## Scientific Computing With Rust

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#### Team and Research Focus

#### Research Focus:

- Numerical Analysis & Scientific Computing
- 2. PDEs: Acoustics, Electromagnetics, Electrostatics
- High-Performance Computing and Software Engineering



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## My Research

# 'Science with Computers and Maths'

- 1. High Performance Computing
- 2. Heterogenous Computing
- 3. Software Engineering
- 4. Problems in Physics and Engineering



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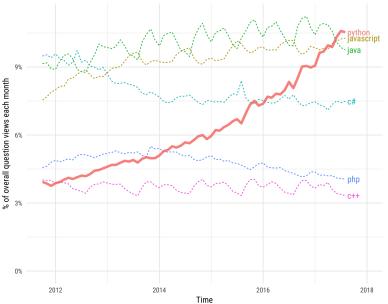
## Expressing Scientific Problems With Software

There is no 'best' language for expressing scientific problems with software.

Though Python has emerged as a defacto standard amongst scientists and engineers for a broad spectrum of problems.

#### **Growth of major programming languages**

Based on Stack Overflow question views in World Bank high-income countries



## The Two Language Problem

- Languages suited for human needs, are less efficient for computers to run.
- 2. Languages easy for computers to run efficiently, are correspondingly less easy for humans to use!

# Why Rust?

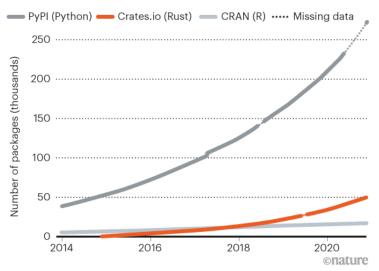
Don't many of the 'two language' problems still exist?

#### Pros of Rust:

- 1. Cargo is awesome!
- 2. Rust is Fast
- 3. Foreign language interfaces are easy
- 4. Easy to learn (harder to master)
- 5. Traits
- 6. Borrow Checker

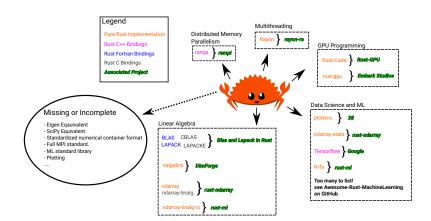
#### **RUST RISING**

The Rust packages repository crates.io has grown sharply since 2016, mirroring the rapid uptake of the language.



https://www.nature.com/articles/d41586-020-03382-2

## State of Scientific Computing in Rust



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## A Splash of Differential Equations

What is an Ordinary Differential Equation?

Imposition of a relationship between functions of a independent single variable and its derivatives.

e.g. Newton's Second Law of Motion (in 1 Dimension)

$$m\frac{d^2x}{dt^2} = F(x(t)) \tag{1}$$

# A Splash of Differential Equations

What is a Partial Differential Equation?

Imposition of a relationship between functions of a multiple independent variables and their derivatives.

e.g. The Heat Equation (in 3D Cartesian Coordinates,

$$\Delta = \frac{d^2}{dx^2} + \frac{d^2}{dy^2} + \frac{d^2}{dz^2}$$

$$\frac{du}{dt} = \Delta u \tag{2}$$

Where u(x, y, z, t).

#### Variational Methods for PDEs I

## Finite Element Method (FEM):

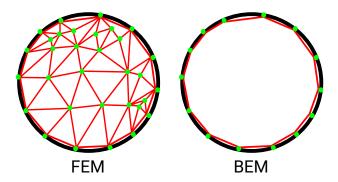
- 1. Meshes over volume.
- 2. Results in sparse matrices.
- Requires explicit boundary conditions.

# Boundary Element Method (BEM):

- 1. Meshes over surface.
- 2. Results in full matrices.
- 3. Boundary conditions captured in formulation.

## Variational Methods for PDEs II

## Consider 2D problem:



# Laplace Interior Boundary Value Problem I

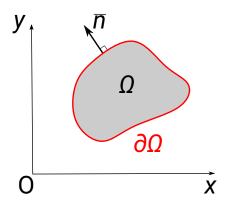
Want to solve

$$\frac{\partial \phi}{\partial x^2} + \frac{\partial \phi}{\partial y^2} = 0 \tag{3}$$

Inside a region of interest  $\Omega$  which has some boundary  $\partial\Omega.$ 

We have conditions for the solution on the boundary:

- 1.  $\frac{\partial \phi(\partial \Omega)}{\partial n}$  Neumann type.
- 2.  $\phi(\partial\Omega)$  Dirichlet type



