# A Data Cleaning Approach for Approximately Up-To-Date Results on Stale Materialized Views

### **ABSTRACT**

TODO

# 1. INTRODUCTION

Database systems increasingly use materialization, caching a computed query result, to speed up queries on large datasets [?]. However, as the base tables update, materialized views derived from these tables become increasingly stale. Incrementally keeping the views up-to-date, also called incremental maintenance, has been well studied [?] including a variety of techniques such as batch maintenance [?] and lazy maintenance [?].

Unfortunately, in many desired applications, incremental view maintenance can be very costly. This cost breaks down into two components: applying the view definition to the updates, and then writing the "delta" view to the out-of-date view. These two pieces can be costly in different applications. (1) In distributed environments where the view is partitioned over a cluster, incremental view maintenance often neccesitates communicating the delta view. (2) Systems such as Apache Spark, Cloudera Impala, and Apache Tez [?] offer materialized view support, however, are not optimized for selective updates nor have native support for indices. This can lead to high maintenance costs in applications where the views are derived from joins that are not aligned with the partitioning of the base tables. (3) Base data is often raw requiring pre-processing such as string processing, deserialization, and formatting; all of which can can be expensive to run on a large number of updates. Consequently, a commonly applied approach is to extend the maintenance period and schedule maintenance at less active times eg. nightly; while accepting that in the interim results will be stale. This approach avoids placing an undue bottleneck on updates to the base tables and reduces contention on hot data; however a user querying the system can get results that are arbitrarily stale.

Querying a stale view is similar to problems studied in data cleaning[?]. SampleClean is a query processing frame-

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work that answers aggregate queries on dirty datasets by applying potentially expensive cleaning techniques to just a sample. The results, while approximate, are bounded with respect to the clean data and the system offers a flexible tradeoff between cleaning cost and result accuracy. Similarly, a stale row and an expensive incremental maintenance scheme, mirrors the problem setting studied in SampleClean.

In this paper, we propose a data cleaning approach for approximate, bounded aggregation queries on stale views. Instead of maintaining the entire view, we maintain only a small sample of the view. Then given an aggregation query on this view, from this small sample, we can estimate how the updates affect the query result. We apply this estimate to correct the dirty aggregation query result on the stale data. Our results are provably bounded, as opposed to unbounded stalness, and the sampling gives a flexible tradeoff to meet performance constraints. Sampling helps reduces both bottlenecks in view maintenance, delta view calculation and view updating, as it reduces the number of updates that need to processed and then written.

Another relevant concept from data cleaning is outlier detection [?]. Sampling has the potential to mask outliers and in fact it is known heavy-tailed distributions are poorly approximated from samples [?]. Recent work has shown that outlier indexing, ie. separating the values from the tail, can improve sample estimates in such distributions. Coupling outlier detection with sampled views has an interesting implication; not only are the outliers themselves interesting for analysis, but the information from the outliers can potentially improve query accuracy or likewise reduce the number of needed samples.

In summary, our contributions are as follows:

- We present a query processing framework that gives bounded error for aggregation queries on stale views, while providing a tradeoff between error and performance.
- We show how coupling concepts from data cleaning such as correction estimates and outlier detection can give increased accuracy (and performance).
- We evaluate our approach on two systems, Apache SparkSQL and MySQL, and discuss how the different systems affect performance performance parameters.

#### 1.1 Background

Materialized views are stored query results that are used to optimize query processing [?]. Due to the decreasing cost of memory, in-memory materialization has had much interest in recent research [?] and materialization research has expanded beyond the SQL setting [?].

However, pre-computed query results face the obvious challenge of staleness when applied in a setting where the underlying tables are updating. One commonly applied solution is to recompute the materialized views when the table has been updated. This can be very expensive in the presence of small updates that hardly change the derived views. Consequently, incremental maintenance of materialized views is well studied see [?] for a survey of the approaches. A simple model of incremental maintenance consists of two steps: calculating a "delta" view, and "refreshing" the materialized view with the delta. More formally, given a base relation T, a set of updates U, and a view  $\mathbf{V}_T$ :

Calculate the Delta View- In this step, we apply the view definition to the updates and we call the intermediate result a "delta" view.

$$\Delta \mathbf{V} = \mathbf{V}_U$$

This is also called a *change propagation formula* in some literature, especially on algebraic representations of incremental view maintenance.

