1 Completing partially observed states with *schematic mutex*

Our sampling space follows the *open world* assumption, i.e. what is not observed is considered unknown. Here we describe a pre-processing mechanism to add new knowledge that completes states that are partially observed in a $\Lambda = \langle \mathcal{M}, \mathcal{O}, \Phi \rangle$ learning task using a particular case of *state-invariants* that we call *schematic mutex*. We pay special attention to *schematic mutex* because they identify the *properties* of a given type of objects [Fox and Long, 1998] and because they enable (1) effectively pruning of inconsistent STRIPS action models and (2) effective completion of partially observed states.

We define a *schematic mutex* as a $\langle p, q \rangle$ predicates pair where both $p \in \Psi$ and $q \in \Psi$ are predicates that shape the set of state variables F and such that they satisfy the following formulae $p \rightarrow \neg q$, where the predicate variables are universally quantified. For instance, predicates $holding(v_1)$ and $clear(v_1)$ from the *blocksworld* are *schematic mutex* while predicates $clear(v_1)$ and $ontable(v_1)$ are not because $\forall v_1\ clear(v_1) \leftrightarrow \neg ontable(v_1)$ does not hold for every possible *blocksworld* state.

Given a *schematic mutex* $\langle p, q \rangle$ and a state observation $s^o_j \in \mathcal{O}$, $(1 \leq j \leq m)$, such that $p(\omega) \in s^o_j$ is a literal built instantiating predicate p with some subset of objects $\omega \subseteq \Omega^{|pars(p)|}$ then, the state observation s^o_j can be safely completed adding the new literal $\neg q(\omega)$ (despite $\neg q(\omega)$ was actually unobserved). For instance, if the literal `holding(blockA)` is observed in a particular blocksword state and we know the *schematic mutex* $\forall x\ holding(x) \rightarrow \neg clear(x)$ we can safely extend that state observation with literal `¬clear(blockA)` (despite this literal was actually unobserved).

4.2 Pruning inconsistent action models with *schematic mutex*

Our approach to implement this pruning is adding new conditional effects to the classical planning compilation for the learning of STRIPS action models [Aineto *et al.*, 2018] that capture when the programmed model is inconsistent with a *schematic mutex* in Φ. Given a $\Lambda = \langle \mathcal{M}, \mathcal{O}, \Phi \rangle$ learning task we build and solve a classical planning problem $P_\Lambda = \langle F_\Lambda, A_\Lambda, I, G_\Lambda \rangle$ that extends the original compilation as follows:

- F_Λ extends F with a fluent $mode_{inval}$, to indicate whether an action model is *inconsistent* with the input *state-invariants* Φ. Like the original compilation we define a fluent $mode_{insert}$, to indicate whether action models are being programmed, and the fluents for the propositional encoding of the corresponding space of STRIPS action models. As explained, this is a set of fluents of the type $\{pre\_e\_\xi, eff\_e\_\xi\}_{\forall e \in \mathcal{I}_{\Psi,\xi}}$.
- $G_\Lambda = G \cup \{\neg mode_{inval}\}$ extends the original goals G with the $\neg mode_{inval}$ literal to validate that only states *consistent* with the state constraints Φ are traversed by P_Λ solutions.
- A_Λ contains actions of two kinds, like in the original compilation:

1. Actions for *inserting* a *precondition*, *positive/negative* effect in ξ following the syntactic constraints of STRIPS models.
   - A precondition p is inserted in ξ when neither pre_p, eff_p exist in ξ. In addition, a conditional effect is added now for every *schematic mutex* $\langle p, q \rangle$ s.t. both p and q belong to $\in \mathcal{I}_{\Psi,\xi}$ to ban the insertion of two preconditions that are *schematic mutex*.

$$\begin{aligned} \mathsf{pre}(\mathsf{insertPre}_{\mathsf{p},\xi}) =& \{\neg pre\_p\_\xi, \neg eff\_p\_\xi, \\ & mode_{insert}, \neg mode_{inval}\}, \\ \mathsf{cond}(\mathsf{insertPre}_{\mathsf{p},\xi}) =& \{\emptyset\} \rhd \{pre\_p\_\xi\}, \\ & \{pre\_q\_\xi\} \rhd \{mode_{inval}\}. \end{aligned}$$

   - Actions which support the addition of a *negative/positive* effect $p \in \mathcal{I}_{\Psi,\xi}$ to the action model ξ are extended with two conditional effects, for every *schematic mutex* $\langle p, q \rangle$ s.t. both p and q belong to $\in \mathcal{I}_{\Psi,\xi}$, to ban the insertion of two positive/negative effects that are *schematic mutex*:

$$\begin{aligned} \mathsf{pre}(\mathsf{insertEff}_{\mathsf{p},\xi}) &= \{\neg eff\_p\_\xi, mode_{insert}, \neg mode_{inval}\}, \\ \mathsf{cond}(\mathsf{insertEff}_{\mathsf{p},\xi}) &= \{\emptyset\} \rhd \{eff\_p\_\xi\}, \\ & \{pre\_q\_\xi, eff\_q\_\xi, pre\_p\_\xi\} \rhd \{mode_{inval}\}, \\ & \{\neg pre\_q\_\xi, eff\_q\_\xi, \neg pre\_p\_\xi\} \rhd \{mode_{inval}\}. \end{aligned}$$

