In [62]:
```
# Initialize OK
from client.api.notebook import Notebook
ok = Notebook('hw3.ok')
```

Homework 3: Predicting Housing Prices

Due Date: Fri 5/14, 11:59 PM

Collaboration Policy: You may talk with others about the homework, but we ask that you **write your solutions individually**. If you do discuss the assignments with others, please **include their names** in the following line.

Collaborators: *list collaborators here (if applicable)*

Score Breakdown

Question	Points
Question 1	3
Question 2	2
Question 3	1
Question 4	1
Question 5	2
Question 6	2
Question 7a	1
Question 7b	2
Question 8a	1
Question 8b	1
Question 8c	2
Question 8d	2
Total	20

Introduction

We will go through the iterative process of specifying, fitting, and analyzing the performance of a model.

In the first portion of the assignment, we will guide you through some basic exploratory data analysis (EDA), laying out the thought process that leads to certain modeling decisions. Next, you will add a new feature to the dataset, before specifying and fitting a linear model to a few features of the housing data to predict housing prices. Finally, we will analyze the error of the model and brainstorm ways to improve the model's performance.

After this homework, you should feel comfortable with the following:

1. Simple feature engineering
2. Using sklearn to build linear models
3. Building a data pipeline using pandas

Next homework will continue working with this dataset to address more advanced and subtle issues with modeling.

In [63]:
```
import numpy as np
import pandas as pd
from pandas.api.types import CategoricalDtype

%matplotlib inline
import matplotlib.pyplot as plt
import seaborn as sns

# Plot settings
plt.rcParams['figure.figsize'] = (12, 9)
plt.rcParams['font.size'] = 12
```

The Ames Housing Price Dataset

The Ames dataset (http://jse.amstat.org/v19n3/decock.pdf) consists of 2930 records taken from the Ames, Iowa, Assessor's Office describing houses sold in Ames from 2006 to 2010. The data set has 23 nominal, 23 ordinal, 14 discrete, and 20 continuous variables (and 2 additional observation identifiers) --- 82 features in total.

An explanation of each variable can be found in the included `codebook.txt` file. The information was used in computing assessed values for individual residential properties sold in Ames, Iowa from 2006 to 2010. **Some noise has been added to the actual sale price, so prices will not match official records.**

The data are split into training and test sets with 2000 and 930 observations, respectively.

In [64]:
```
training_data = pd.read_csv("./data/ames_train.csv")
test_data = pd.read_csv("./data/ames_test.csv")
```

As a good sanity check, we should at least verify that the data shape matches the description.

In [65]:
```
# 2000 observations and 82 features in training data
assert training_data.shape == (2000, 82)
# 930 observations and 81 features in test data
assert test_data.shape == (930, 81)
# SalePrice is hidden in the test data
assert 'SalePrice' not in test_data.columns.values
# Every other column in the test data should be in the training data
assert len(np.intersect1d(test_data.columns.values,
                          training_data.columns.values)) == 81
```

The next order of business is getting a feel for the variables in our data. The Ames dataset contains

information that typical homebuyers would want to know.

A more detailed description of each variable is included in `codebook.txt`. **You should take some time to familiarize yourself with the codebook before moving forward.**

In [66]:
```
training_data.columns.values
```

Out[66]:
```
array(['Order', 'PID', 'MS_SubClass', 'MS_Zoning', 'Lot_Frontage',
       'Lot_Area', 'Street', 'Alley', 'Lot_Shape', 'Land_Contour',
       'Utilities', 'Lot_Config', 'Land_Slope', 'Neighborhood',
       'Condition_1', 'Condition_2', 'Bldg_Type', 'House_Style',
       'Overall_Qual', 'Overall_Cond', 'Year_Built', 'Year_Remod/Add',
       'Roof_Style', 'Roof_Matl', 'Exterior_1st', 'Exterior_2nd',
       'Mas_Vnr_Type', 'Mas_Vnr_Area', 'Exter_Qual', 'Exter_Cond',
       'Foundation', 'Bsmt_Qual', 'Bsmt_Cond', 'Bsmt_Exposure',
       'BsmtFin_Type_1', 'BsmtFin_SF_1', 'BsmtFin_Type_2', 'BsmtFin_SF_
2',
       'Bsmt_Unf_SF', 'Total_Bsmt_SF', 'Heating', 'Heating_QC',
       'Central_Air', 'Electrical', '1st_Flr_SF', '2nd_Flr_SF',
       'Low_Qual_Fin_SF', 'Gr_Liv_Area', 'Bsmt_Full_Bath',
       'Bsmt_Half_Bath', 'Full_Bath', 'Half_Bath', 'Bedroom_AbvGr',
       'Kitchen_AbvGr', 'Kitchen_Qual', 'TotRms_AbvGrd', 'Functional',
       'Fireplaces', 'Fireplace_Qu', 'Garage_Type', 'Garage_Yr_Blt',
       'Garage_Finish', 'Garage_Cars', 'Garage_Area', 'Garage_Qual',
       'Garage_Cond', 'Paved_Drive', 'Wood_Deck_SF', 'Open_Porch_SF',
       'Enclosed_Porch', '3Ssn_Porch', 'Screen_Porch', 'Pool_Area',
       'Pool_QC', 'Fence', 'Misc_Feature', 'Misc_Val', 'Mo_Sold',
       'Yr_Sold', 'Sale_Type', 'Sale_Condition', 'SalePrice'], dtype=obje
ct)
```

