

# Goal Recognition as Planning with Unknown Domain Models

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## Abstract

The *plan recognition as planning* approach assumes that *observers* must have both correct and complete knowledge of the action model of the observed agents. This paper shows that this assumption can be relaxed formulating a novel setup for classical planning where action models are unknown but the state variables and the action parameters are however known. The experimental results demonstrate that this novel classical planning setup allows us to solve standard goal recognition benchmarks, still using an off-the-shelf classical planner, but without knowing beforehand the precise action model of the observed agents.

## Introduction

*Goal recognition* is a particular classification task in which each class represents a different goal for the observed agents and classification examples are observations of the agents pursuing one of those goals. While there exist diverse approaches for *goal recognition*, *plan recognition as planning* (Ramírez and Geffner 2009; ?) is one of the most popular and it is currently at the core of various model-based activity recognition tasks such as, *goal recognition design* (Keren, Gal, and Karpas 2014), *deceptive planning* (Masters and Sardina 2017), *planning for transparency* (MacNally et al. 2018) or *counter-planning* (Pozanco et al. 2018).

*Plan recognition as planning* leverages the action model of the observed agents, a single plan observation, and an off-the-shelf classical planner to estimate the most likely goal of the observed agents (Ramírez 2012). In this paper we show how to relax the assumption of *knowing the action model of the observed agents*, which can become a too strong requirement when applying *plan recognition as planning* on real-world problems. We formulate a novel set up for classical planning where no action model is given (instead, only the state variables and the action parameters are known beforehand) and we show that this formulation neatly fits into the *plan recognition as planning* approach. The experimental results demonstrate that we can solve standard goal recognition benchmarks, still using an off-the-shelf classical planner, but without requiring having at hand a model of

the *preconditions* and *effects* of the actions of the observed agents

## Background

This section formalizes the *classical planning* model that we follow in this work, the kind of *observations* that input the *goal recognition* task, and the *plan recognition as planning* approach for *goal recognition*.

### Classical planning with conditional effects

We denote as  $F$  (*fluents*) the set of propositional state variables. A partial assignment of values to fluents is represented by  $L$  (*literals*). We adopt the *open world assumption* (what is not known to be true in a state is unknown) to implicitly represent the unobserved literals of a state. Hence, a state  $s$  includes positive literals ( $f$ ) and negative literals ( $\neg f$ ) and it is defined as a full assignment of values to fluents;  $|s| = |F|$ . We use  $\mathcal{L}(F)$  to denote the set of all literal sets on  $F$ ; i.e. all partial assignments of values to fluents.

A *planning action*  $a$  comprises a set of preconditions  $\text{pre}(a) \in \mathcal{L}(F)$  and a set of effects  $\text{eff}(a) \in \mathcal{L}(F)$ . The semantics of an action  $a$  is specified with two functions:  $\rho(s, a)$  denoting whether  $a$  is *applicable* in a state  $s$  and  $\theta(s, a)$  denoting the *successor state* that results from applying  $a$  in a state  $s$ . Then,  $\rho(s, a)$  holds iff  $\text{pre}(a) \subseteq s$ , i.e. the action preconditions hold in the given state. The result of executing an applicable action  $a$  in a state  $s$  is a new state  $\theta(s, a) = \{s \setminus \neg\text{eff}(a) \cup \text{eff}(a)\}$ , where  $\neg\text{eff}(a)$  is the complement of  $\text{eff}(a)$ , which is subtracted from  $s$  so as to ensure that  $\theta(s, a)$  remains a well-defined state. The subset of effects of an action  $a$  that assign a positive value to a fluent is called *positive effects* and denoted by  $\text{eff}^+(a) \in \text{eff}(a)$  while  $\text{eff}^-(a) \in \text{eff}(a)$  denotes the *negative effects*.

Planning actions can also define *conditional effects*. Formally the conditional effects of an action  $a_c$  is composed of two sets of literals:  $C \in \mathcal{L}(F)$ , the *condition*, and  $E \in \mathcal{L}(F)$ , the *effect*. The *triggered effects* resulting from the action application (conditional effects whose conditions hold in  $s$ ) is defined as  $\text{eff}_c(s, a) = \bigcup_{C \supset E \in \text{cond}(a_c), C \subseteq s} E$ .

A *planning problem* is a tuple  $P = \langle F, A, I, G \rangle$ , where  $A$  is a set of actions,  $I$  is the initial state and  $G \in \mathcal{L}(F)$  is the set of goal conditions over the state variables. A *plan*  $\pi$  is an action sequence  $\pi = \langle a_1, \dots, a_n \rangle$ , with  $|\pi| = n$  denoting

its *plan length*. The execution of  $\pi$  in  $I$  induces a *trajectory*  $\tau = \langle s_0, a_1, s_1, \dots, a_n, s_n \rangle$  such that  $s_0 = I$  and, for each  $1 \leq i \leq n$ , it holds  $\rho(s_{i-1}, a_i)$  and  $s_i = \theta(s_{i-1}, a_i)$ . A plan  $\pi$  solves  $P$  iff the induced trajectory reaches a final state  $s_n$  such that  $G \subseteq s_n$ .

