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5.12 Using the fact that S is a state function to determine the dependence of S on V and T

$$dS = \left(\frac{\partial S}{\partial T} \right)_V dT + \left(\frac{\partial S}{\partial V} \right)_T dV$$

S = entropy T = temperature
 V = volume

where $\left(\frac{\partial S}{\partial T} \right)_V = \frac{C_V}{T}$ and $\left(\frac{\partial S}{\partial V} \right)_T = \frac{1}{T} \left[P + \left(\frac{\partial U}{\partial V} \right)_T \right] = \left(\frac{\partial P}{\partial T} \right)_V = \frac{\beta}{\alpha}$

C_V = heat capacity (constant volume) P = pressure U = energy

The second law of thermodynamics is applied here.

5.13 The Dependence of S on T and P

$$dS = \left(\frac{\partial S}{\partial T} \right)_P dT + \left(\frac{\partial S}{\partial P} \right)_T dP = \frac{C_P}{T} dT - \frac{V\beta}{\alpha} dP$$

C_P = heat capacity (constant pressure)

The second law of thermodynamics is applied here.

6.1 The Gibbs Energy and the Helmholtz Energy

$$\Delta G = \Delta H - T\Delta S$$

G = Gibbs energy H = enthalpy

$$\Delta A = \Delta U - T\Delta S$$

A = Helmholtz energy

Both equations involve reactions

The second law of thermodynamics is applied here.

5.2 The Differential Forms of U, H, A, G

$$H = U + PV$$

$$A = U - TS$$

$$G = H - TS$$

$$dU = TdS - PdV$$

$$dH = TdS + VdP$$

$$dA = -SdT - PdV$$

$$dG = -SdT + VdP$$

$$\left(\frac{\partial U}{\partial S}\right)_V = T$$

$$\left(\frac{\partial U}{\partial V}\right)_S = -P$$

$$\left(\frac{\partial A}{\partial V}\right)_T = -P$$

$$\left(\frac{\partial A}{\partial T}\right)_V = -S$$

$$\left(\frac{\partial H}{\partial S}\right)_P = T$$

$$\left(\frac{\partial H}{\partial P}\right)_S = V$$

$$\left(\frac{\partial G}{\partial T}\right)_P = -S$$

$$\left(\frac{\partial G}{\partial P}\right)_T = V$$

The second law of thermodynamics is applied here.

6.3 The Dependence of the Gibbs and Helmholtz Energies on P, V and T

$$\left(\frac{\partial A}{\partial T}\right)_V = -S$$

$$\left(\frac{\partial A}{\partial V}\right)_T = -P$$

$$\left(\frac{\partial G}{\partial T}\right)_P = -S$$

$$\left(\frac{\partial G}{\partial P}\right)_T = V$$

Gibbs-Helmholtz equation $\frac{d\left(\frac{G}{T}\right)}{dT} = -\frac{H}{T^2}$

$$\left(\frac{\partial(G/T)}{\partial(1/T)}\right)_P = H$$

The second law of thermodynamics is applied here.

Reading HW 6

Kevin Marry

$$\frac{q_{ab}}{T_h} + \frac{q_{cd}}{T_c} = \int \frac{dq_{rev}}{T} = 0$$

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$$\int \frac{dq_{rev}}{T} = \int \frac{dq_{rev}}{T} = \Delta S$$

- (2) $ab \rightarrow q^+$
 $bc \rightarrow q=0$
 $cd \rightarrow q^-$
 $ad \rightarrow q=0$

$$q_{ab} = -q_{cd}$$

$$\Delta U=0, \Delta H=0, \Delta S=0$$

(b) $T_{hot} V_b$

This occurs at step ab.

(c) $w_{cycle} = -(q_{ab} + q_{cd})$

The total work is 0.

(d) $\epsilon = -\left(\frac{w_{cycle}}{q_{ab}}\right)$

The efficiency has to be less than 1 because a cyclic process can't convert heat to work with 100% efficiency.

(3) $\left(\frac{\partial S}{\partial T}\right)_P = \frac{C_p}{T}$

$$\left(\frac{\partial S}{\partial P}\right)_T = -V\beta$$

(b) $dS = \frac{C_p}{T} dT - V\beta dP$

(4) $\Delta H_{rxn}^{\circ} = (-1364 \text{ kJ/mol}) + (-278 \text{ kJ/mol}) + (-394 \text{ kJ/mol}) - (-1273 \text{ kJ/mol}) = -763 \text{ kJ/mol}$

$$\Delta S_{rxn}^{\circ} = (192 \text{ J/mol K}) + (161 \text{ J/mol K}) + (213 \text{ J/mol K}) - (209 \text{ J/mol K}) = 357 \text{ J/mol K}$$

$$\Delta S_{sur} = -\left(\frac{-763 \text{ kJ/mol}}{298 \text{ K}}\right) \approx 2.56 \text{ kJ/mol K}$$

$$\Delta S_{uni} = 357 \text{ J/mol K} - 2.56 \text{ kJ/mol K} = -2.203 \text{ J/mol K}$$

The reaction isn't spontaneous because in the equation $\Delta G = \Delta H - T\Delta S$, since ΔS is negative, and $|\Delta S| > |\Delta H|$, ΔG will be positive.

$$\textcircled{5} \Delta H = (65.6 \text{ J mol}^{-1} \text{ K}^{-1} + 2.38 \times 10^{-4} \text{ J mol}^{-1} \text{ K}^{-1})(58.3 \text{ K}) - (112 \text{ J mol}^{-1} \text{ K}^{-1})(58.3 \text{ K}) \approx -1.4 \text{ kJ/mol}$$

$$\Delta S = \frac{-1.4 \text{ kJ/mol}}{78.3 \text{ K}} \approx -17.8 \text{ J/mol K}$$

$$\textcircled{6} S_m(70 \text{ K}) = 0 + \int_0^{23.66} 0.83 dT + \frac{93.8 \text{ J/mol}}{23.66 \text{ K}} + \int_{23.66}^{43.76} 0.19 dT + \frac{743 \text{ J/mol}}{93.76 \text{ K}} + \int_{43.76}^{54.39} -0.20 dT + \frac{4450 \text{ J/mol}}{54.39 \text{ K}} + \int_{54.39}^{90.2} -0.6 dT + \frac{6815 \text{ J/mol}}{35.81 \text{ K}} + \int_{90.2}^{70} 0.5 dT = 282.8 \text{ J/mol K}$$

$$S_m(150 \text{ K}) = 322.8 \text{ J/mol K}$$

same process, replace 70 with 150

$$S_m 70 \rightarrow 150 \quad (322.8 \text{ J/mol K} - 282.8 \text{ J/mol K}) = 40 \text{ J/mol K}$$

Questions