Part 1: Exploratory Data Analysis

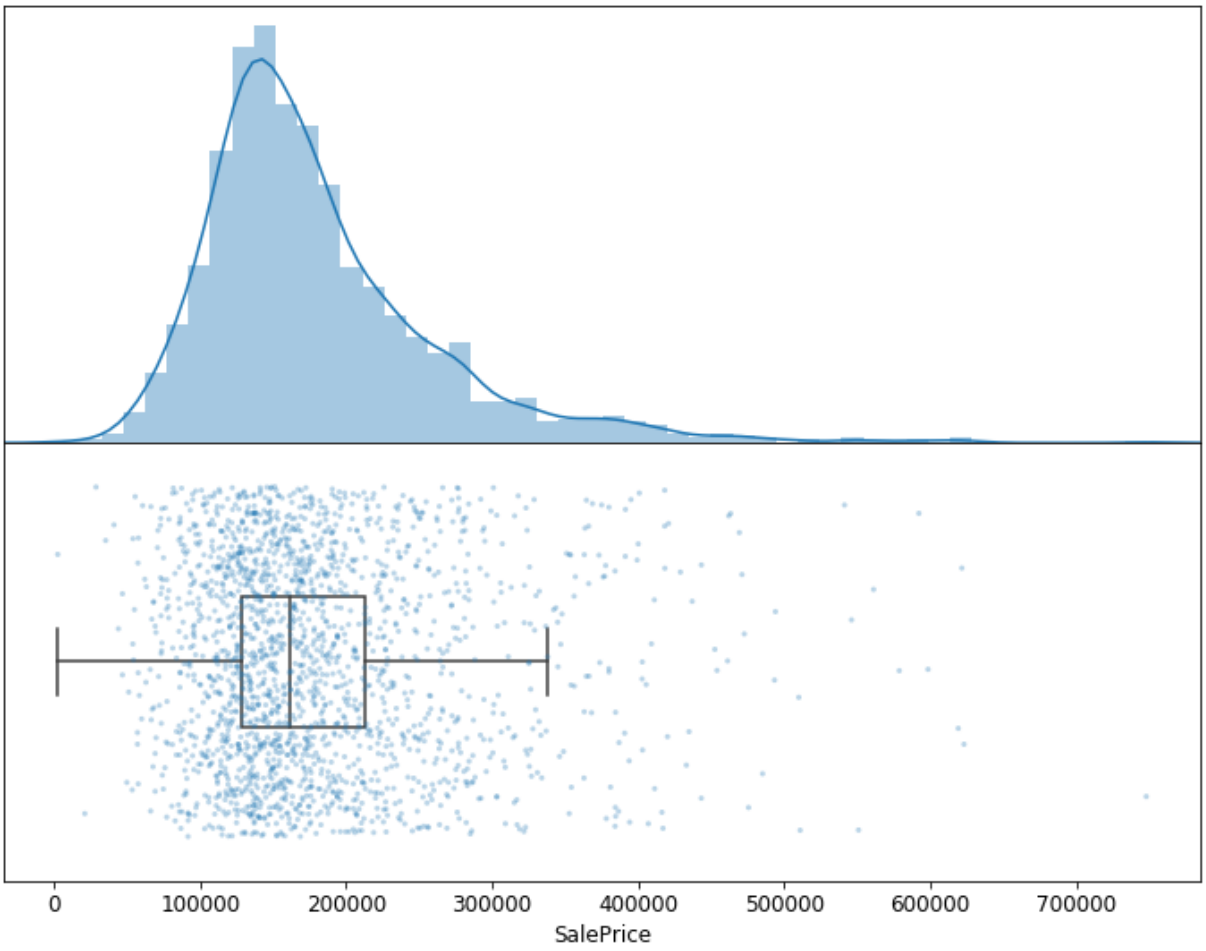
In this section, we will make a series of exploratory visualizations and interpret them.

Note that we will perform EDA on the **training data** so that information from the test data does not influence our modeling decisions.

Sale Price

We begin by examining a raincloud plot (https://micahallen.org/2018/03/15/introducing-raincloud-plots/amp/?__twitter_impression=true) (a combination of a KDE, a histogram, a strip plot, and a box plot) of our target variable `SalePrice`. At the same time, we also take a look at some descriptive statistics of this variable.

In [67]:
```
fig, axs = plt.subplots(nrows=2)

sns.distplot(
    training_data['SalePrice'],
    ax=axs[0]
)
sns.stripplot(
    training_data['SalePrice'],
    jitter=0.4,
    size=3,
    ax=axs[1],
    alpha=0.3
)
sns.boxplot(
    training_data['SalePrice'],
    width=0.3,
    ax=axs[1],
    showfliers=False,
)

# Align axes
spacer = np.max(training_data['SalePrice']) * 0.05
xmin = np.min(training_data['SalePrice']) - spacer
xmax = np.max(training_data['SalePrice']) + spacer
axs[0].set_xlim((xmin, xmax))
axs[1].set_xlim((xmin, xmax))

# Remove some axis text
axs[0].xaxis.set_visible(False)
axs[0].yaxis.set_visible(False)
axs[1].yaxis.set_visible(False)

# Put the two plots together
plt.subplots_adjust(hspace=0)

# Adjust boxplot fill to be white
axs[1].artists[0].set_facecolor('white')
```



In [68]:
```
training_data['SalePrice'].describe()
```

Out[68]:
```
count      2000.000000
mean     180775.897500
std       81581.671741
min        2489.000000
25%      128600.000000
50%      162000.000000
75%      213125.000000
max      747800.000000
Name: SalePrice, dtype: float64
```

Question 1

To check your understanding of the graph and summary statistics above, answer the following `True` or `False` questions:

1. The distribution of `SalePrice` in the training set is left-skew.
2. The mean of `SalePrice` in the training set is greater than the median.

3. At least 25% of the houses in the training set sold for more than $200,000.00.

The provided tests for this question do not confirm that you have answered correctly; only that you have assigned each variable to `True` or `False`.