**Refresh View-** Given the "delta" view, we merge the results with the existing view:

$$\mathbf{V}_{T}^{'} = refresh(\mathbf{V}_{T}, \Delta \mathbf{V})$$

The details of the refresh operation depend on the view definition. Refer to [?] for details.

In this work, we address three types of materialized views: Select-Project, Aggregation, and Foreign-Key Join views; and four common aggregation queries on these views: SUM, COUNT, AVG, and VAR. We further analyze only insertions into the database and defer analysis of updates and deletions for future work.

#### 1.2 Scheduling Maintenance

While often less expensive than recomputing a materialized view, incremental maintenance can still be computationally expensive. Materialized views are growing larger and are more frequently implemented in distributed systems. Due to this cost, which we will refer to as the "maintenance" cost, scheduling the refresh operation has been an important topic of research.

There are two principle types of scheduling strategies: immediate and deferred. In immediate maintenance, as soon as a record is updated, the change is propagated to any derived materialized view. Immediate maintenance has an advantage that materialized view is always up-to-date, however it can be very expensive. This scheduling strategy places a bottleneck when records are written reducing the available write-throughput for the database. Furthermore, especially in a distributed setting, record-by-record maintenance cannot take advantage of the benefits of consolidating overheads by batching. To address these challenges, deferred maintenance is alternative solution. In deferred maintenance, the user often accepts some degree of staleness in the materialized view for additional flexibility for scheduling refresh operations. For example, a user can update the materialized view nightly during times of low-activity in the system. More sophisticated deferred scheduling schemes are also possible, refer to [?] for a full survey.

# 1.3 A Data Cleaning Approach

Without consistency guarantees, in many deferred incremental maintenance approaches, queries on the materialized view are stale until the refresh. In fact, in general, the relative error between the stale result and the up-to-date result is unbounded. But the tradeoff is that deferred maintainence allows flexibility in scheduling to meet the performance constraints of the system and workload.

To similar effect, sampling has been applied to scale expensive query processing operations in streaming [?], aggregate query processing [?], and data cleaning [?]. In particular, the problem of staleness closely resembles a data cleaning problem. There are rows in materialized view that are incorrect, and there is a procedure to "clean" these rows. In the SampleClean project [?], the authors suggested that to process aggregate queries on dirty datasets, one need not clean the entire dataset but rather a random sample to get an approximate answer. Rather than an uncleaned result that can be arbitrarily dirty, you acheive an approximate result with bounded sampling error.

Similarly, in context of materialized views, we address the key question of whether we have to maintain the entire view to answer aggregate queries with bounded error. In this work, we use sampling to infer up-to-date results for aggregation queries on stale materialized views. We can apply incremental maintenance to just a sample of the view, thus greatly reducing the cost needed to maintain the view (Figure ?). With the sampling ratio, the user has a knob to tradeoff performance (in terms of throughput and refresh latency) and accuracy.

We envision that this work is complementary to incremental maintenance. In the periods between full materialized view refreshes, the user maintains a sample of the view. The user specifies a sampling ratio that meets the systems performance constraints. With this, the user gets guarantees that for the aggregate queries the results have bounded error and the queries return with error bars.

#### 1.4 Extending SampleClean For Correcting Staleness

Given the three categories of views and the SUM, COUNT, AVG, and VAR queries on these views, we can formalize the concept of staleness. Let  $\mathbf{V}_T$  be the old view, and  $\mathbf{V}_T'$  be the up-to-date view. If f is an aggregation function, then we call the staleness error of the query  $\epsilon$  if:

$$f(\mathbf{V}_T') = f(\mathbf{V}_T) + \epsilon$$

Since we already have the out-of-date view, we can easily compute  $f(\mathbf{V}_T)$ . In this work, we look at correcting staleness by estimating  $\epsilon$  from the sample. In other words, we use sampling to learn how updates affect the aggregation query on the view and then correct the query results.

In [?], the authors proposed an algorithm called "NormalizedSC" which estimated the error term  $\epsilon$  from a sample of the difference set. We address a few new challenges in this work. First, NormalizedSC was designed in the context of static tables and data dirtiness that can be modeled as record transformations. In this work, we notice that correcting staleness can imply inserting new rows into the view as well as transforming old ones. A further addition, is we consider the effects of outliers on the estimate of NormalizedSC and characterize the optimality of the NormalizedSC algorithm.

#### 2. SYSTEM ARCHITECTURE

The architecture of our proposed solution is shown in Figure 2.4. In this section, we will give an overview of each of the blocks of the system.