### The observation model

Given a planning problem  $P = \langle F, A, I, G \rangle$ , a plan  $\pi$  that solves  $P$ , and the corresponding trajectory  $\tau$  induced by the execution of  $\pi$  in  $I$ ,  $\tau = \langle s_0, a_1, s_1, \dots, a_n, s_n \rangle$ ; there exist as many observations of  $\tau$  as combinations of observable actions and observable fluents of the states of  $\tau$ . We refer to the set of all possible combinations of observable elements of  $\tau$  as  $Obs(\tau)$ .

We define an *observation*  $\mathcal{O} \in Obs(\tau)$  as a sequence of possibly *partially observable states*,  $\mathcal{O} = \langle s_0^o, s_1^o, \dots, s_m^o \rangle$ , except for the initial state  $s_0^o = I$  which is fully observable. A *partially observable state* is one in which  $|s_i^o| < |F|$ ,  $1 \leq i \leq m \leq n$ ; i.e., a state in which at least a fluent of  $F$  is not observable. It may be also the case that  $|s_i^o| = 0$  when an intermediate state is fully unobservable.

The observation model can also include *observed actions* as fluents indicating the applied action in a given state. This means that a sequence of observed actions  $\langle a_1^o, \dots, a_l^o \rangle$  is a sub-sequence of  $\pi = \langle a_1, \dots, a_n \rangle$  such that  $a_i^o \in s_{i-1}^o$ ,  $0 \leq i \leq l$ . Consequently, the number of fluents that represent observed actions,  $l$ , can range from 0 (in a fully unobservable action sequence) to  $|\pi| = n$  (in a fully observed action sequence).

Given  $\mathcal{O} \in Obs(\tau)$ , the number of observed states of  $\mathcal{O} = \langle s_0^o, s_1^o, \dots, s_m^o \rangle$  ranges from 2 (at least the initial and final state, as explained above) to  $|\pi| + 1$ . The number of fluents of the full observable state  $s_0^o$  will be  $|F|$ , or  $|F| + 1$  in case the fluent of the applied action in  $s_0$  is also observed. Every observable intermediate state will comprise a number of fluents between  $[1, |F| + 1]$ , where a single fluent may represent a sensing fluent of the state or the observation of the applied action.

This observation model can distinguish between *observable state variables*, whose value may be read from sensors, and *hidden (or latent) state variables*, that cannot be observed. Given a subset of fluents  $\Gamma \subseteq F$  we say that  $\mathcal{O}$  is a  $\Gamma$ -observation of the execution of  $\pi$  on  $P$  iff for every observed state  $s_i^o$ ,  $1 \leq i \leq m$ ,  $s_i^o$  only contains fluents in  $\Gamma$ .

### Goal recognition as planning

*Goal recognition* is a specific classification task in which each class represents a different possible goal  $G \in G[\cdot]$  (where  $G[\cdot]$  represents the set of *recognizable* goals) and there is a single classification example  $\mathcal{O}(\tau)$  (that represents the observation of a plan where agents act to achieve a goal  $G \in G[\cdot]$ ).

Following the *naive Bayes classifier*, the *solution* to the *goal recognition* task is the subset of goals in  $G[\cdot]$  that maximizes this expression.

$$\operatorname{argmax}_{G \in G[\cdot]} P(\mathcal{O}|G)P(G). \quad (1)$$

The *plan recognition as planning* approach for goal recognition shows that the  $P(\mathcal{O}|G)$  likelihood can be es-

timated leveraging the action model of the observed agents and an off-the-shelf classical planner (Ramírez 2012). Given  $P = \langle F, A, I, G[\cdot] \rangle$  then  $P(\mathcal{O}|G)$  is estimated computing, for each goal  $G \in G[\cdot]$ , the cost difference of the solution plans to two classical planning problems:

- $P_G^\top$ , the classical planning problem built constraining  $P = \langle F, A, I, G \rangle$  to achieve the particular goal  $G \in G[\cdot]$  through a plan  $\pi^\top$  that is *consistent* with the input observation  $\mathcal{O}$ .
- $P_G^\perp$ , the classical planning problem that constrains solutions of  $P = \langle F, A, I, G \rangle$  to plans  $\pi^\perp$ , that achieve  $G \in G[\cdot]$ , but that are *inconsistent* with  $\mathcal{O}$ .

The higher the value of the  $\Delta(\pi^\top, \pi^\perp)$  cost difference, the higher the probability of the observed agents to aim goal  $G \in G[\cdot]$ . *Plan recognition as planning* uses the *sigmoid function* to map the previous cost difference into a likelihood:

$$P(\mathcal{O}|G) = \frac{1}{1 + e^{-\beta \Delta(\pi^\top, \pi^\perp)}} \quad (2)$$

This expression is derived from the assumption that while the observed agents are not perfectly rational, they are more likely to follow cheaper plans, according to a *Logistic* distribution. The larger the value of  $\beta$ , the more rational the agents, and the less likely that they will follow suboptimal plans. Recent work on *goal recognition* exploit the structure of action *preconditions* and *effects* to compute fast estimates of the  $P(\mathcal{O}|G)$  likelihood (Pereira, Oren, and Meneguzzi 2017).