In [69]:
```
# These should be True or False
q1statement1 = False
q1statement2 = True
q1statement3 = True
```

In [70]:
```
ok.grade("q1");
```

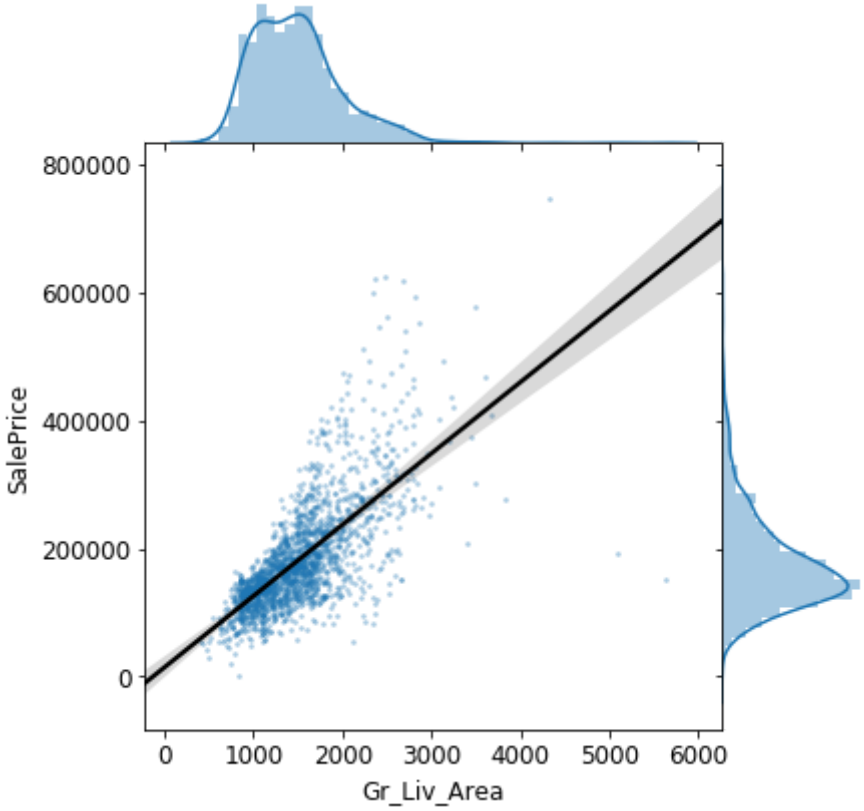
```
---------------------------------------------------------------------------
AssertionError                            Traceback (most recent call last)
<ipython-input-70-d00e0552e78a> in <module>()
----> 1 ok.grade("q1");

~/anaconda3/envs/data100/lib/python3.6/site-packages/client/api/notebook.py in grade(self, question, global_env)
     56             # inspect trick to pass in its parents' global env.
     57             global_env = inspect.currentframe().f_back.f_globals
---> 58         result = grade(path, global_env)
     59         # We display the output if we're in IPython.
     60         # This keeps backwards compatibility with okpy's grade method

~/anaconda3/envs/data100/lib/python3.6/site-packages/okgrade/grader.py in grade(test_file_path, global_env)
     59     Returns a TestResult object.
     60     """
---> 61     tests = parse_ok_test(test_file_path)
     62     if global_env is None:
     63         # Get the global env of our callers - one level below us in the stack

~/anaconda3/envs/data100/lib/python3.6/site-packages/okgrade/grader.py in parse_ok_test(path)
     24
     25     # Do not support point values other than 1
---> 26     assert test_spec.get('points', 1) == 1
     27
     28     test_suite = test_spec['suites'][0]

AssertionError:
```

SalePrice vs Gr_Liv_Area

Next, we visualize the association between `SalePrice` and `Gr_Liv_Area`. The `codebook.txt` file tells us that `Gr_Liv_Area` measures "above grade (ground) living area square feet."

This variable represents the square footage of the house excluding anything underground. Some additional research (into real estate conventions) reveals that this value also excludes the garage space.

In [71]:
```
sns.jointplot(
    x='Gr_Liv_Area',
    y='SalePrice',
    data=training_data,
    stat_func=None,
    kind="reg",
    ratio=4,
    space=0,
    scatter_kws={
        's': 3,
        'alpha': 0.25
    },
    line_kws={
        'color': 'black'
    }
);
```



There's certainly an association, and perhaps it's linear, but the spread is wider at larger values of both variables. Also, there are two particularly suspicious houses above 5000 square feet that look too inexpensive for their size.

Question 2

What are the Parcel Indentification Numbers for the two houses with `Gr_Liv_Area` greater than 5000 sqft?

The provided tests for this question do not confirm that you have answered correctly; only that you have assigned `q2house1` and `q2house2` to two integers that are in the range of PID values.

In [72]:
```
# BEGIN YOUR CODE
# ------------------------
# Hint: You can answer this question in one line
q2house1, q2house2 = training_data.loc[training_data['Gr_Liv_Area'] > 5000,
# ------------------------
# END YOUR CODE
```

In [73]:
```
ok.grade("q2");
```

```
---------------------------------------------------------------------------
--
AssertionError                            Traceback (most recent call las
t)
<ipython-input-73-907f50eefa75> in <module>()
----> 1 ok.grade("q2");

~/anaconda3/envs/data100/lib/python3.6/site-packages/client/api/notebook.
py in grade(self, question, global_env)
     56             # inspect trick to pass in its parents' global env.
     57             global_env = inspect.currentframe().f_back.f_globals
---> 58         result = grade(path, global_env)
     59         # We display the output if we're in IPython.
     60         # This keeps backwards compatibility with okpy's grade me
thod

~/anaconda3/envs/data100/lib/python3.6/site-packages/okgrade/grader.py in
grade(test_file_path, global_env)
     59     Returns a TestResult object.
     60     """
---> 61     tests = parse_ok_test(test_file_path)
     62     if global_env is None:
     63         # Get the global env of our callers - one level below us
 in the stack

~/anaconda3/envs/data100/lib/python3.6/site-packages/okgrade/grader.py in
parse_ok_test(path)
     24
     25     # Do not support point values other than 1
---> 26     assert test_spec.get('points', 1) == 1
     27
     28     test_suite = test_spec['suites'][0]

AssertionError:
```

Question 3

The codebook tells us how to manually inspect the houses using an online database called Beacon. These two houses are true outliers in this data set: they aren't the same time of entity as the rest. They were partial sales, priced far below market value. If you would like to inspect the valuations, follow the directions at the bottom of the codebook to access Beacon and look up houses by PID.