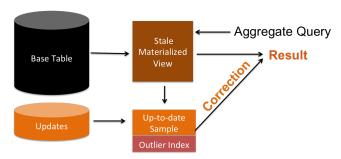


Figure 1: TODO

# 2.1 Supported Materialized Views

We will first introduce the taxonomy of materialized views that can benefit from our approach. In particular, we provide example situations when view maintenance can be costly.

#### Select-Project Views

One type of view that we consider are views generated from Select-Project expressions of the following form:

```
SELECT [col1,col2,...]
FROM table
WHERE condition([col1,col2,...])
```

There are situations when such views are expensive to maintain. For example, as often the case with activity logs, the base table may contain semi-structured data that requires parsing or preprocessing as a part of the view definition. Consider the following example, a typical column in online activity logs is the User-Agent String (Figure ?). When a user accesses a webpage the browser reports this string to identify the browser type, operating system, and layout engine. Suppose, we wanted to create the following view:

```
SELECT * FROM Log
WHERE userAgent
LIKE '% Mozilla%'
```

This involves evaluating regular expression on the string to see if it matches a criteria. Testing a complex regular expression will be far more expensive than numerical comparisions or equality testing. In more extreme examples, the columns may be serialized objects (eg. represented in JSON) which need to be describilized before evaluating a predicate.

#### **Aggregation Views**

We also consider aggregation views of the following form:

```
SELECT [f1(col1), f2(col2), ...]
FROM table
WHERE condition([col1, col2, ...])
GROUP BY [col1, col2, ...]
```

While the same costs that Select-Project views can incur due to pre-process apply as well, aggregation views pose additional challenges to incremental view maintenance. Aggregation views can be costly to maintain when the cardinality of the result is large; that is when there group by clause is very selective. Consider the following example:

```
 \begin{array}{ccc} {\rm SELECT\ videoID\ ,} \\ & {\rm max(responseTime)} \end{array} \ {\rm as\ maxResponseTime} \\ {\rm FROM\ Log} \\ {\rm GROUP\ BY\ videoID\ ;} \end{array}
```

The cardinality of the delta view is the total number of videos in the log which can be very large. Thus it will be costly to propagate this result with the existing view, potentially updating a large number of rows. These costs increase in a distributed environment where a larger delta view means that more data has to be communicated through a shuffle operation.

#### Foreign-Key Join Views

The third type of view we consider are Foreign-Key Join views:

```
SELECT table1.[col1,col2,...], table2.[col1,col2,...]
FROM table1, table2
WHERE table1.fk = table2.fk
AND condition([col1,col2,...])
```

Such views are ubquitious in star schemas [?] and can be particularly costly to maintain in distributed environments. Consider the following example:

```
SELECT *
FROM Log, Video
WHERE Log.videoID = Video.videoID;
```

Suppose new recrods have been inserted into Log. Calculating the delta view involves joining the new records with the entire table Video. While indexing is the prefered strategy to optimize such joins, many distributed systems, such as Apache Spark, Cloudera Impala, and Apache Tez, lack native support for join indices. To avoid scanning the entire table, these systems rely on partitioned joins where records linked by foreign keys are stored on the same partition. However, when these join keys cross partition lines this operation can become increasingly expensive.

#### 2.2 Reducing Maintenance Cost With Sampling

We presented examples where these views can be expensive to maintain. In this work, we address the question of whether we need to maintain the entire view to answer aggregate queries on these views. Our proposed solution is to sample the delta view  $\Delta \mathbf{V}$ , and incrementally maintain just a sample of  $\mathbf{V}_T$ . For example, in our Select-Project view example application, we would have to parse only a sample of the inserted records. Similarly, for the Aggregation view, sampling  $\Delta \mathbf{V}$  reduces the cardinality of the result and consequently communication/merging costs. And finally, for the Join views, we would only have to join a sample of the inserted records.

# 2.3 Outlier Indexing

We are often interested in records that outliers, which we define in this work as records with abnormally large attribute values. Outliers and power-law distributions are a common property in web-scale datasets. Often the queries of interest involve the outlier records, however sampling does have the potential to mask outliers in the updates. If we

have a small sampling ratio, more likely than not, outliers will be missed.

Therefore, we propose coupling sampling with outlier indexing. That is, we guarantee that records (or rows in the view derived from those records) with abnormally large attribute values are included in the sample. What is particularly interesting is that these records give information about the distribution and can be used to reduce variance in our estimates.

