#### The Count Distinct Problem

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We will use  $\mathbb S$  to represent the set of all the data, and  $\mathbb V$  to represent the set of unique elements.

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- ▶ We can ignore the duplicate values in V.

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  - 3. Find m mod 721.

#### **Implementation**

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```
array.each do | pokemon |
         hash_table[pokemon.hash] = pokemon.hash
3
   end
4 \text{ total} = 0
5 hash_table.each do |val|
6
         if val !=-1
              total = total + 1
8
         end
   end
   puts "The total number of unique encounters is #{total}"
10
   On average: 461 unique encounters
```

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  - ▶ Twitter Problem deals with S of size 200,000,000.
  - Collisions and collision policies also add to the amount of memory required.

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- 4. Take the harmonic average of all the totals in the bitmap.

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Memory Required 
$$\approx \log_2(\log_2(200, 000, 000 \times 10))$$
  
 $\approx 4.94kb$ 

▶ What is the predicted error?

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▶ m is the number of spaces in the bitmap ( $\mathbb{V}$ ).

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- We can lower the sample size and apply a best fit line to the data.
  - For 24 hours, gather 2000 tweets containing "#" every 2 minutes
  - 2. Using the HyperLogLog, determine the unique number of total hashtags every time a new sample is gathered.

### Implementation

```
1  mhll = Hyperll::HyperLogLog.new(10)
2  File.open("twitter_data.txt","r") do | file|
3          file.each_line do | line|
4          mhll.offer line
5          end
6  end
7  str = "Unique Elements: #{mhll.cardinality}"
8  puts str
```

#### Results

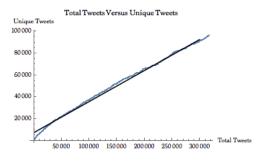


Figure: 0.284356x + 7361.39

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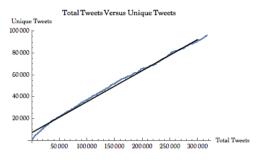


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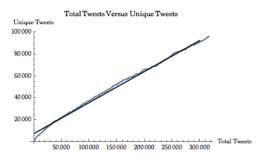


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- ▶  $5.68785 \times 10^7$  unique hashtags.