To compute the target probability distribution  $P(G|\mathcal{O})$  plug the  $P(\mathcal{O}|G)$  likelihoods into the *Bayes rule* from which the goal posterior probabilities are obtained. In this case the  $P(\mathcal{O})$  probabilities are obtained by normalization (goal probabilities must add up to 1 when summed over all possible goals).

### Goal recognition as planning with unknown domain models

We define the task of *goal recognition with unknown domain models* as a  $\langle P, \mathcal{O} \rangle$  pair, where:

- $P = \langle F, A[\cdot], I, G[\cdot] \rangle$  is a classical planning problem where  $G[\cdot]$  is the set of *recognizable* goals and  $A[\cdot]$  is a set of actions s.t., for each  $a \in A[\cdot]$ , the semantics of  $a$  is unknown (i.e. the functions  $\rho$  and/or  $\theta$  of  $a$  are undefined).
- $\mathcal{O}$  is the observation of the execution of an unknown plan  $\pi$  to reach goal  $G \in G[\cdot]$  starting from the given initial state  $I = s_0^o$ .

The *solution* to the *goal recognition with unknown domain models* task is again the subset of goals in  $G[\cdot]$  that maximizes expression (1). With this regard this new task is defined exactly as the original goal recognition task (Ramírez 2012) except that the preconditions and effects of the input set of actions are now unknown.

## Estimating $P(\mathcal{O}|G)$ with unknown action models

Our approach to estimate the  $P(\mathcal{O}|G)$  likelihood is to leverage the available input knowledge to build a reasonable model for the actions in  $A[\cdot]$ , use such model to compute solution plans to the classical planning problems  $P_G^\top$  and  $P_G^\perp$  and, estimate  $P(\mathcal{O}|G)$  as in the *plan recognition as planning* approach for goal recognition.

In more detail, given  $P$  and  $\mathcal{O}$ , we compute the estimate of the  $P(\mathcal{O}|G)$  likelihood following these steps:

1. Compute an action model  $A$  that is able to solve  $P_G^\top$ , the classical planning problem that constrains solutions of  $\langle F, A[\cdot], I, G \rangle$  to plans  $\pi^\top$  consistent with the input observation  $\mathcal{O}$ .
2. Replace  $A[\cdot]$  with  $A$ , solve  $P_G^\top$  and take  $\text{cost}(\pi^\top)$  from that solution.
3. Replace  $A[\cdot]$  with  $A$ , solve  $P_G^\perp$  (i.e., the classical planning problem that constrains  $\langle F, A, I, G \rangle$  to achieve  $G \in G[\cdot]$  through a plan  $\pi^\perp$  inconsistent with  $\mathcal{O}$ ) and take  $\text{cost}(\pi^\perp)$  from that solution.
4. Compute the  $\Delta(\pi^\top, \pi^\perp)$  cost difference and plug it into equation (2) to get the  $P(\mathcal{O}|G)$  likelihoods.

## Planning with unknown domain models

This section formulates *planning with unknown domain models*, a novel setup for classical planning where no action model is given. The state variables, action parameters and a single plan observation are known though. This setup is closely related to the learning of planning action models (Stern and Juba 2017) and can be seen as an extreme learning task where action models must be *learned* from a single example that contain only two state observations: the initial state and the goals. This planning setup is of interest because it allows to formulate steps 1. and 2. as a single classical planning problem.

A *classical planning with unknown domain models* is defined as a tuple  $P = \langle F, A[\cdot], I, G \rangle$ , where  $A[\cdot]$  is a set of actions s.t., the semantics of each action  $a \in A[\cdot]$  is unknown (i.e. the functions  $\rho$  and/or  $\theta$  of  $a$  are undefined).

A *solution plan* is a sequence of actions  $\pi = \langle a_1, \dots, a_n \rangle$  whose execution on  $I$  induces a trajectory  $\tau = \langle s_0, a_1, s_1, \dots, a_n, s_n \rangle$  such that  $s_0 = I$  and there exists at least one possible action model (e.g. one possible definition of the  $\rho$  and  $\theta$  functions within the given state variables) satisfying:

- For every  $1 \leq i \leq n$  then  $\rho(s_{i-1}, a_i) = \text{True}$ .
- For every  $1 \leq i \leq n$  then  $s_i = \theta(s_{i-1}, a_i)$ .
- Goals are met at the final state  $G \subseteq s_n$ .

We can define further constraints to reduce the hypothesis space for the functions  $\rho(s, a)$  and  $\theta(s, a)$  corresponding to the  $A[\cdot]$  actions:

- *Observations*. The action model must be consistent with the input observation. Specifically, the states induced by plans computable with such model must comprise the observed states of the sample, which further constrains the space of possible action models. The observation  $\mathcal{O}$  can

also be regarded as a sequence of ordered *landmarks* for the planning problem  $P_{\mathcal{O}}$  (Hoffmann, Porteous, and Sebastia 2004) since all the fluents of the sets in  $\mathcal{O}$  must be achieved by any plan that solves  $P_{\mathcal{O}}$  and in the same order as defined in the observation  $\mathcal{O}$ .