# 2.4 Relationship to SAQP

Estimating the results of aggregate queries from samples has been well studied in a field called Sample-based Approximate Query Processing (SAQP). While the concept of estimating a correction from a sample is similar to SAQP it differs in a few critical ways. Traditional SAQP techniques apply their sampling directly to base tables and not on views. The SAQP approach to this problem, would be to treat aggregate queries on views as nested queries and then apply them to a sample of the base data [?]. Another potential technique would be to estimate the result directly from the maintained sample; a sort of SAQP scheme on the sample of the view. We found that empricially estimating a correction and leveraging an existing deterministic result lead to lower variance results on real datasets (see Section?). We analyze the tradeoffs of these techniques in the following sections.

# 3. CORRECTION APPROXIMATE QUERY PROCESSING

In this section, we will extend the NormalizedSC algorithm to estimate corrections for queries on stale views. The key challenge is to estimate  $\epsilon$  such that:

$$f(\mathbf{V}_{T}^{'}) = f(\mathbf{V}_{T}) + \epsilon$$

### 3.1 Model for Aggregate Queries on Views

What is special about SUM, COUNT, AVG, and VAR aggregate functions is that upto proportionality constant, they can be expressed as means. For example, a SUM is just the mean value times the dataset size, a COUNT is the mean occurance rate times the dataset size, and VAR is mean squared deviation. Let N be the number of tuples in the view V. These queries can also have predicates so we have to incorporate that as an indicator function (true = 1, false = 0) that skips a tuple in the aggregation if the predicate is false. When we couple these queries with predicates, we can express them in the following way:

$$\forall v_i \in V : f(V) = \frac{1}{N} \sum_{i}^{N} \phi(v_i) \cdot predicate(i)$$

We define  $\phi$  in the following way:

Aggregation Query	$\phi(v_i)$
SUM	$N \cdot v_i$
COUNT	N
AVG	$\frac{N}{\sum_{i}^{N} predicate(i)} \cdot v_i$

# 3.2 Corrections For Select-Project and Foreign-Key Join Views

With the model for aggregate queries described above, we can first derive the exact value for  $\epsilon$  without sampling. Since

we only consider a model were records are inserted into the base tables, for these two categories of views  $\mathbf{V}_T \subseteq \mathbf{V}_T'$ . The row differences between  $\mathbf{V}_T$  and  $\mathbf{V}_T'$  are completely represented by the delta table  $\Delta \mathbf{V}$ ; that is rows will only be inserted into the views. Since the aggregate queries are in the form of means, we notice that we can exploit the associativity of summations:

$$f(\mathbf{V}_{T}') = f(\mathbf{V}_{T}) + \epsilon$$

$$f(\mathbf{V}_{T}^{'}) - f(\mathbf{V}_{T}) = \epsilon$$

Up-to a scaling constant c,  $\epsilon$  is the aggregation function applied to the delta table.

$$c \cdot f(\Delta \mathbf{V}) = \epsilon$$

Aggregation Query	Scaling Constant c
SUM	1
COUNT	1
AVG	$\frac{ \Delta V }{ \Delta V  + N}$

#### 3.2.1 Sampling the Delta View

We can extend this theory to a simple random sample  $S_{\Delta V}$  of the delta view  $S_{\Delta V} \subseteq \Delta \mathbf{V}$ . Recall that a simple random sample is uniform sample where every row  $r \in \Delta V$  is in  $S_{\Delta V}$  with equal probability p. For Select-Project and Foreign-Key Join Views, this means we have to take a sample of the updates and then apply the view definition to the sample of the updates. Formally, for every record u inserted into the table, with probability p, we include it in the sample S. Then, we take the sample updates S and apply the view definition forming  $S_{\Delta V}$ . Therefore,

$$c \cdot f(S_{\Delta V}) \approx \epsilon$$

The scaling constant c for the SUM and COUNT queries depends on the sample size and is  $c=\frac{K}{N}$ . By the Central Limit Theorem, means of independent random variables converge to a Gaussian. Furthermore the expected value of  $c \cdot f(S_{\Delta V})$  is  $\epsilon$ .

$$c \cdot f(S_{\Delta V}) \sim N(\epsilon, \frac{\sigma_{diff}^2}{k})$$

$$f(\mathbf{V}_T) + c \cdot f(S_{\Delta V}) \sim N(f(\mathbf{V}_T'), \frac{\sigma_{diff}^2}{k})$$

 $\sigma_{diff}^2$  is an interesting parameter as it quantifies the variance of the delta view. In Section ?, we will analyze this parameter and describe how the statistics of the updates affect the estimate accuracy.