For this assignment, we will remove these outliers from the data. Write a function `remove_outliers` that removes outliers from a data set based off a threshold value of a variable. For example, `remove_outliers(training_data, 'Gr_Liv_Area', upper=5000)` should return a data frame with only observations that satisfy `Gr_Liv_Area` less than or equal to 5000.

The provided tests check that training_data was updated correctly, so that future analyses are not corrupted by a mistake. However, the provided tests do not check that you have implemented remove_outliers correctly so that it works with any data, variable, lower, and upper bound.

In [74]:
```
def remove_outliers(data, variable, lower=-np.inf, upper=np.inf):
    """
    Input:
      data (data frame): the table to be filtered
      variable (string): the column with numerical outliers
      lower (numeric): observations with values lower than this will be remo
      upper (numeric): observations with values higher than this will be rem

    Output:
      a winsorized data frame with outliers removed

    Note: This function should not change mutate the contents of data.
    """
    # BEGIN YOUR CODE
    # ------------------------
    return data.loc[(data[variable] > lower) & (data[variable] < upper), :]
    # ------------------------
    # END YOUR CODE

training_data = remove_outliers(training_data, 'Gr_Liv_Area', upper=5000)
```

In [75]:
```
ok.grade("q3");
```

```
/Users/sjk/datascience/COSE471-hw3(1)/tests/q3.py: All tests passed!
```

Part 2: Feature Engineering

In this section we will create a new feature out of existing ones through a simple data transformation.

Bathrooms

Let's create a groundbreaking new feature. Due to recent advances in Universal WC Enumeration Theory, we now know that Total Bathrooms can be calculated as:

$$\text{TotalBathrooms} = (\text{BsmtFullBath} + \text{FullBath}) + \frac{1}{2}(\text{BsmtHalfBath} + \text{HalfBath})$$

The actual proof is beyond the scope of this class, but we will use the result in our model.

Question 4

Write a function `add_total_bathrooms(data)` that returns a `copy of data` with an additional column called `TotalBathrooms` computed by the formula above.

The provided tests check that you answered correctly, so that future analyses are not corrupted by a mistake.

In [76]:
```
def add_total_bathrooms(data):
    """
    Input:
      data (data frame): a data frame containing at least 4 numeric columns
            Bsmt_Full_Bath, Full_Bath, Bsmt_Half_Bath, and Half_Bath
    """
    with_bathrooms = data.copy()
    bath_vars = ['Bsmt_Full_Bath', 'Full_Bath', 'Bsmt_Half_Bath', 'Half_Bath
    weights = pd.Series([1, 1, 0.5, 0.5], index=bath_vars)
    with_bathrooms = with_bathrooms.fillna({var: 0 for var in bath_vars})
    # BEGIN YOUR CODE
    # ------------------------
    with_bathrooms['TotalBathrooms'] = with_bathrooms[bath_vars].dot(weights
    # ------------------------
    # END YOUR CODE
    return with_bathrooms

training_data = add_total_bathrooms(training_data)
```

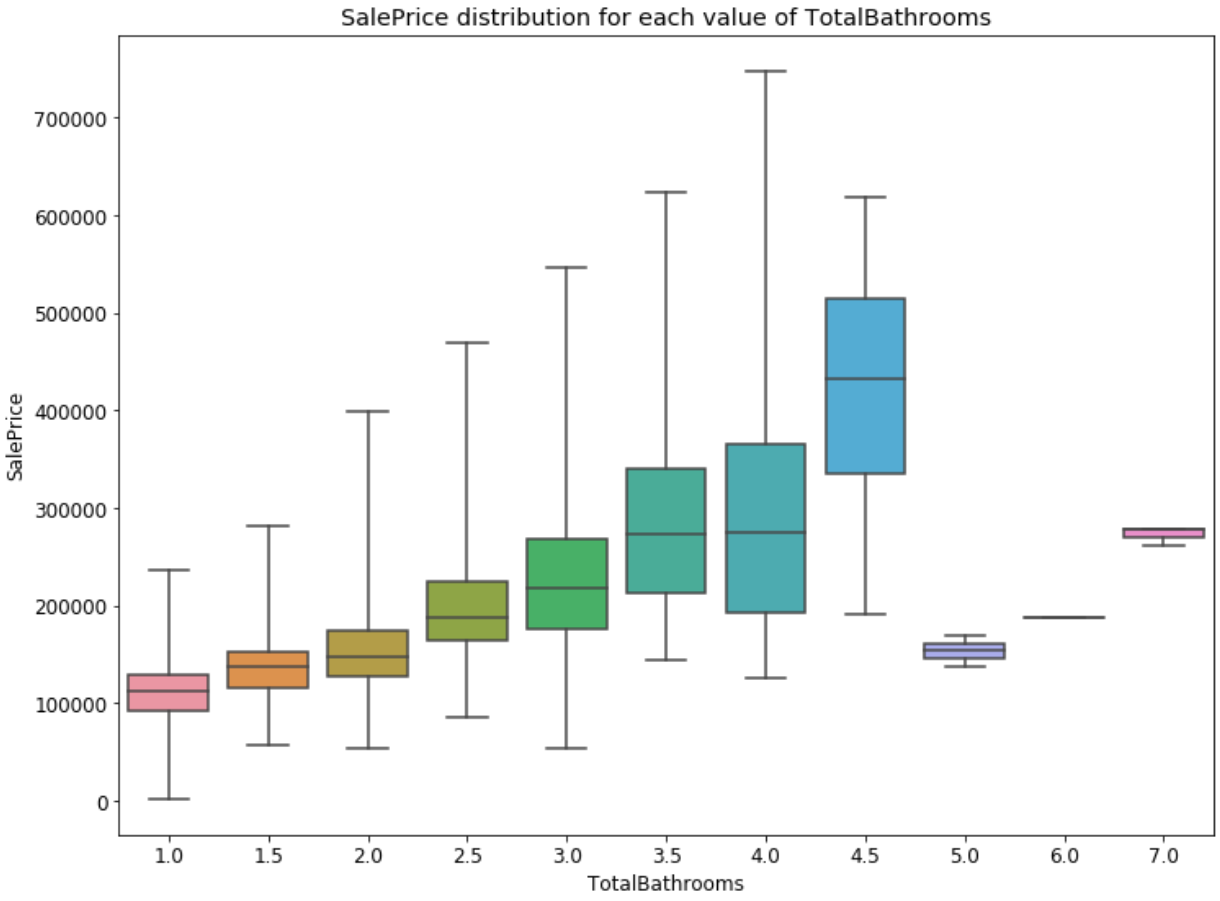
In [77]:
```
ok.grade("q4");
```

```
/Users/sjk/datascience/COSE471-hw3(1)/tests/q4.py: All tests passed!
```

Question 5

Create a visualization that clearly and succintly shows that `TotalBathrooms` is associated with `SalePrice`. Your visualization should avoid overplotting.

