Good Enough?

- Chess:
 - branching factor b≈35
 - -game length m≈100
 - -search space $b^{m/2} \approx 35^{50} \approx 10^{77}$
- The Universe:
 - number of atoms ≈ 10^{78}
 - $-age ≈ 10^{18} seconds$
 - -10^8 moves/sec x 10^{78} x 10^{18} = 10^{104}

The universe

- can we?

can play chess

Cutting off Search

MinimaxCutoff is identical to MinimaxValue except

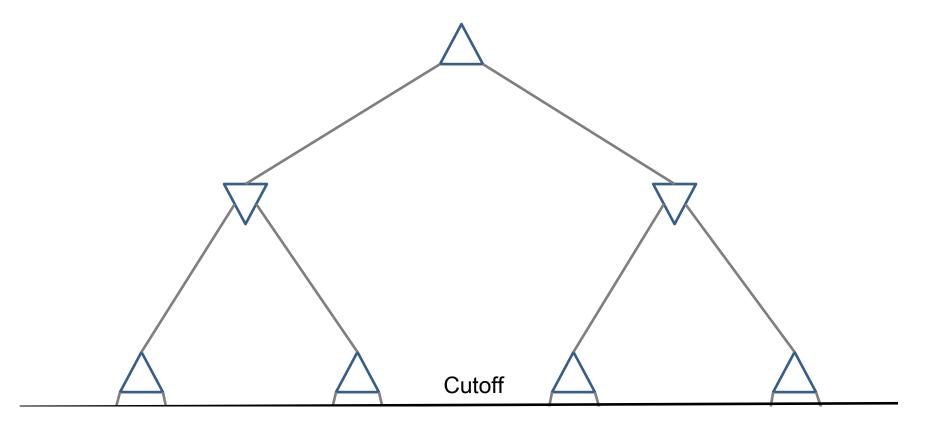
- 1. Terminal? is replaced by Cutoff?
- 2. Utility is replaced by Eval

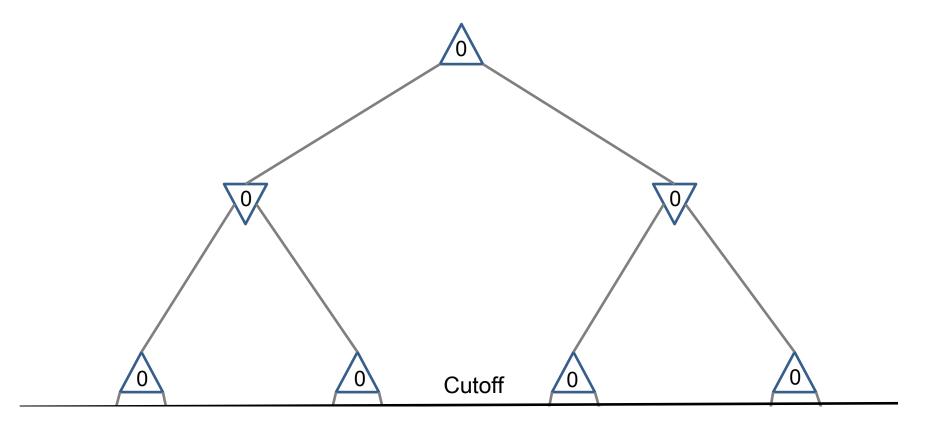
Does it work in practice?

$$b^{m} = 10^{6}, b=35 \rightarrow m=4$$

4-ply lookahead is a hopeless chess player!

- 4-ply ≈ human novice
- 8-ply ≈ typical PC, human master
- 12-ply ≈ Deep Blue, Kasparov



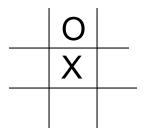


Evaluation Functions _____ Tic Tac Toe

- Let p be a position in the game
- Define the utility function f(p) by
 - f(p) =
 - largest positive number if p is a win for computer
 - smallest negative number if p is a win for opponent
 - RCDC RCDO
 - where RCDC is number of rows, columns and diagonals in which computer could still win
 - and RCDO is number of rows, columns and diagonals in which opponent could still win.