### 3.3 Aggregation Views

Applying the view definition to the updates is not enough information to calculate  $\epsilon$  in aggregation views. Consider the following example view and query pair:

 $\label{eq:View1} \begin{array}{ll} View1 := SELECT \ col2 \; , \; MAX(\,col1 \,) \; \; as \; \; col1\_max \\ FROM \ table \\ GROUP \; BY \; col2 \end{array}$ 

 $\begin{array}{ll} {\rm Query1} \; := \; {\rm SELECT} \; \; {\rm AVG}(\; {\rm col1\_max} \,) \\ {\rm FROM} \; \; {\rm View1} \end{array}$ 

col1	col2	col2	col1_max
3	1	1	6
6	1	2	2
2	2		

Suppose records are inserted into **table** and we can apply the the definition View1 to set of inserted records:

col1	col2		
3	1	col2	col1_max
6	1	2	1
2	1		

However, we see that when we perform the refresh operation, the updated View1 remains the same, thus the  $\epsilon$  for Query1 is 0, even though the delta table has non-zero rows:

col2	col1_max	
1	6	
2	2	

The key point is that the refresh operation depends on the aggregations in view definition, and we need to know how these aggregates change after the refresh to estimate  $\epsilon$ . Let  $\mathbf{W}$  be the join of up-to-date view  $\mathbf{V}_T'$  and the old view  $\mathbf{V}_T$  on the group-by key. To make the example above more interesting we can insert a few more records,  $\mathbf{W}$  would be:

col1	col2			
3	1	col2	col1_max_new	col1_max_old
6	2	1	6	6
2	1	2	4	2
4	2			

The value of  $\epsilon$  for Query1 would be the avg query applied to the difference:

 $\label{eq:QueryEpsilon1} \begin{array}{ll} \operatorname{QueryEpsilon1} & := & \operatorname{SELECT} \operatorname{AVG}(\operatorname{col1\_max\_new} - \operatorname{col1\_max\_old}) \\ \operatorname{FROM} \operatorname{W} \end{array}$ 

However, an interesting about aggregation views is that they do not require scaling constant c as in the the other two categories of views. This is because we refresh the delta view; inferring a correction from the entire view rather than just the updates.

#### 3.3.1 Sampling the Refreshed View

We notice that in the refreshed view each GROUP BY key is unique, and thus, to sample the refreshed view we have to sample by GROUP BY keys in the inserted records. For each inserted record we apply a hash to the cols in the GROUP BY clause, and then we take the result of the hash modulo a sampling ratio to sample the table. The result is that we ensure that every record with the same group by key is either fully in the sample or not, thus none of the rows in the delta view are approximate. Then, we refresh this sample delta view with the old view to get the set of differences.

As in the Select-Project and Foreign-Key views the Central Limit Theorem can be used to bound the approximation, and similarly the result is guaranteed to be unbiased.

$$f(S_{\Delta V}) \sim N(\epsilon, \frac{\sigma_{diff}^2}{k})$$

#### 4. OUTLIER INDEXING

An application of particular interest for up-to-date query results is outlier detection. When we have growing datasets, for example activity logs, we may want to know which records correspond to abnormal activity. Up-to-date query results, as opposed to long periods of staleness, have to potential to detect these outliers quickly. However, as we use sampling to processes aggregate queries on the views, this has a potential to mask outliers. Our framework can be extended to guarantee that outliers records will be incorporated into the sample. In this section, we discuss how not only are these outliers themselves of interest but that these outliers give information about the distribution of an column, and can greatly improve the accuracy of estimates.

# 4.1 A Model For Outlier Indexing

We propose the following model for detecting and indexing outliers. When creating a view, the user specifies an attribute in the base relation to "outlier index". What this means is the that the records with the l largest attribute values are guaranteed to be included in the sample view. In this outlier model, we detect outliers in updates with a single pass and without having to build the entire delta table. For aggregation views, for the records that are indexed as outliers, we simply add those group by keys to the sample.