In [78]:
```
-------
alBathrooms', y='SalePrice', data=training_data, whis=5).set_title('SalePric
-------
```



Part 3: Modeling

We've reached the point where we can specify a model. But first, we will load a fresh copy of the data, just in case our code above produced any undesired side-effects. Run the cell below to store a fresh copy of the data from `ames_train.csv` in a dataframe named `full_data`. We will also store the number of rows in `full_data` in the variable `full_data_len`.

In [79]:
```
# Load a fresh copy of the data and get its length
full_data = pd.read_csv("./data/ames_train.csv")
full_data_len = len(full_data)
full_data.head()
```

Out[79]:

	Order	PID	MS_SubClass	MS_Zoning	Lot_Frontage	Lot_Area	Street	Alley	Lot_Shape
0	1	526301100	20	RL	141.0	31770	Pave	NaN	IR1
1	2	526350040	20	RH	80.0	11622	Pave	NaN	Reg
2	3	526351010	20	RL	81.0	14267	Pave	NaN	IR1
3	4	526353030	20	RL	93.0	11160	Pave	NaN	Reg
4	5	527105010	60	RL	74.0	13830	Pave	NaN	IR1

5 rows × 82 columns

Question 6

Now, let's split the data set into a training set and test set. We will use the training set to fit our model's parameters, and we will use the test set to estimate how well our model will perform on unseen data drawn from the same distribution. If we used all the data to fit our model, we would not have a way to estimate model performance on unseen data.

"Don't we already have a test set in `ames_test.csv` ?" you might wonder. The sale prices for `ames_test.csv` aren't provided, so we're constructing our own test set for which we know the outputs.

In the cell below, split the data in `full_data` into two DataFrames named `train` and `test` . Let `train` contain 80% of the data, and let `test` contain the remaining 20% of the data.

To do this, first create two NumPy arrays named `train_indices` and `test_indices` . `train_indices` should contain a *random* 80% of the indices in `full_data` , and `test_indices` should contain the remaining 20% of the indices. Then, use these arrays to index into `full_data` to create your final `train` and `test` DataFrames.

The provided tests check that you not only answered correctly, but ended up with the exact same train/test split as our reference implementation. Later testing is easier this way.

In [80]:
```
# This makes the train-test split in this section reproducible across differ
# of the notebook. You do not need this line to run train_test_split in gene
np.random.seed(1337)
shuffled_indices = np.random.permutation(full_data_len)

# Set train_indices to the first 80% of shuffled_indices and and test_indice
# BEGIN YOUR CODE
# ----------------------
train_indices = shuffled_indices[:int(full_data_len * 0.8)]
test_indices = shuffled_indices[int(full_data_len * 0.8):]
# ----------------------
# END YOUR CODE

# Create train and test` by indexing into `full_data` using
# `train_indices` and `test_indices`
# BEGIN YOUR CODE
# ----------------------
train = full_data.iloc[train_indices]
test = full_data.iloc[test_indices]
# ----------------------
# END YOUR CODE
test
```

Out[80]:

	Order	PID	MS_SubClass	MS_Zoning	Lot_Frontage	Lot_Area	Street	Alley	Lot_Shap
800	1202	534251280	60	RL	NaN	9130	Pave	NaN	Re
512	751	903429080	70	RM	50.0	2500	Pave	Pave	Re
1715	2535	534201260	20	RL	78.0	9360	Pave	NaN	Re
154	217	905101300	90	RL	72.0	10773	Pave	NaN	Re
1276	1888	534278150	20	RL	NaN	14357	Pave	NaN	IR
1303	1937	535325280	80	RL	60.0	7134	Pave	NaN	Re
1450	2150	907262020	60	RL	65.0	8158	Pave	NaN	Re
632	938	909475040	20	RL	NaN	17597	Pave	NaN	Re
999	1481	907420080	60	RL	63.0	8199	Pave	NaN	Re
336	473	528228455	120	RL	43.0	3182	Pave	NaN	Re
1137	1679	527451020	160	RM	24.0	2016	Pave	NaN	Re
980	1454	907250020	20	RL	75.0	9742	Pave	NaN	Re
1884	2765	906426090	20	RL	NaN	36500	Pave	NaN	IR
1528	2259	916326090	20	RL	149.0	19958	Pave	NaN	Re
1032	1524	909251080	70	RL	66.0	8969	Pave	NaN	Re
844	1260	535383100	190	RL	60.0	10800	Pave	Grvl	Re
1296	1927	535180030	20	RL	72.0	10152	Pave	NaN	Re
595	879	907290210	120	RM	NaN	4435	Pave	NaN	Re
1508	2231	909475230	20	RL	70.0	18044	Pave	NaN	IR