2. Actions for *applying* an action model ξ built by the *insert* actions and bounded to objects $\omega \subseteq \Omega^{|pars(\xi)|}$. The action parameters, $pars(\xi)$, are bound to the objects in ω that appear in the same position. The definition $\mathsf{apply}_{\xi,\omega}$ actions is more compact than the one previously proposed by Aineto *et al.* 2018 since we are not using disjunctions to code the possible preconditions of an action schema.

$$\begin{aligned} \mathsf{pre}(\mathsf{apply}_{\xi,\omega}) =& \{\neg mode_{inval}\}, \\ \mathsf{cond}(\mathsf{apply}_{\xi,\omega}) =& \{pre\_p\_\xi \wedge eff\_p\_\xi\} \rhd \{\neg p(\omega)\}_{\forall p \in \mathcal{I}_{\Psi,\xi}}, \\ & \{\neg pre\_p\_\xi \wedge eff\_p\_\xi\} \rhd \{p(\omega)\}_{\forall p \in \mathcal{I}_{\Psi,\xi}}\}, \\ & \{pre\_p\_\xi \wedge \neg p(\omega)\} \rhd \{mode_{inval}\}_{\forall p \in \mathcal{I}_{\Psi,\xi}}, \\ & \{\emptyset\} \rhd \{\neg mode_{insert}\}, \end{aligned}$$

For every *state-invariant* $\phi \in \Phi$ we can extend $\mathsf{apply}_{\xi,\omega}$ actions with a conditional effect $\{\neg\phi\} \rhd \{mode_{inval}\}$ that checks the consistency of the *state-invariant* ϕ at every state traversed by a solution to the P_Λ problem. Cheking arbitrary ϕ formulae can be too expensive for current classical planners. Instead, we prefer to add these conditional effects into $\mathsf{apply}_{\xi,\omega}$ actions for checking the consistency of a *schematic mutex* $\langle p, q \rangle$ s.t. both p and q belong to $\in \mathcal{I}_{\Psi,\xi}$.

$$\{pre\_p\_\xi \wedge q(\omega)\} \rhd \{mode_{inval}\}_{\forall p \in \mathcal{I}_{\Psi,\xi}},$$

4.3 The bias of the initially *empty* action model

Classical planners tend to preffer shorter solution plans, so our compilation may introduce a bias to $\Lambda = \langle \mathcal{M}, \mathcal{O}, \Phi \rangle$ learning tasks preferring solutions that are referred to action models with a shorter number of *preconditions/effects*. In more detail, all $\{pre\_e\_\xi, eff\_e\_\xi\}_{\forall e \in \mathcal{I}_{\Psi,\xi}}$ fluents are false at the initial state of our P_Λ compilation so classical planners tend to solve P_Λ with plans that require a shorter number of *insert* actions.

This bias could be eliminated defining a cost function for the actions in P_Λ (e.g. *insert* actions have *zero cost* while $\mathsf{apply}_{\xi,\omega}$ actions have a *positive constant cost*). In practice we use a different approach to disregard the cost of *insert* actions because classical planners are not proficiency optimizing *plan cost* when there are zero-cost actions. Instead, our approach is to use a SAT-based planner [Rintanen, 2014] that can apply all actions for inserting preconditions in a single planning step (these actions do not interact). Further, the actions for inserting action effects are also applied in another single planning step. The plan horizon for programming any action model is then always bound to 2, which significantly reduces the planning horizon. The SAT-based planning approach is also convenient because its ability to deal with classical planning problems populated with dead-ends and because symmetries in the insertion of preconditions/effects into an action model do not affect to the planning performance.

4.4 Compilation properties

Lemma 1. *Soundness. Any classical plan π_Λ that solves P_Λ produces a* STRIPS *model $\mathcal{M}'$ that solves the $\Lambda = \langle \mathcal{M}, \mathcal{O}, \Phi \rangle$ learning task.*

Proof. According to the P_Λ compilation, once a given precondition or effect is inserted into the action model $\mathcal{M}$ it cannot be removed back. In addition, once the action model $\mathcal{M}$ is applied it cannot be *programmed*. In the compiled planning problem P_Λ, only $\mathsf{apply}_{\xi,\omega}$ actions can update the value of the state fluents F. This means that a state consistent with an observation s^o_n can only be achieved executing an applicable sequence of $\mathsf{apply}_{\xi,\omega}$ actions that, starting in the corresponding initial state s^o_0, validates that every generated intermediate state s_i, s.t. $0 \leq i \leq n$, is consistent with the input state observations and *state-invariants*. This is exactly the definition of the solution condition for an action model $\mathcal{M}'$ to solve the $\Lambda = \langle \mathcal{M}, \mathcal{O}, \Phi \rangle$ learning task. □