Sample Evaluations

• X = Computer; O = Opponent



X O
rows
cols
diags

X O
rows
cols
diags

Evaluation functions

For chess/checkers, typically linear weighted sum of features

$$Eval(s) = w_1 f_1(s) + w_2 f_2(s) + ... + w_m f_m(s)$$

e.g., $w_1 = 9$ with

 $f_1(s) = (number of white queens) - (number of black queens), etc.$

Example: Samuel's Checker-Playing Program

It uses a linear evaluation function

$$f(n) = w_1 f_1(n) + w_2 f_2(n) + ... + w_m f_m(n)$$

For example: f = 6K + 4M + U

- K = King Advantage
- M = Man Advantage
- U = Undenied Mobility Advantage (number of moves that Max where Min has no jump moves)

Samuel's Checker Player

In learning mode

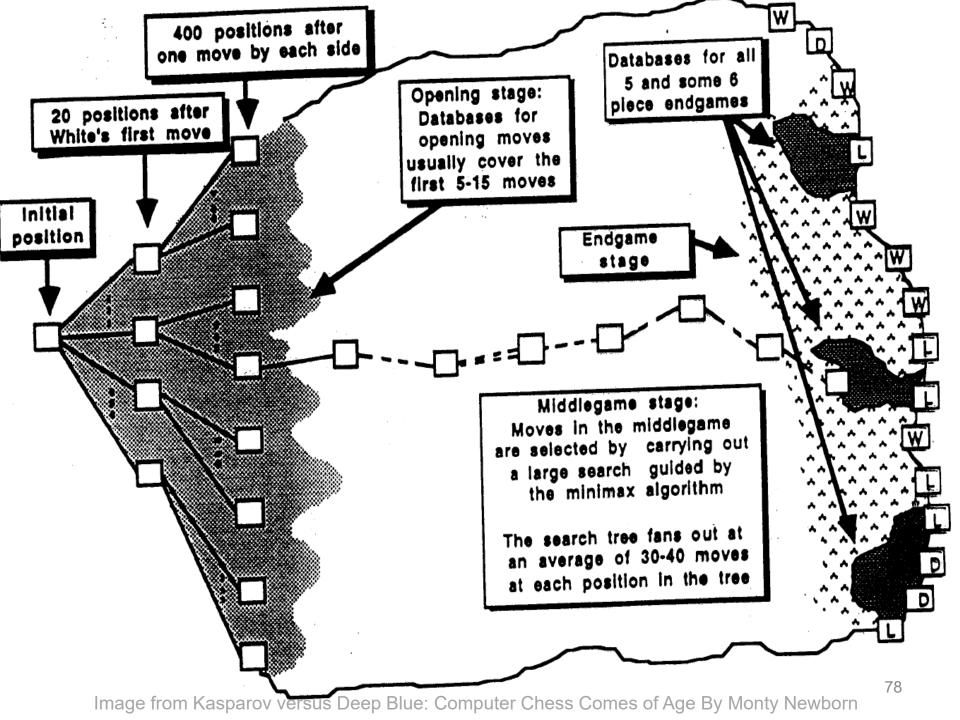
- Computer acts as 2 players: A and B
- A adjusts its coefficients after every move
- B uses the static utility function
- If A wins, its function is given to B

Samuel's Checker Player

How does A change its function?
 Coefficent replacement

Chess: Rich history of cumulative ideas

- Minimax search, evaluation function learning (1950).
- Alpha-Beta search (1966).
- Transposition Tables (1967).
- Iterative deepening DFS (1975).
- End game data bases ,singular extensions(1977, 1980)
- Parallel search and evaluation(1983, 1985)
- Circuitry (1987)

