The Count Distinct Problem

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- ▶ How many *unique* elements are in V?

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We will use $\mathbb S$ to represent the set of all the data, and $\mathbb V$ to represent the set of unique elements.

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- ▶ We can ignore the duplicate values in V.

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 - 3. Find *m mod* 721.

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On average: 461 unique encounters

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 - ▶ Twitter Problem deals with S of size 200,000,000.
 - Collisions and collision policies also add to the amount of memory required.

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- 4. Take the harmonic average of all the totals in the bitmap.

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Memory Required
$$\approx \log_2(\log_2(200, 000, 000 \times 10))$$

 $\approx 4.94kb$

▶ What is the predicted error?

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▶ m is the number of spaces in the bitmap (\mathbb{V}).

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- We can lower the sample size and apply a best fit line to the data.
 - For 24 hours, gather 2000 tweets containing "#" every 2 minutes
 - 2. Using the HyperLogLog, determine the unique number of total hashtags every time a new sample is gathered.

Implementation

```
1  mhll = Hyperll::HyperLogLog.new(10)
2  File.open("twitter_data.txt","r") do | file|
3          file.each_line do | line|
4          mhll.offer line
5          end
6  end
7  str = "Unique Elements: #{mhll.cardinality}"
8  puts str
```

Results

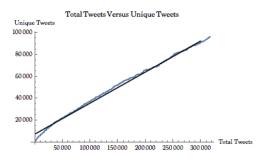


Figure: 0.284356x + 7361.39

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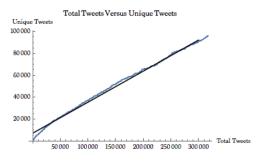


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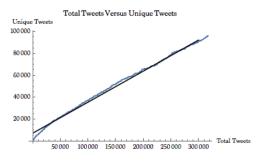


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- ▶ Plugging in 200,000,000 gives us
- ▶ 5.68785×10^7 unique hashtags.