Lemma 2. *Completeness. Any* STRIPS *model $\mathcal{M}'$ that solves the $\Lambda = \langle \mathcal{M}, \mathcal{O}, \Phi \rangle$ learning task can be computed with a classical plan π_Λ that solves P_Λ.*

Proof. By definition $\mathcal{I}_{\Psi,\xi}$ fully captures the set of elements that can appear in a STRIPS action schema ξ using predicates Ψ. In addition the P_Λ compilation does not discard any possible action model $\mathcal{M}'$ definable within $\mathcal{I}_{\Psi,\xi}$ that satisfies the domain mutex in Φ. This means that, for every STRIPS model $\mathcal{M}'$ that solves the $\Lambda = \langle \mathcal{M}, \mathcal{O}, \Phi \rangle$, we can build a plan π_Λ that solves P_Λ by selecting the appropriate $\mathsf{insertPre}_{\mathsf{p},\xi}$ and $\mathsf{insertEff}_{\mathsf{p},\xi}$ actions for *programming* the precondition and effects of the corresponding action model $\mathcal{M}'$ and then, selecting the corresponding $\mathsf{apply}_{\xi,\omega}$ actions that transform the initial state observation s^o_0 into the final state observation s^o_m. □

The size of the classical planning task P_Λ output by our compilation depends on the arity of the given *predicates* Ψ, that shape the propositional state variables F, and the number of parameters of the action models, $|pars(\xi)|$. The larger these arities, the larger $|\mathcal{I}_{\Psi,\xi}|$. The size of the $\mathcal{I}_{\Psi,\xi}$ set is the term that dominates the compilation size because it defines the pre_e_ξ/eff_e_ξ fluents, the corresponding set of *insert* actions, and the number of conditional effects in the $\mathsf{apply}_{\xi,\omega}$ actions. Note that *typing* can be used straightforward to constrain the FOL interpretations of Ψ over the parameters $pars(\xi)$ which significantly reduces $|\mathcal{I}_{\Psi,\xi}|$ and hence, the size of the classical planning task output by the compilation.

5 Evaluation

This section evaluates the performance of our approach for learning STRIPS action models with different amounts of available input knowledge.

Reproducibility

The domains used in the evaluation are IPC domains that satisfy the STRIPS requirement [Fox and Long, 2003], taken from the PLANNING.DOMAINS repository [Muise, 2016]. We only used 1 learning examples for each learning task and we fixed the examples for all the experiments so that we can evaluate the impact of the different amount and source of the input knowledge in the quality of the learned models. All experiments are run on an Intel Core i5 3.10 GHz x 4 with 8 GB of RAM.

The classical planner we used to solve the instances that result from our compilations is the SAT-based plannerMADAGASCAR [Rintanen, 2014]. We used MADAGASCAR due to its ability to deal with planning instances populated with dead-ends [López *et al.*, 2015].

For the sake of reproducibility, the compilation source code, evaluation scripts, used benchmarks and input *state-invariants* are fully available at the repository *https://github.com/anonsub/*.

6 Related work

In *Inductive Logic Programming* it is common to make the hypothesis be consistent with the *background knowledge*, that is some form *deductive knowledge* apart from the examples [Muggleton and De Raedt, 1994].

State-invariants have also been previously used to improve the automatic construction of HTN planning model [Lotinac and Jonsson, 2016].

7 Conclusions

In some contexts it is however reasonable to assume that the action model is not learned from scratch, e.g. because some parts of the action model are known [Zhuo *et al.*, 2013; Sreedharan *et al.*, 2018; Pereira and Meneguzzi, 2018]. Our compilation is also flexible to this particular learning scenario. The known preconditions and effects are encoded setting the corresponding fluents $\{pre\_e\_\xi, eff\_e\_\xi\}_{\forall e \in \mathcal{I}_{\Psi,\xi}}$ to true in the initial state. Further, the corresponding insert actions, $\mathsf{insertPre}_{\mathsf{p},\xi}$ and $\mathsf{insertEff}_{\mathsf{p},\xi}$, become unnecessary and are removed from

A_Λ, making the classical planning task P_Λ easier to be solved. For example, suppose that the preconditions of the *blocksworld* action schema `stack` are known, then the initial state is extended with literals, `(pre_holding_v1_stack)` and `(pre_clear_v2_stack)` and the associated actions $\mathsf{insertPre}_{\mathsf{holding_v1,stack}}$ and $\mathsf{insertPre}_{\mathsf{clear_v2,stack}}$ can be safely removed from the A_Λ action set without altering the *soundness* and *completeness* of the P_Λ compilation.

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