

Complex Data - lab1

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Task 1 and Task 2

1. In the first two tasks we compare two different estimators of error variance covariance matrices. We consider unstructured matrices. The first one is REML estimator:

```
## Marginal variance covariance matrix
##      [,1] [,2] [,3] [,4]
## [1,] 25.210 15.466 15.138 22.985
## [2,] 15.466 58.866 44.028 35.965
## [3,] 15.138 44.028 61.657 33.021
## [4,] 22.985 35.965 33.021 85.494
## Standard Deviations: 5.0209 7.6724 7.8522 9.2463
```

The second one is ML estimator:

```
## Marginal variance covariance matrix
##      [,1] [,2] [,3] [,4]
## [1,] 24.706 15.156 14.835 22.526
## [2,] 15.156 57.690 43.149 35.247
## [3,] 14.835 43.149 60.424 32.362
## [4,] 22.526 35.247 32.362 83.786
## Standard Deviations: 4.9705 7.5954 7.7733 9.1535
```

We can see that they don't differ much. Actually the only distinction when considering summaries for both models (first using REML estimators, second one using ML estimators) is the residual standard error (or using notation from exercises - σ_{11}). They are 5.020936 and 4.9704633 respectively. Therefore these variance covariance matrices differ just by multiplication constant.

Task 3 and Task 4

In task 3 and 4 we should choose some assumptions about the structure of the variance covariance matrix from the first task. Unfortunately, at the first glance the matrix doesn't have any structure at all. The only clearly visible thing is that the variances are getting bigger with time. First we try to test if assumptions of equal variance is plausible. From the unstructured variance covariance matrix it does not look so. Therefore we choose parameters `correlation=corSymm(form= 1 | id)`, `weights=varIdent()`. We received following output (to compare the models we use `anova` function, which performs likelihood ratio test):

```
## Marginal variance covariance matrix
##      [,1] [,2] [,3] [,4]
## [1,] 57.154 24.226 22.812 24.093
## [2,] 24.226 57.154 41.108 26.098
## [3,] 22.812 41.108 57.154 23.499
## [4,] 24.093 26.098 23.499 57.154
## Standard Deviations: 7.56 7.56 7.56 7.56

##      Model df      AIC      BIC    logLik    Test  L.Ratio p-value
## lead.cat.new      1 11 1324.325 1360.384 -651.1625
## lead.cat          2 14 1308.337 1354.231 -640.1687 1 vs 2 21.98756 1e-04
```

We can clearly see that p-value was very small - we reject the null hypothesis that the unstructured model explains as much variability as the simpler one.

Next we choose some better assumption: variances are powers of *time* variable. we use parameters: *correlation=corSymm(form= 1 | id), weights=varPower(form = time+1)*:

```
## Marginal variance covariance matrix
##      [,1] [,2] [,3] [,4]
## [1,] 32.233 14.660 18.917 25.833
## [2,] 14.660 44.602 38.422 28.417
## [3,] 18.917 38.422 68.520 32.385
## [4,] 25.833 28.417 32.385 80.222
## Standard Deviations: 5.6774 6.6785 8.2777 8.9567

##           Model df      AIC      BIC    logLik    Test  L.Ratio p-value
## lead.cat.new      1 12 1310.289 1349.627 -643.1447
## lead.cat          2 14 1308.337 1354.231 -640.1687 1 vs 2 5.951938 0.051
```

Here the p-value is just above significance level - we do not reject the null hypothesis and such assumption about the such structure of variance covariance matrix is believable. We further extend this approach just by relaxing the structure. We again use *varPower* but this time the multiplication constants in the powers can be different for different *time.cat* factor levels. We use parameters: *correlation=corSymm(form= 1 | id), weights=varPower(form = time+1 | factor(time.cat))*:

```
## Marginal variance covariance matrix
##      [,1] [,2] [,3] [,4]
## [1,] 25.210 15.465 15.138 22.986
## [2,] 15.465 58.868 44.030 35.967
## [3,] 15.138 44.030 61.658 33.023
## [4,] 22.986 35.967 33.023 85.495
## Standard Deviations: 5.0209 7.6725 7.8523 9.2463

##           Model df      AIC      BIC    logLik    Test      L.Ratio
## lead.cat.new      1 15 1310.337 1359.509 -640.1687
## lead.cat          2 14 1308.337 1354.231 -640.1687 1 vs 2 2.601837e-08
##           p-value
## lead.cat.new
## lead.cat          0.9999
```

Now p-value is very high. We can clearly say that such assumptions about the covariance matrix does not weaken our model.

