

5.12 Using the Fact that S is a state Function to Determine the Dependence of S on V and T .

- ds is an exact differential... $ds = \frac{1}{T} du + \frac{p}{T} dv$
because $1/T$ and p/T are > 0 the entropy of a system increases with the internal energy at constant V , increases with volume at constant internal energy.
- ds can be expressed in terms of dt and dv as

$$ds = \frac{C_V}{T} dt + \frac{p}{K} dv$$

$$\Delta S = \int_{T_i}^{T_f} \frac{C_V}{T} dt + \int_{V_i}^{V_f} \frac{p}{K} dv$$

this applies to a single-phase system $T_i, V_i \rightarrow T_f, V_f$ (no phase change occurs or chemical reaction occurs in system)

5.13 The Dependence of S on T and P

- since normal reactions carried in constant pressure instead of constant vol, we need know how S varies with T and P

$$ds = \left(\frac{\partial S}{\partial T} \right)_P dT + \left(\frac{\partial S}{\partial P} \right)_T dP$$

- S is a monotonically increasing function of temp.

$$\left(\frac{\partial S}{\partial P} \right)_T = - \left(\frac{\partial V}{\partial T} \right)_P = -V\beta$$

$$\Delta S = \int_{T_i}^{T_f} \frac{C_P}{T} dT - \int_{P_i}^{P_f} V\beta dP$$

- this applies for single-phase system of pure liquid, solid, gas that goes from $T_i, P_i \rightarrow T_f, P_f$ w/ no phase change or chemical reaction in system.