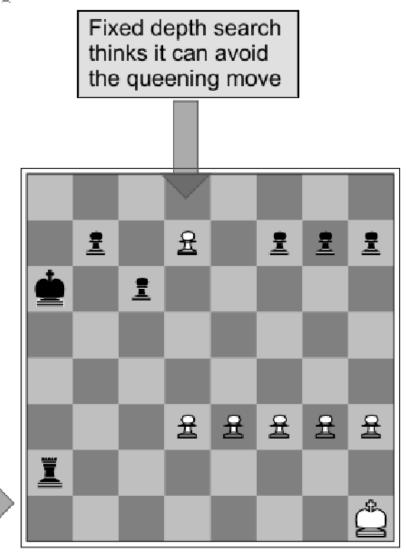


Problem with fixed depth Searches

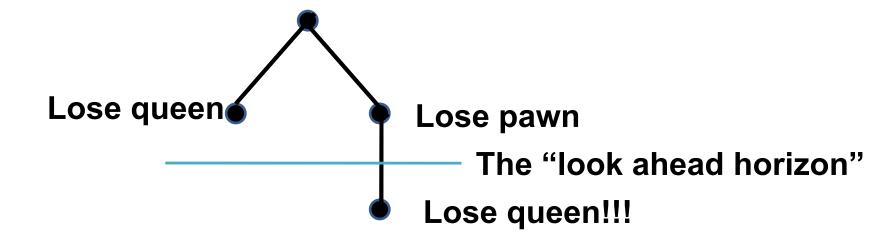
if we only it may be catastroph sequence make any

also works (good mo

Black can give many consecutive checks before white escapes



Problems with a fixed ply: The Horizon Effect



- Inevitable losses are postponed
- Unachievable goals appear achievable
- Short-term gains mask unavoidable consequences (traps)

Solutions

- How to counter the horizon effect
 - Feedover
 - Do not cut off search at non-quiescent board positions (dynamic positions)
 - Example, king in danger
 - Keep searching down that path until reach quiescent (stable) nodes
 - Secondary Search
 - Search further down selected path to ensure this is the best move

Quiescence Search

This involves searching past the terminal search nodes (depth of 0) and testing all the non-quiescent or 'violent' moves until the situation becomes calm, and only then apply the evaluator.

Enables programs to detect long capture sequences and calculate whether or not they are worth initiating.

Expand searches to avoid evaluating a position where tactical disruption is in progress.

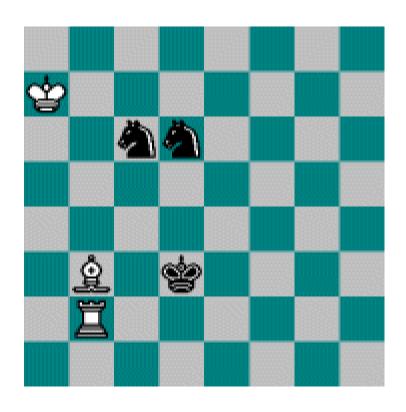
Additional Refinements

- Probabilistic Cut: cut branches probabilistically based on shallow search and global depth-level statistics (forward pruning)
- Openings/Endgames: for some parts of the game (especially initial and end moves), keep a catalog of best moves to make.
- Singular Extensions: find obviously good moves and try them at cutoff.

End-Game Databases

- Ken Thompson all 5 piece end-games
- Lewis Stiller all 6 piece end-games
 - Refuted common chess wisdom: many positions thought to be ties were really forced wins -- 90% for white
 - Is perfect chess a win for white?

The MONSTER



White wins in 255 moves (Stiller, 1991)

Deterministic Games in Practice

- Checkers: Chinook ended 40-year-reign of human world champion Marion Tinsley in 1994. Used a precomputed endgame database defining perfect play for all positions involving 8 or fewer pieces on the board, a total of 444 billion positions. Checkers is now solved!
- Chess: Deep Blue defeated human world champion Garry Kasparov in a six-game match in 1997. Deep Blue searches 200 million positions per second, uses very sophisticated evaluation, and undisclosed methods for extending some lines of search up to 40 ply. Current programs are even better, if less historic!
- Othello: human champions refuse to compete against computers, who are too good.
- Go: until recently, human champions refused to compete against computers, who were too bad. In Go, b > 300, so most programs use pattern knowledge bases to suggest plausible moves, along with aggressive pruning. In 2016, DeepMind's AlphaGo defeated Lee Sedol 4-1 to end the human reign.