- *Domain-specific knowledge* is also helpful to constrain further the space of possible action schemata. For instance, in the *blocksworld* one can argue that  $\text{on}(?x, ?y)$  will not appear in the preconditions/effects of an action because, in this specific domain, a block cannot be on top of itself.
- *Partially-specified action models*. In some contexts it is however reasonable to assume that some portions of the action model are known (Zhuo, Nguyen, and Kambhampati 2013; Sreedharan, Chakraborti, and Kambhampati 2018; Pereira and Meneguzzi 2018).

## Planning with unknown STRIPS models

This section shows that, when the unknown precondition and effects of the actions in  $A[\cdot]$  follow the STRIPS model, we can solve the task of *planning with unknown domain models* (and hence estimate the  $P(\mathcal{O}|G)$  likelihood) with an off-the-shelf classical planner.

### The space of possible action models

A STRIPS *action model* is defined as  $\xi = \langle \text{name}(\xi), \text{pars}(\xi), \text{pre}(\xi), \text{add}(\xi), \text{del}(\xi) \rangle$ , where  $\text{name}(\xi)$  and parameters,  $\text{pars}(\xi)$ , define the header of  $\xi$ ; and  $\text{pre}(\xi)$ ,  $\text{del}(\xi)$  and  $\text{add}(\xi)$  are sets of fluents that represent the *preconditions*, *negative effects* and *positive effects*, respectively, of the actions induced from the action model  $\xi$ .

Let  $\Psi$  be the set of *predicates* that shape the fluents  $F$  (the initial state is a full assignment of values to fluents so the predicates  $\Psi$  are extractable from  $I$ ). The set of propositions that can appear in  $\text{pre}(\xi)$ ,  $\text{del}(\xi)$  and  $\text{add}(\xi)$  of a given  $\xi$ , denoted as  $\mathcal{I}_{\xi, \Psi}$ , are FOL interpretations of  $\Psi$  over the parameters  $\text{pars}(\xi)$ . For instance, in a four-operator *blocksworld* (Slaney and Thiébaux 2001), the  $\mathcal{I}_{\xi, \Psi}$  set contains five elements for the  $\text{pickup}(v_1)$  model,  $\mathcal{I}_{\text{pickup}, \Psi} = \{\text{handempty}, \text{holding}(v_1), \text{clear}(v_1), \text{ontable}(v_1), \text{on}(v_1, v_1)\}$  and eleven elements for the model of  $\text{stack}(v_1, v_2)$ ,  $\mathcal{I}_{\text{stack}, \Psi} = \{\text{handempty}, \text{holding}(v_1), \text{holding}(v_2), \text{clear}(v_1), \text{clear}(v_2), \text{ontable}(v_1), \text{ontable}(v_2), \text{on}(v_1, v_1), \text{on}(v_1, v_2), \text{on}(v_2, v_1), \text{on}(v_2, v_2)\}$ .

### Syntactic constraints

An action model  $\xi$  must be consistent with the STRIPS constraints:  $\text{del}(\xi) \subseteq \text{pre}(\xi)$ ,  $\text{del}(\xi) \cap \text{add}(\xi) = \emptyset$  and  $\text{pre}(\xi) \cap \text{add}(\xi) = \emptyset$ . *Typing constraints* are also a type of syntactic constraint that reduce the size of  $\mathcal{I}_{\xi, \Psi}$  (McDermott et al. 1998). Considering only these syntactic constraints, the size of the space of possible STRIPS models is given by  $2^{2 \times |\mathcal{I}_{\Psi, \xi}|}$  because one element in  $\mathcal{I}_{\xi, \Psi}$  can appear both in the preconditions and effects of  $\xi$ . Given  $p \in \mathcal{I}_{\Psi, \xi}$ , the belonging of  $p$  to the preconditions, positive effects or negative effects of  $\xi$  is handled with a propositional encoding

Encoding	Meaning
$\neg pre_{p,\xi} \wedge \neg eff_{p,\xi}$	$p$ belongs neither to the preconditions nor effects of $\xi$ ( $p \notin pre(\xi) \wedge p \notin add(\xi) \wedge p \notin del(\xi)$ )
$pre_{p,\xi} \wedge \neg eff_{p,\xi}$	$p$ is only a precondition of $\xi$ ( $p \in pre(\xi) \wedge p \notin add(\xi) \wedge p \notin del(\xi)$ )
$\neg pre_{p,\xi} \wedge eff_{p,\xi}$	$p$ is a positive effect of $\xi$ ( $p \notin pre(\xi) \wedge p \in add(\xi) \wedge p \notin del(\xi)$ )
$pre_{p,\xi} \wedge eff_{p,\xi}$	$p$ is a negative effect of $\xi$ ( $p \in pre(\xi) \wedge p \notin add(\xi) \wedge p \in del(\xi)$ )