# Laplace Interior Boundary Value Problem II

Find a solution in terms of a boundary integral,

$$\lambda(\xi,\eta)\phi(\xi,\eta) = \int_{\partial\Omega} [\phi(x,y)\frac{\partial}{\partial n}(\Phi(x,y;\xi,\eta)) - \Phi(x,y;\xi,\eta)\frac{\partial}{\partial n}(\phi(x,y))]ds(x,y)$$
(4)

Where,

$$\lambda(\xi,\eta) = \begin{cases} 0 & (\xi,\eta) \notin \Omega \cup \partial\Omega \\ 1/2 & (\xi,\eta) \in \partial\Omega \\ 1 & (\xi,\eta) \in \Omega \end{cases}$$
 (5)

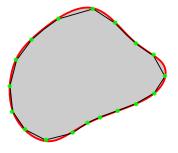
and the Fundamental Solution,

$$\Phi(x, y; \xi, \eta) = \frac{1}{4\pi} \ln[(x - \xi)^2 + (y - \eta)^2]$$
 (6)

# Laplace Interior Boundary Value Problem III

$$\lambda(\xi,\eta)\phi(\xi,\eta) = \int_{\partial\Omega} [\phi(x,y)\frac{\partial}{\partial n}(\Phi(x,y;\xi,\eta)) - \Phi(x,y;\xi,\eta)\frac{\partial}{\partial n}(\phi(x,y))]ds(x,y)$$
(7

# Laplace Interior Boundary Value Problem IV



# Laplace Interior Boundary Value Problem V

Approximate with N constant elements, with a midpoint value.

$$\lambda(\xi,\eta)\phi(\xi,\eta) = \sum_{k=1}^{N} \overline{\phi(x,y)}^{(k)} \int_{\partial\Omega} \frac{\partial}{\partial n} (\Phi(x,y;\xi,\eta)) ds(x,y) - \overline{\frac{\partial}{\partial n}} (\phi(x,y)) \int_{\partial\Omega} \Phi(x,y;\xi,\eta) ds(x,y)$$
(8)

## Laplace Interior Boundary Value Problem VI

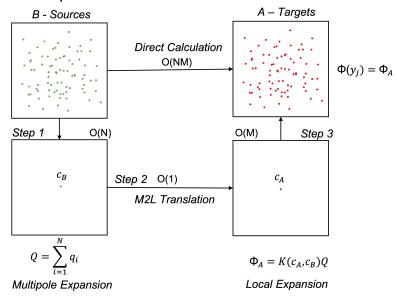
Final Matrix Vector product (matvec) relating points on boundary, to solution in interior of the form,

$$Ax = b (9)$$

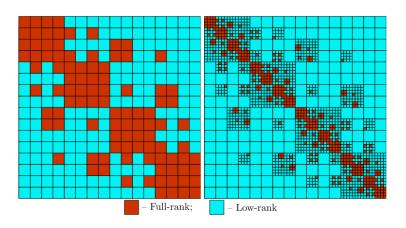
Where A is the coefficient matrix, x is the boundary data and b is the solution.

- 1.  $O(N^2)$  scaling with N elements.
- 2. Each matrix element also involves calculating horrible maths.

## Fast Multipole Methods

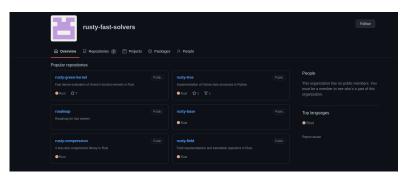


## Fast Direct Solvers



Ambisekaran, S & Darve, E. *The Inverse Fast Multipole Method*, arXiv:1407.1572v1 (2014)

## Rusty Fast Solvers Project I



https://github.com/rusty-fast-solvers

## Rusty Fast Solvers Project II

#### Checklist:

- 1. Rusty Green Kernel Optimized math kernel operations.
- 2. Rusty Tree Distributed Octrees.
- 3. Hyksort Sorting algorithm for distributed arrays.
- 4. Rusty Compression Randomized compression library.
- 5. Rusty Field Field representations.
- 6. Rusty FMM Fast Multipole Method.
- 7. Rusty Inverse Fast Direct Solvers.

## Rusty Fast Solvers Project III

Rusty Tree is the most complete work item, with full Python bindings.

It's a distributed octree implementation, parallelized with MPI.

https://github.com/rusty-fast-solvers/rusty-tree

#### Maturin

Maturin is a tool for developing Python bindings for Rust using its foreign function interface.

Let's look at a demo project together:

https://github.com/skailasa/pyrustmpi

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#### Conclusion

- 1. We're building Rust infrastructure for the O(N) forward and inverse application of a large class of integral operators that incorporates multiple levels of parallelism.
- 2. Rust makes building and distributing scientific software easy.
- 3. Ecosystem of numerics tools is growing.
- 4. We're excited to be part of a larger movement!