Game of Go

human champions refused to compete against computers, because software used to be too bad.

	Chess	Go
Size of board	8 x 8	19 x 19
Average no. of moves per game	100	300
Avg branching factor per turn	35	235
Additional complexity		Players can pass

AlphaGo (2016)

- Combination of
 - Deep Neural Networks
 - Monte Carlo Tree Search

More details later.

Other Games

deterministic

chance

perfect information

chess, checkers, go, othello

backgammon, monopoly

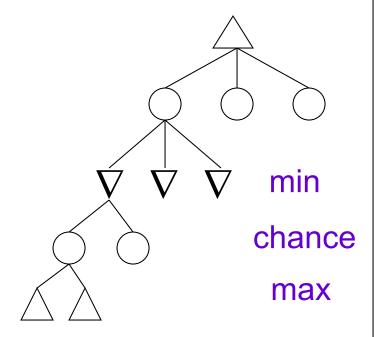
imperfect information

stratego

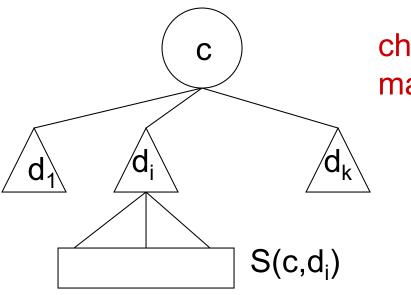
bridge, poker, scrabble

Games of Chance

- What about games that involve chance, such as
 - rolling dice
 - picking a card
- Use three kinds of nodes:
 - max nodes
 - min nodes
 - chance nodes



Games of Chance Expectiminimax



chance node with max children

```
expectimax(c) = \sum P(d_i) max(backed-up-value(s))
i s in S(c,d_i)
```

expectimin(c') =
$$\sum P(d_i)$$
 min(backed-up-value(s))
i s in S(c,d_i)

Example Tree with Chance

max

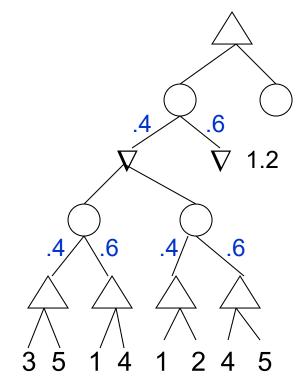
chance

min

chance

max

leaf



Complexity

Instead of O(b^m), it is O(b^mn^m) where n is the number of chance outcomes.

 Since the complexity is higher (both time and space), we cannot search as deeply.

Pruning algorithms may be applied.

Imperfect Information

E.g. card games, where opponents' initial cards unknown



- Idea: For all deals consistent with what you can see
 - compute the minimax value of available actions for each of possible deals
 - -compute the expected value over all deals

Status of Al Game Players

Tic Tac Toe

Tied for best player in world

Othello

- Computer better than any human
- Human champions now refuse to play computer

Scrabble

Maven beat world champions Joel
 Sherman and Matt Graham

Backgammon

 1992, <u>Tesauro</u> combines 3-ply search & neural networks (with 160 hidden units) yielding top-3 player

Bridge

Gib ranked among top players in the world

Poker

2015, Heads-up limit hold'em poker is solved

Checkers

 1994, <u>Chinook</u> ended 40-year reign of human champion Marion Tinsley

Chess

- 1997, <u>Deep Blue</u> beat human champion Gary Kasparov in sixgame match
- Deep Blue searches 200M positions/second, up to 40 ply
- Now looking at other applications (molecular dynamics, drug synthesis)

Go

 2016, Deepmind's AlphaGo defeated Lee Sedol & 2017 defeated Ke Jie

Summary

Games are fun to work on!

They illustrate several important points about AI.

 Game playing programs have shown the world what Al can do.