Figure 1: Combinations of the propositional encoding and their meaning

```

(:action stack
  :parameters (?v1 ?v2)
  :precondition (and (holding ?v1) (clear ?v2))
  :effect (and (not (holding ?v1)) (not (clear ?v2))
              (clear ?v1) (handempty) (on ?v1 ?v2)))

(pre_holding_v1_stack) (pre_clear_v2_stack)
(eff_holding_v1_stack) (eff_clear_v2_stack)
(eff_clear_v1_stack) (eff_handempty_stack) (eff_on_v1_v2_stack)

```

Figure 2: PDDL encoding of the `stack(?v1, ?v2)` schema and our propositional representation for this same schema.

that uses fluents of two types,  $pre_{p,\xi}$  and  $eff_{p,\xi}$ . The four possible combinations of these two fluents are summarized in Figure 1.

To illustrate better this encoding, Figure 2 shows the PDDL encoding of the `stack(?v1, ?v2)` schema and our propositional representation for this same schema with  $pre_{p,stack}$  and  $eff_{p,stack}$  fluents ( $p \in \mathcal{I}_{\Psi,stack}$ ).

### A classical planning compilation for planning with unknown domain models

The approach for learning STRIPS action models presented in (Aineto, Jiménez, and Onaindia 2018), which we will use as our baseline learning system (hereafter BLS, for short), is a compilation scheme that transforms the problem of learning the preconditions and effects of action models into a planning task  $P'$ . A STRIPS *action model*  $\xi$  is defined as  $\xi = \langle name(\xi), pars(\xi), pre(\xi), add(\xi), del(\xi) \rangle$ , where  $name(\xi)$  and  $parameters$ ,  $pars(\xi)$ , define the header of  $\xi$ ; and  $pre(\xi)$ ,  $del(\xi)$  and  $add(\xi)$  are sets of fluents that represent the *preconditions*, *negative effects* and *positive effects*, respectively, of the actions induced from the action model  $\xi$ .

The BLS receives as input an empty domain model, which only contains the headers of the action models, and a set of observations of plan executions, and creates a propositional encoding of the planning task  $P'$ . Let  $\Psi$  be the set of *predicates*<sup>1</sup> that shape the variables  $F$ .

<sup>1</sup>The initial state of an observation is a full assignment of values to fluents,  $|s_0| = |F|$ , and so the predicates  $\Psi$  are extractable from

The set of propositions of  $P'$  that can appear in  $pre(\xi)$ ,  $del(\xi)$  and  $add(\xi)$  of a given  $\xi$ , denoted as  $\mathcal{I}_{\xi,\Psi}$ , are FOL interpretations of  $\Psi$  over the parameters  $pars(\xi)$ . For instance, in a four-operator *blocksworld* (Slaney and Thiébaux 2001), the  $\mathcal{I}_{\xi,\Psi}$  set contains five elements for the `pickup( $v_1$ )` model,  $\mathcal{I}_{pickup,\Psi} = \{handempty, holding(v_1), clear(v_1), ontable(v_1), on(v_1, v_1)\}$  and eleven elements for the model of `stack( $v_1, v_2$ )`,  $\mathcal{I}_{stack,\Psi} = \{handempty, holding(v_1), holding(v_2), clear(v_1), clear(v_2), ontable(v_1), ontable(v_2), on(v_1, v_1), on(v_1, v_2), on(v_2, v_1), on(v_2, v_2)\}$ . Hence, solving  $P'$  consists in determining which elements of  $\mathcal{I}_{\xi,\Psi}$  will shape the preconditions, positive and negative effects of each action model  $\xi$ .

The decision as to whether or not an element of  $\mathcal{I}_{\xi,\Psi}$  will be part of  $pre(\xi)$ ,  $del(\xi)$  or  $add(\xi)$  is given by the plan that solves  $P'$ . Specifically, two different sets of actions are included in the definition of  $P'$ : *insert actions*, which insert preconditions and effects on an action model; and *apply actions*, which validate the application of the learned action models in the input observations. Roughly speaking, in the *blocksworld* domain, the insert actions of a plan that solves  $P'$  will look like `(insert_pre_stack_holding_v1)`,

`(insert_eff_stack_clear_v1)`, `(insert_eff_stack_clear_v2)`, where the second action denotes a positive effect and the third one a negative effect both to be inserted in the model of `stack`; and the second set of actions of the plan that solves  $P'$  will be like `(apply_unstack_blockB_blockA)`, `(validate_1)`, `(apply_putdown_blockB)`, `(validate_2)`, where the `validate` actions denote the points at which the states generated through the `apply` actions must be validated with the observations of plan executions.

In a nutshell, the output of the BLS compilation is a plan that completes the empty input domain model by specifying the preconditions and effects of each action model such that the validation of the completed model over the input observations is successful.