	Order	PID	MS_SubClass	MS_Zoning	Lot_Frontage	Lot_Area	Street	Alley	Lot_Shap
480	695	902103120	90	RM	57.0	10307	Pave	Grvl	Re
569	834	906426210	60	RL	NaN	16698	Pave	NaN	IF
1149	1702	528118050	20	RL	59.0	17169	Pave	NaN	IF
1621	2394	528142060	60	RL	82.0	10672	Pave	NaN	IF
771	1152	532354150	20	RL	75.0	8100	Pave	NaN	Re
421	615	534450150	30	RL	50.0	5330	Pave	NaN	Re
216	310	914467040	60	RL	85.0	11050	Pave	NaN	Re
146	201	903234050	30	RM	51.0	6120	Pave	NaN	Re
79	104	533223100	160	FV	NaN	2403	Pave	NaN	IF
1868	2742	905452140	50	RL	75.0	9525	Pave	NaN	Re
1322	1968	535457040	90	RL	80.0	8000	Pave	NaN	Re
...	...	...	...	...	...	...	...	...	
60	79	531452050	120	RL	50.0	7175	Pave	NaN	Re
1857	2728	905225080	50	RL	81.0	15593	Pave	NaN	Re
1227	1818	531477040	90	RH	60.0	8400	Pave	NaN	Re
1896	2782	907200170	80	RL	55.0	10780	Pave	NaN	IF
1641	2427	528228550	120	RL	43.0	3010	Pave	NaN	Re
962	1431	906476030	60	RL	79.0	12798	Pave	NaN	IF
370	535	531363030	20	RL	63.0	7500	Pave	NaN	Re
1046	1543	909451020	160	RM	24.0	1879	Pave	NaN	Re
774	1156	532477030	20	RL	95.0	19508	Pave	NaN	Re
1117	1653	527328050	20	RL	79.0	11850	Pave	NaN	Re
795	1193	534201240	60	RL	73.0	8814	Pave	NaN	Re
1153	1709	528150120	60	RL	99.0	12099	Pave	NaN	IF
664	987	923400110	60	RL	62.0	10429	Pave	NaN	Re
1047	1546	910201130	50	RM	60.0	6000	Pave	NaN	Re
1370	2032	903451110	45	RM	57.0	7449	Pave	Grvl	Re
438	642	535302120	90	RL	76.0	9482	Pave	NaN	Re
390	565	533135020	60	RL	NaN	11949	Pave	NaN	Re
265	372	527302175	20	RL	48.0	17043	Pave	NaN	IF
72	95	533208090	160	FV	39.0	3515	Pave	Pave	Re
1108	1637	527212060	60	RL	98.0	12328	Pave	NaN	IF
82	110	534102025	20	FV	80.0	8000	Pave	NaN	Re
1906	2796	907265030	20	RL	NaN	8125	Pave	NaN	Re
346	495	528315090	60	RL	82.0	9430	Pave	NaN	Re

	Order	PID	MS_SubClass	MS_Zoning	Lot_Frontage	Lot_Area	Street	Alley	Lot_Shap
679	1011	527208010	60	RL	101.0	13543	Pave	NaN	IF
1497	2217	909279080	50	RL	NaN	11275	Pave	NaN	IF
1191	1766	528344020	60	RL	74.0	11002	Pave	NaN	IF
1256	1859	533254100	80	RL	80.0	9600	Pave	NaN	Re
860	1293	902109110	50	RM	63.0	11426	Pave	NaN	Re
189	270	907290240	120	RM	NaN	4426	Pave	NaN	Re
1175	1743	528228275	120	RL	53.0	3922	Pave	NaN	Re

400 rows × 82 columns

In [81]:
```
ok.grade("q6");
```

```
---------------------------------------------------------------------------
AssertionError                            Traceback (most recent call last)
<ipython-input-81-834849d13f88> in <module>()
----> 1 ok.grade("q6");

~/anaconda3/envs/data100/lib/python3.6/site-packages/client/api/notebook.py in grade(self, question, global_env)
     56             # inspect trick to pass in its parents' global env.
     57             global_env = inspect.currentframe().f_back.f_globals
---> 58         result = grade(path, global_env)
     59         # We display the output if we're in IPython.
     60         # This keeps backwards compatibility with okpy's grade method

~/anaconda3/envs/data100/lib/python3.6/site-packages/okgrade/grader.py in grade(test_file_path, global_env)
     59     Returns a TestResult object.
     60     """
---> 61     tests = parse_ok_test(test_file_path)
     62     if global_env is None:
     63         # Get the global env of our callers - one level below us in the stack

~/anaconda3/envs/data100/lib/python3.6/site-packages/okgrade/grader.py in parse_ok_test(path)
     24
     25     # Do not support point values other than 1
---> 26     assert test_spec.get('points', 1) == 1
     27
     28     test_suite = test_spec['suites'][0]

AssertionError:
```

Reusable Pipeline

Throughout this assignment, you should notice that your data flows through a single processing pipeline several times. From a software engineering perspective, it's best to define functions/methods that can apply the pipeline to any dataset. We will now encapsulate our entire pipeline into a single function `process_data_gm`. gm is shorthand for "guided model". We select a handful of features to use from the many that are available.

In [82]:
```
def select_columns(data, *columns):
    """Select only columns passed as arguments."""
    return data.loc[:, columns]

def process_data_gm(data):
    """Process the data for a guided model."""
    data = remove_outliers(data, 'Gr_Liv_Area', upper=5000)

    # Transform Data, Select Features
    data = add_total_bathrooms(data)
    data = select_columns(data,
                          'SalePrice',
                          'Gr_Liv_Area',
                          'Garage_Area',
                          'TotalBathrooms',
                         )

    # Return predictors and response variables separately
    X = data.drop(['SalePrice'], axis = 1)
    y = data.loc[:, 'SalePrice']

    return X, y
```

Now, we can use `process_data_gm` to clean our data, select features, and add our `TotalBathrooms` feature all in one step! This function also splits our data into `X`, a matrix of features, and `y`, a vector of sale prices.

Run the cell below to feed our training and test data through the pipeline, generating `X_train`, `y_train`, `X_test`, and `y_test`.