# 4.2 Query Processing with the Outlier Index

We can incorporate the outliers into our estimates of the correction  $\epsilon$ . By guaranteeing that certain rows are in the index, we have to merge a deterministic result (set of outlier rows) with the estimate. One way to think of this is that we have  $\epsilon$  is calculated from the set of records that are not outliers. Let  $|V_T'|$  be the size of the updated view, l be the number of rows in the outlier index, and let  $D_o$  be the set of differences (as defined in Section?) for the rows in the outlier index. We can update  $\epsilon$  with the outlier information by:

$$\frac{|V_T^{'}|}{|V_T^{'}| - l}\epsilon + c \cdot f(D_o)$$

# 4.3 Increased Accuracy For Heavy-Tailed Distributions

This outlier indexing procedure can greatly increase the accuracy of estimates where the set of difference is heavy tailed. This approach has been well studied in AQP [?] and is called truncation in Statistics [?]. The intuition is that by removing the tail, you are reducing the variance of the distribution, and thus, making it easier to estimate an aggregate from a sample.

#### 5. ANALYSIS

#### 5.1 Cost Analysis

Let n be the number of inserted records, v be the cardinality of the old view, v' be the cardinality of the new view,  $\delta_v$  be the cardinality of the delta view, p be the sampling ratio, and l be the size of the outlier index.

**Scan of Updates:** Both incremental maintenance and our proposed solution require at least one scan of the inserted records, and in both solutions we can load the updates into memory once and amortize that I/O cost over all views. If a user chooses to add an outlier index on an

attribute in the updates building this index also requires a single scan of the inserted records. However, as the index is based on the base relation and not the delta view this can be populated when the record is inserted.

**Delta View:** For Select-project and foreign-key join views, incremental maintenance has processing cost of n records where the predicate or the join has to be evaluated for each inserted record. Our approach has a cost of np as we have to evaluate this only on our sample. For aggregation views, incremental maintenance has the processing cost of n and in addition an aggregation cost of  $\delta_v$  where aggregates for each of the groups have to be maintained. In contrast, for aggregation views, our approach has a cost of  $p\delta_v$  as we sample the group by keys and an expected processing cost of np. If there is an outlier index, the cost increases additively to  $p\delta_v + l$ . For aggregation views, in a distributed environment, there are potentially additional communication costs as the updates may not be partitioned by the group by key.

**Refresh:** Let us first analyze the refresh step in a single node system with a join index. For Select-project and foreign-key join views, incremental maintenance has to insert  $\delta_v$  rows while we have to insert only  $p\delta_v$  records. If there is an outlier index, this cost increases to  $p\delta_v + l$ . For aggregation views, the cost is a little bit more complicated as we have a combination of insertions into the view and updates to the view. Incremental maintenance has to refresh  $\delta_v$  rows while we have to refresh  $p\delta_v$  rows. If there is a join index, in constant time, we can determine which rows are new insertions and which correspond to rows already in the view.

The costs become higher in a distributed environment as we need to consider communication and query processing engines that rely on partitioned joins rather than indices. For aggregation views, we want to partition the data by the group by key. This allows a paritioned join which only requires communication (a shuffle operation) of the delta table. Therefore, in incremental maintenance we have to communicate  $\delta_v$  rows while our solution requires  $p\delta_v$  rows.

**Query:** As incremental maintenance completely refreshes the view, the cost of processing a query on the view is at most v'. In our approach, we use the old view, sample, and outlier index to process a query. For Select-project and foreign-key join views, the processing cost is  $v + p\delta_v + l$  and this is guaranteed to be less than v'. For aggregation views, the cost is v + pv' + l where we calculate a correction by processing pv' + l rows and correct an existing aggregation of v records.

# **5.2** Variance Analysis

We will first analyze the variance of the estimate  $\epsilon$  without the outlier index. In Section ?, we discussed how the variance of  $\epsilon$  is the variance of the difference set. For Select-project and foreign-key join views, this variance can be analytically derived from the variance formula for statistical mixtures [?].

$$f(\Delta V)\frac{\delta_v}{v'}(1 - \frac{\delta_v}{v'}) + var(\Delta V)\frac{\delta_v}{v'} \tag{1}$$

For Aggregation views, the accuracy depends on both the variance of the inserted rows and the updates to existing rows. <TODO>

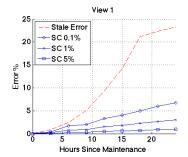
# 5.3 Optimality of Corrections

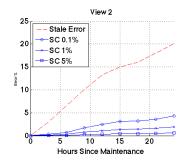
<TODO>

#### 6. RESULTS

# 6.1 Experimental Setting

# 6.2 Query Correction





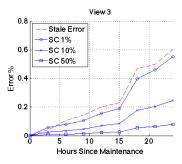


Figure 2: TODO