### Observations

This requires the compilation to include actions for *validating* partially observed states  $s_j^o \in \mathcal{O}$ . These actions are also part of the postfix of the solution plan  $\pi_\Lambda$  and they are aimed at checking that the observation  $\mathcal{O}$  follows after the execution of the `apply` actions.

$$\begin{aligned}
 pre(validate_j) &= s_j^o \cup \{test_{j-1}\}, \\
 cond(validate_j) &= \{\emptyset\} \triangleright \{\neg test_{j-1}, test_j\}.
 \end{aligned}$$

There will be a `validate` action in  $\pi_\Lambda$  for every observed state in  $\mathcal{O}$ . The position of the `validate` actions in  $\pi_\Lambda$  will be determined by the planner by checking that the state resulting after the execution of an `apply` action comprises the observed state  $s_j^o \in \mathcal{O}$ .

the observed state  $s_0$ .

## Domain-specific constraints

Our approach is to introduce *domain-specific knowledge* in the form of *state constraints* to further restrict the space of the action models. Back to the *blocksworld* domain, one can argue that  $\text{on}(v_1, v_1)$  and  $\text{on}(v_2, v_2)$  will not appear in the  $\text{pre}(\xi)$ ,  $\text{del}(\xi)$  and  $\text{add}(\xi)$  of any action model  $\xi$  because, in this specific domain, a block cannot be on top of itself. The notion of state constraint is very general and has been used in different areas of AI and for different purposes. In planning, state constraints are compact and abstract representations that relate the values of variables in each state traversed by a plan, and allow to specify the set of states where a given action is applicable, the set of states where a given *axiom* or *derived predicate* holds or the set of states that are considered goal states (Haslum et al. 2018).

*State invariants* is a useful type of state constraints for computing more compact state representations of a given planning problem (Helmert 2009) and for making *satisfiability planning* or *backward search* more efficient (Rintanen 2014; Alcázar and Torralba 2015). Given a planning problem  $P = \langle F, A, I, G \rangle$ , a state invariant is a formula  $\phi$  that holds in  $I$ ,  $I \models \phi$ , and in every state  $s$  built out of  $F$  that is reachable by applying actions of  $A$  in  $I$ .

A *mutex* (mutually exclusive) is a state invariant that takes the form of a binary clause and indicates a pair of different properties that cannot be simultaneously true (Kautz and Selman 1999). For instance in a three-block *blocksworld*,  $\neg \text{on}(\text{block}_A, \text{block}_B) \vee \neg \text{on}(\text{block}_A, \text{block}_C)$  is a *mutex* because  $\text{block}_A$  can only be on top of a single block.

Recently, some works point at extracting *lifted* invariants, also called *schematic* invariants (Rintanen 2017), that hold for any possible state and any possible set of objects. Invariant templates obtained by inspecting the lifted representation of the domain have also been exploited for deriving *lifted mutex* (Bernardini, Fagnani, and Smith 2018). In this work we exploit domain-specific knowledge that is given as *schematic mutex*. We pay special attention to *schematic mutex* because they identify mutually exclusive properties of a given type of objects (Fox and Long 1998) and because they enable (1) an effective completion of a partially observed state and (2) an effective pruning of inconsistent STRIPS action models.

We define a schematic mutex as a  $\langle p, q \rangle$  pair where both  $p, q \in \mathcal{I}_{\xi, \Psi}$  are predicates that shape the preconditions or effects of a given action scheme  $\xi$  and they satisfy the formulae  $\neg p \vee \neg q$ , considering that their corresponding variables are universally quantified. For instance,  $\text{holding}(v_1)$  and  $\text{clear}(v_1)$  from the *blocksworld* are *schematic mutex* while  $\text{clear}(v_1)$  and  $\text{ontable}(v_1)$  are not because  $\forall v_1, \neg \text{clear}(v_1) \vee \neg \text{ontable}(v_1)$  does not hold for every possible state. Figure 3 shows an example of four clauses that define schematic mutexes for the *blocksworld* domain.

*state invariants* can be exploited either as *syntactic* constraints (to reduce the space of possible action models) but also as *semantic* constraints (to complete partial observations of the states traversed by a plan) (Fox and Long 1998).

$$\begin{aligned} &\forall x_1, x_2 \neg \text{ontable}(x_1) \vee \neg \text{on}(x_1, x_2). \\ &\forall x_1, x_2 \neg \text{clear}(x_1) \vee \neg \text{on}(x_2, x_1). \\ &\forall x_1, x_2, x_3 \neg \text{on}(x_1, x_2) \vee \neg \text{on}(x_1, x_3) \text{ such that } x_2 \neq x_3. \\ &\forall x_1, x_2, x_3 \neg \text{on}(x_2, x_1) \vee \neg \text{on}(x_3, x_1) \text{ such that } x_2 \neq x_3. \end{aligned}$$

Figure 3: *Schematic mutexes* for the *blocksworld* domain.