Due to the problem with seeing a structure in correlations, we checked many different possible correlations structure. However none of them seemed good enough. For example for parameters *correlation=corCompSymm(form= 1 | id), weights=varIdent(form = 1 | factor(time.cat))* we got:

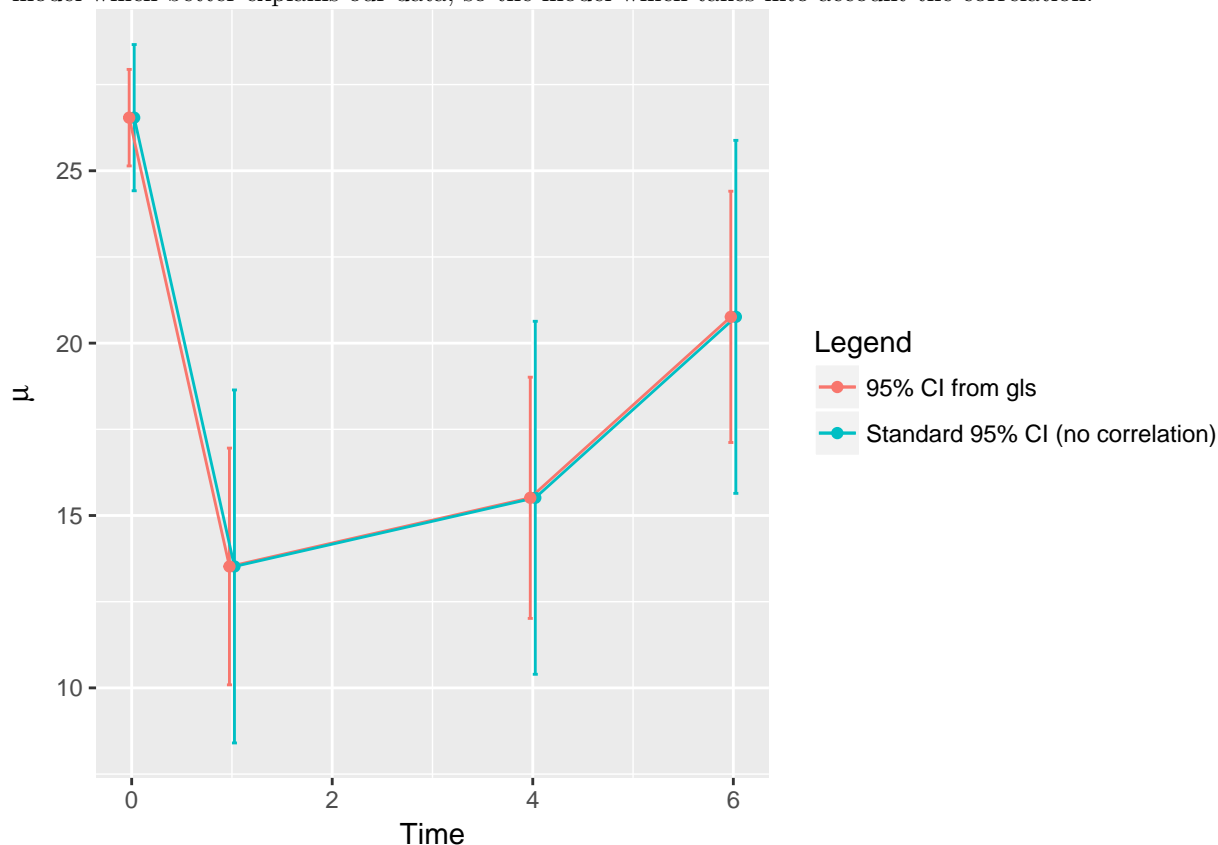
```
## Marginal variance covariance matrix
##      [,1] [,2] [,3] [,4]
## [1,] 26.804 19.321 19.961 23.915
## [2,] 19.321 56.362 28.945 34.678
## [3,] 19.961 28.945 60.157 35.827
## [4,] 23.915 34.678 35.827 86.350
## Standard Deviations: 5.1773 7.5074 7.7561 9.2925

##           Model df      AIC      BIC    logLik    Test  L.Ratio p-value
## lead.cat.new      1  9 1311.470 1340.973 -646.7351
## lead.cat          2 14 1308.337 1354.231 -640.1687 1 vs 2 13.13289 0.0222
```

Therefore we reject the null hypothesis - for this case unstructured model is significantly different than structured one.

Task 5

In this task we compare confidence intervals for means at different time points in two settings: taking into account correlations and the opposite. In this case these confidence intervals are the same as confidence intervals for coefficients β , because our explanatory variables are just levels of a factor *time.cat*. To get them from *gls* and the standard ones, we use *intervals* and *confint* respectively. We expect to get narrower CIs for model which better explains our data, so the model which takes into account the correlation.



Of course in both settings means are the same. However, as expected the CIs for means from *gls* are narrower because model taking into account correlation better explains the variability in our data.

Task 6

In this task we just have to test a contrast $L = (0, 1, -1, 0)$. This means that $H_0 : L^T \beta = 0$. Again we can use *anova* function which takes the model and contrast as parameters:

```
## Denom. DF: 196
## F-test for linear combination(s)
## factor(time.cat)2 factor(time.cat)3
##           1           -1
## numDF  F-value p-value
## 1      1 6.111008 0.0143
```

Here we can see that p-value is lower than 0.05. Therefore we reject the null hypothesis at significance level 0.05 and infer that these means are significantly different.