In [83]:
```
# Pre-process our training and test data in exactly the same way
# Our functions make this very easy!
X_train, y_train = process_data_gm(train)
X_test, y_test = process_data_gm(test)
```

Fitting Our First Model

We are finally going to fit a model! The model we will fit can be written as follows:

$$\text{SalePrice} = \theta_0 + \theta_1 \cdot \text{Gr\_Liv\_Area} + \theta_2 \cdot \text{Garage\_Area} + \theta_3 \cdot \text{TotalBathrooms}$$

In vector notation, the same equation would be written:

$$y = \theta \cdot x$$

where y is the SalePrice, θ is a vector of all fitted weights, and x contains a 1 for the bias followed by each of the feature values.

Note: Notice that all of our variables are continuous, except for `TotalBathrooms`, which takes on discrete ordered values (0, 0.5, 1, 1.5, ...). In this homework, we'll treat `TotalBathrooms` as a continuous quantitative variable in our model, but this might not be the best choice. The next homework may revisit the issue.

Question 7a

We will use a `sklearn.linear_model.LinearRegression` (https://scikit-learn.org/stable/modules/generated/sklearn.linear_model.LinearRegression.html) object as our linear model. In the cell below, create a `LinearRegression` object and name it `linear_model`.

Hint: See the `fit_intercept` parameter and make sure it is set appropriately. The intercept of our model corresponds to θ_0 in the equation above.

The provided tests check that you answered correctly, so that future analyses are not corrupted by a mistake.

In [84]:
```
from sklearn import linear_model as lm

# BEGIN YOUR CODE
# ----------------------
linear_model = lm.LinearRegression(fit_intercept=True)
# ----------------------
# END YOUR CODE
```

In [85]:
```
ok.grade("q7a");
```

```
/Users/sjk/datascience/COSE471-hw3(1)/tests/q7a.py: All tests passed!
```

Question 7b

Now, remove the commenting and fill in the ellipses `...` below with `X_train`, `y_train`, `X_test`, or `y_test`.

With the ellipses filled in correctly, the code below should fit our linear model to the training data and generate the predicted sale prices for both the training and test datasets.

The provided tests check that you answered correctly, so that future analyses are not corrupted by a mistake.

In [86]:
```
# Uncomment the lines below and fill in the ... with X_train, y_train, X_tes
# BEGIN YOUR CODE
# ------------------------
linear_model.fit(X_train, y_train)
y_fitted = linear_model.predict(X_train)
y_predicted = linear_model.predict(X_test)
# ------------------------
# END YOUR CODE
```

In [87]:
```
ok.grade("q7b");
```

```
---------------------------------------------------------------------------
--
AssertionError                            Traceback (most recent call las
t)
<ipython-input-87-930562b39ab5> in <module>()
----> 1 ok.grade("q7b");

~/anaconda3/envs/data100/lib/python3.6/site-packages/client/api/notebook.
py in grade(self, question, global_env)
     56             # inspect trick to pass in its parents' global env.
     57             global_env = inspect.currentframe().f_back.f_globals
---> 58         result = grade(path, global_env)
     59         # We display the output if we're in IPython.
     60         # This keeps backwards compatibility with okpy's grade me
thod

~/anaconda3/envs/data100/lib/python3.6/site-packages/okgrade/grader.py in
grade(test_file_path, global_env)
     59     Returns a TestResult object.
     60     """
---> 61     tests = parse_ok_test(test_file_path)
     62     if global_env is None:
     63         # Get the global env of our callers - one level below us
 in the stack

~/anaconda3/envs/data100/lib/python3.6/site-packages/okgrade/grader.py in
parse_ok_test(path)
     24
     25     # Do not support point values other than 1
---> 26     assert test_spec.get('points', 1) == 1
     27
     28     test_suite = test_spec['suites'][0]

AssertionError:
```

Question 8a

Is our linear model any good at predicting house prices? Let's measure the quality of our model by calculating the Root-Mean-Square Error (RMSE) between our predicted house prices and the true prices stored in `SalePrice`.

$$\text{RMSE} = \sqrt{\frac{\sum_{\text{houses in test set}} (\text{actual price of house} - \text{predicted price of house})^2}{\text{\# of houses in data set}}}$$

In the cell below, write a function named `rmse` that calculates the RMSE of a model.

Hint: Make sure you are taking advantage of vectorized code. This question can be answered without any `for` statements.

The provided tests check that you answered correctly, so that future analyses are not corrupted by a mistake.

In [88]:
```
def rmse(actual, predicted):
    """
    Calculates RMSE from actual and predicted values
    Input:
      actual (1D array): vector of actual values
      predicted (1D array): vector of predicted/fitted values
    Output:
      a float, the root-mean square error
    """
    # BEGIN YOUR CODE
    # ----------------------
    return np.sqrt(np.mean((actual - predicted)**2))
    # ----------------------
    # END YOUR CODE
```

In [89]:
```
ok.grade("q8a");
```

```
/Users/sjk/datascience/COSE471-hw3(1)/tests/q8a.py: All tests passed!
```

Question 8b

Now use your `rmse` function to calculate the training error and test error in the cell below.

The provided tests for this question do not confirm that you have answered correctly; only that you have assigned each variable to a non-negative number.

In [90]:
```
# BEGIN YOUR CODE
# ----------------------
training_error = rmse(y_fitted, y_train)
test_error = rmse(y_predicted, y_test)
# ----------------------
# END YOUR CODE
(training_error, test_error)
```

Out[90]:
```
(46710.597505875856, 46146.642656826247)
```

In [91]:
```
ok.grade("q8b");
```

```
/Users/sjk/datascience/COSE471-hw3(1)/tests/q8b.py: All tests passed!
```

Question 8c

How much does including `TotalBathrooms` as a predictor reduce the RMSE of the model on the test set? That is, what's the difference between the RSME of a model that only includes `Gr_Liv_Area` and `Garage_Area` versus one that includes all three predictors?

The provided tests for this question do not confirm that you have answered correctly; only that you have assigned the answer variable to a non-negative number.