ID	Action	New conditional effect
1	$(\text{insert\_pre})_{\xi, p}$	$\{pre\_q\} \triangleright \{invalid\}$
2	$(\text{insert\_eff})_{\xi, p}$	$\{pre\_q \wedge eff\_q \wedge pre\_p\} \triangleright \{invalid\}$
3	$(\text{insert\_eff})_{\xi, p}$	$\{\neg pre\_q \wedge eff\_q \wedge \neg pre\_p\} \triangleright \{invalid\}$
4	$(\text{apply})_{\xi, \omega}$	$\{\neg pre\_p \wedge eff\_p \wedge q(\omega) \wedge \neg pre\_q\} \triangleright \{invalid\}$
5	$(\text{apply})_{\xi, \omega}$	$\{\neg pre\_p \wedge eff\_p \wedge q(\omega) \wedge \neg eff\_q\} \triangleright \{invalid\}$

Figure 4: Summary of the new conditional effects added to the classical planning compilation for the learning of STRIPS action models.

**Completing partially observed states with *schematic mutexes*** The addition of new literals to complete the partial states  $\langle s_1^o, \dots, s_m^o \rangle$  of an observation  $\mathcal{O}$  using a set of schematic mutexes  $\Phi$  is done in a pre-processing stage.

Let  $\Omega$  be the set of objects that appear in  $F$  as the values of the arguments of the predicates  $\Psi$ , and  $\phi = \langle p, q \rangle$  a schematic mutex. There exist many possible instantiations of  $\phi$  of the type  $\langle p(\omega), q(\omega') \rangle$  with objects of  $\Omega$ , where  $\omega \subseteq \Omega^{|\text{args}(p)|}$  and  $\omega' \subseteq \Omega^{|\text{args}(q)|}$ . Let us now assume that the instantiation  $p(\omega) \in s_j^o$ , ( $1 \leq j \leq m$ ), being  $s_j^o$  a partially observed state of  $\mathcal{O}$ . Then, two situations may occur: (a)  $\neg q(\omega') \in s_j^o$ , in which case the expression  $\neg p(\omega) \vee \neg q(\omega')$  holds in  $s_j^o$ ; or (b)  $\neg q(\omega') \notin s_j^o$ , in which case the literal has not been observed in  $s_j^o$  and so we can safely complete the state with  $\neg q(\omega')$  (the same applies inversely, when  $q(\omega') \in s_j^o$  but  $\neg p(\omega) \notin s_j^o$ ). In other words, if we find that one component of a schematic mutex is positively observed in a state and the other component is not observable in such state, we can complete the state with the missing negative literal. For instance, if the literal  $\text{holding}(\text{block}_A)$  is observed in a particular state and  $\Phi$  contains the schematic mutex  $\neg \text{holding}(v_1) \vee \neg \text{clear}(v_1)$ , we extend the state observation with literal  $\neg \text{clear}(\text{block}_A)$  (despite this particular literal being initially unknown).

**Pruning inconsistent action models with *schematic mutexes*** We could extend the classical planning compilation for the learning of STRIPS action models (Aineto, Jiménez, and Onaindia 2018) to check the consistency of the *state-constraints* in  $\Phi$  at every state traversed by a solution to the compiled problem. Unfortunately, checking arbitrary  $\phi$  formulae is too expensive for current classical planners.

Instead, our approach is to define a mechanism to check *state-constraints* in the form of *schematic mutex*. To implement this checking mechanism we add new conditional effects to the *insert* and *apply* actions of the classical planning compilation. Figure 4 summarizes the new conditional effects added to the compilation and next, we describe them in

detail:

Our approach to learning action models consistent with the schematic mutexes in  $\Phi$  is to ensure that newly generated states induced by the learned actions do not introduce any inconsistency. This is implemented by adding new conditional effects to the `insert` and `apply` actions of the BLS compilation. Figure 4 summarizes the new conditional effects added to the compilation and next, we describe them in detail:

- 1-3 For every schematic mutex  $\langle p, q \rangle$ , where both  $p$  and  $q$  belong to  $\mathcal{I}_{\xi, \Psi}$ , one conditional effect is added to the  $(\text{insert\_pre})_{\xi, p}$  actions to prevent the insertion of two preconditions that are schematic mutex. Likewise, two conditional effects are added to the  $(\text{insert\_eff})_{\xi, p}$  actions, one to prevent the insertion of two positive effects that are schematic mutex and another one to prevent two mutex negative effects.
- 4-5 For every schematic mutex  $\langle p, q \rangle$ , where both  $p$  and  $q$  belong to  $\mathcal{I}_{\xi, \Psi}$ , two conditional effects are added to the  $(\text{apply})_{\xi, \omega}$  actions to prevent positive effects that are inconsistent with an input observation (in  $(\text{apply})_{\xi, \omega}$  actions the variables in  $\text{pars}(\xi)$  are bounded to the objects in  $\omega$  that appear in the same position).

In theory, conditional effects of the type 4-5 are sufficient to guarantee that all the states traversed by a plan produced by the compilation are *consistent* with the input set of schematic mutexes  $\Phi$  (obviously provided that the input initial state  $s_0^o$  is a valid state). In practice we include also conditional effects of the type 1-3 because they prune *invalid* action models at an earlier stage of the planning process (these effects extend the `insert` actions that always appear first in the solution plans).

The goals of the planning task  $P'$  generated by the original BLS compilation are extended with the  $\neg \text{invalid}$  literal to validate that only states consistent with the state constraints defined in  $\Phi$  are traversed by solution plans. Remarkably, the  $\neg \text{invalid}$  literal allows us also to define  $(\text{apply})_{\xi, \omega}$  actions more compactly than in the original compilation. Disjunctions are no longer required to code the possible preconditions of an action schema since they can now be encoded with conditional effects of the type  $\{pre\_e\_p \wedge \neg p(\omega)\} \triangleright \{\text{invalid}\}$ .

### Partially specified action models

Our compilation approach is also flexible to this particular scenario. The known preconditions and effects are encoded setting the corresponding fluents  $\{pre\_e\_e, eff\_e\_e\}_{e \in \mathcal{I}_{\Psi, \xi}}$  to true in the initial state. Further, the corresponding insert actions,  $\text{insertPre}_{p, \xi}$  and  $\text{insertEff}_{p, \xi}$ , become unnecessary and are removed from  $A_\Lambda$ , making the classical planning task  $P_\Lambda$  easier to be solved.

For example, suppose that the preconditions of the *blocksworld* action schema `stack` are known, then the initial state  $I$  is extended with literals,  $(\text{pre\_holding\_v1\_stack})$  and  $(\text{pre\_clear\_v2\_stack})$  and the associated actions  $\text{insertPre}_{\text{holding\_v1\_stack}}$  and  $\text{insertPre}_{\text{clear\_v2\_stack}}$  can be safely removed from the  $A_\Lambda$

action set without altering the *soundness* and *completeness* of the  $P_\Lambda$  compilation.

## Evaluation

### Related Work

The problem of *classical planning with unknown domain models* has been previously addressed (Stern and Juba 2017). In this work we evidence the relevance of this task for addressing *goal recognition* when the action model of the observed agent is not available.

The paper also showed that *goal recognition*, when the domain model is unknown, is closely related to the learning of planning action models. With this regard, the classical planning compilation for learning STRIPS action models (Aineto, Jiménez, and Onaindia 2018) is very appealing because it allows to produce a STRIPS action model from minimal input knowledge (a single initial state and goals pair), and to refine this model if more input knowledge is available (e.g. observation constraints). Most of the existing approaches for learning action models aim maximizing an statistical consistency of the learned model with respect to the input observations so require large amounts of input knowledge and do not produce action models that are guaranteed to be *logically consistent* with the given input knowledge.

Our approach for *planning with an unknown domain model* is related to *goal recognition design* (Keren, Gal, and Karpas 2014). The reason is that we are encoding the space of propositional schemes as state variables of the planning problem (the initial state encodes the *empty* action model with no preconditions and no effects) and provide actions to modify the value of this state variables as in *goal recognition design*. The aims of *goal recognition design* are however different. *Goal recognition design* applied to *goal recognition with unknown domain models* would compute the action model, in the space of possible models, that allows to reveal any of the possible goals as early as possible.

## Conclusions

Classical planners tend to preffer shorter solution plans, so our compilation may introduce a bias to  $P = \langle F, A[\cdot], I, G \rangle$  problems preferring solutions that are referred to action models with a shorter number of *preconditions/effects*. In more detail, all  $\{pre\_e\_e, eff\_e\_e\}_{e \in \mathcal{I}_{\Psi, \xi}}$  fluents are false at the initial state of our  $P' = \langle F', A', I, G \rangle$  compilation so classical planners tend to solve  $P'$  with plans that require a shorter number of *insert* actions.

This bias could be eliminated defining a cost function for the actions in  $A'$  (e.g. *insert* actions has *zero cost* while  $\text{apply}_{\xi, \omega}$  actions has a *positive constant cost*). In practice we use a different approach to disregard the cost of *insert* actions because classical planners are not proficiency optimizing *plan cost* with zero-cost actions. Instead, our approach is to use a SAT-based planner (Rintanen 2014) because it can apply all actions for inserting preconditions in a single planning step (these actions do not interact). Further, the actions for inserting action effects are also applied in a single planning step so the plan horizon for programming any action

model is always bound to 2, which significantly reduces the planning horizon.

Our compilation for *planning with unknown domain models* can then be understood as an extension of the SATPLAN approach for classical planning (Kautz, Selman, and others 1992) with two additional initial layers: a first layer for inserting the action preconditions and a second one for inserting the action effects. These two extra layers are followed by the typical  $N$  layers of the SATPLAN encoding (extended however to apply the action models that are determined by the previous two initial layers, the  $\text{apply}_{\xi, \omega}$  actions). Regarding again the example of Figure ??, this means that steps [00-04] are applied in parallel in the first SATPLAN layer, steps [05-13] are applied in parallel in the second layer and each step [14-17] is applied sequentially and corresponds to a different SATPLAN layer (so just six layers are necessary to compute the example plan of Figure ??).

The SAT-based planning approach is also convenient for the task of *goal recognition as planning with unknown domain models* because its ability to deal with classical planning problems populated with dead-ends and because symmetries in the insertion of preconditions/effects into an action model do not affect to the planning performance.

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