In [92]:
```
# BEGIN YOUR CODE
# ----------------------
...
test_error_no_bath =
# ----------------------
# END YOUR CODE

test_error_difference = test_error_no_bath - test_error
test_error_difference
```

```
  File "<ipython-input-92-df1df3b559c4>", line 4
    test_error_no_bath =
                        ^
SyntaxError: invalid syntax
```

In [93]:
```
ok.grade("q8c");
```

```
---------------------------------------------------------------------
--
AssertionError                            Traceback (most recent call las
t)
<ipython-input-93-71339715db32> in <module>()
----> 1 ok.grade("q8c");

~/anaconda3/envs/data100/lib/python3.6/site-packages/client/api/notebook.
py in grade(self, question, global_env)
     56             # inspect trick to pass in its parents' global env.
     57             global_env = inspect.currentframe().f_back.f_globals
---> 58         result = grade(path, global_env)
     59         # We display the output if we're in IPython.
     60         # This keeps backwards compatibility with okpy's grade me
thod

~/anaconda3/envs/data100/lib/python3.6/site-packages/okgrade/grader.py in
grade(test_file_path, global_env)
     59     Returns a TestResult object.
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 in the stack

~/anaconda3/envs/data100/lib/python3.6/site-packages/okgrade/grader.py in
parse_ok_test(path)
     24
     25     # Do not support point values other than 1
---> 26     assert test_spec.get('points', 1) == 1
     27
     28     test_suite = test_spec['suites'][0]

AssertionError:
```
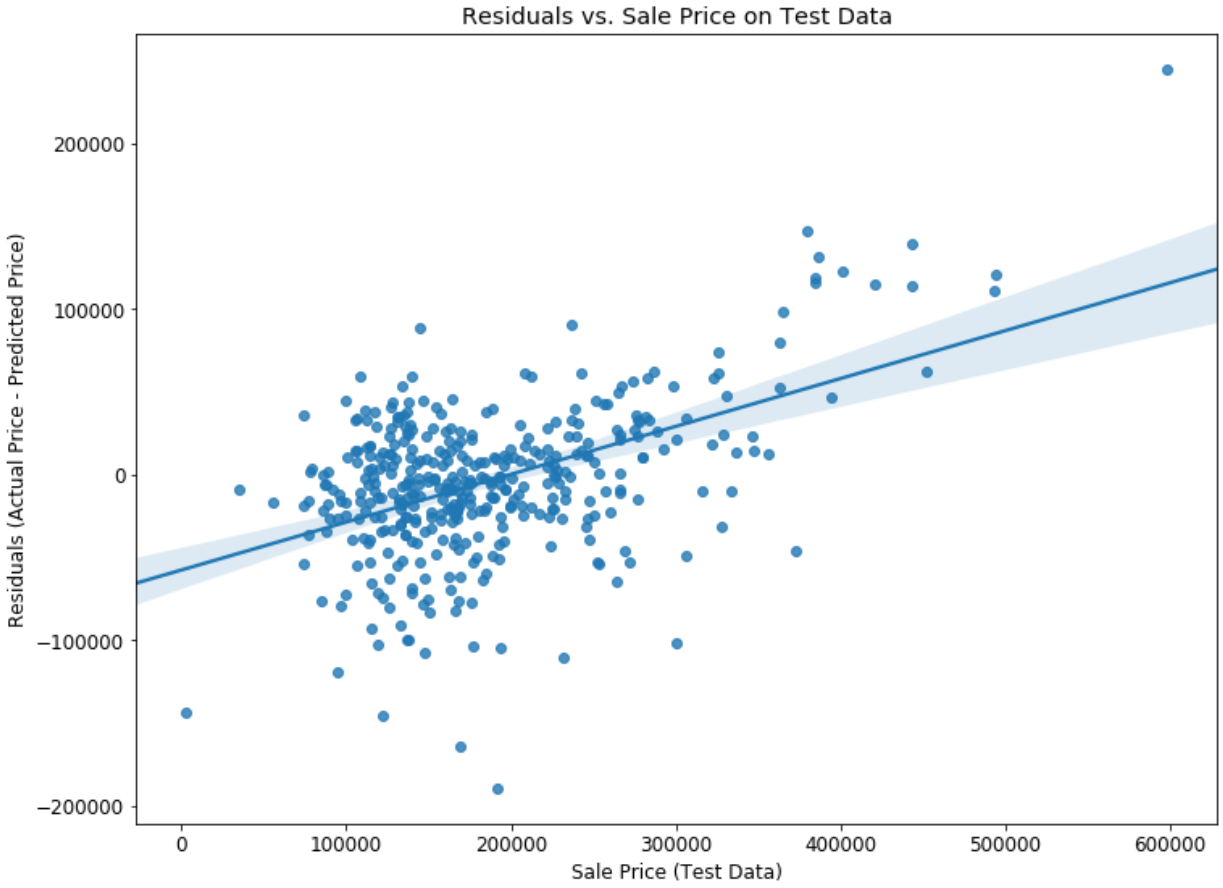

Residual Plots

One way of understanding the performance (and appropriateness) of a model is through a residual plot. Run the cell below to plot the actual sale prices against the residuals of the model for the test data.

In [94]:
```
residuals = y_test - y_predicted
ax = sns.regplot(y_test, residuals)
ax.set_xlabel('Sale Price (Test Data)')
ax.set_ylabel('Residuals (Actual Price - Predicted Price)')
ax.set_title("Residuals vs. Sale Price on Test Data");
```



Ideally, we would see a horizontal line of points at 0 (perfect prediction!). The next best thing would be a homogenous set of points centered at 0.

But alas, our simple model is probably too simple. The most expensive homes are systematically more expensive than our prediction.

Question 8d

What changes could you make to your linear model to improve its accuracy and lower the test error? Suggest at least two things you could try in the cell below, and carefully explain how each change could potentially improve your model's accuracy.

Answer: `We could colorcode and group the houses by their locations to see if there is any relation in that. Also we could find more factors that could contribute to pricier houses by collecting more data about the houses`

Congratulations! You have completed HW3.

Make sure you have run all cells in your notebook in order before running the cell below, so that all images/graphs appear in the output.,

Please save before submitting!

Please generate pdf as follows and submit it to Gradescope.

File > Print Preview > Print > Save as pdf