# In Harm's Way? Infrastructure Investments and the Persistence of Coastal Cities by Clare Balboni

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#### Motivation

- How should we make investments in transportation infrastructure today, when the future might look different from today?
- Depends on how future changes in environment affect net present value from today's investments.
- People respond to infrastructure changes and environmental changes, so the NPV is an equilibrium object.
- This paper provides a framework for comparing this NPV under alternative investment scenarios.

#### Context

- Sea level rise will "flood" many low lying coastal areas.
- Yet, currently these areas globally have high concentration of economic activity and population.
- Vietnam is a classic case of this.
- However, from 2000-2010 massive infrastructure upgrades were made to connect coastal areas to inland.
- Is this misallocation? How much?

#### Plan

- Focus on theoretical framework
- Testing the model and calibration
- Solving the model and counterfactuals

#### Theoretical Framework

- Discrete time t, several locations  $n, i \in N$ .
- Locations differ in productivity  $A_{n,t}$ , amenities  $B_{n,t}$ , supply of land  $H_{n,t}$  and initial labor endownment  $L_{n,0}$ .
- Monopolistically competitive firms in each location produce horizontally differentiated varieties using labor.
- Forward looking consumers in each locations
  - choose consumption (goods and housing) and where to live/work next period, and
  - inelastically supply one unit labor.
- Locations trade goods with each other and also with rest of the world.

#### Consumers

Value function in location n at time t is given by

$$v_{n,t} = \underbrace{\alpha \log \left( C_{n,t} / \alpha \right) + \left( 1 - \alpha \right) \log \left( H_{n,t} / (1 - \alpha) \right)}_{\text{consumption choice at } t \text{ given income and prices in } n} \\ + \max_{i \in N} \left[ \beta E \left( v_{i,t+1} \right) - \underbrace{\mu_{in}}_{\text{time-invariant}} + B_{i,t} + \underbrace{b_{i,t}}_{\text{location preference shock:}} \right] \\ = \underbrace{\mu_{in}}_{\text{time-invariant}} + B_{i,t} + \underbrace{b_{i,t}}_{\text{location preference shock:}} \\ = \underbrace{\mu_{in}}_{\text{time-invariant}} + B_{i,t} + \underbrace{b_{i,t}}_{\text{location preference shock:}} \\ = \underbrace{\mu_{in}}_{\text{time-invariant}} + B_{i,t} + \underbrace{b_{i,t}}_{\text{location preference shock:}} \\ = \underbrace{\mu_{in}}_{\text{time-invariant}} + B_{i,t} + \underbrace{b_{i,t}}_{\text{location preference shock:}} \\ = \underbrace{\mu_{in}}_{\text{time-invariant}} + B_{i,t} + \underbrace{b_{i,t}}_{\text{location preference shock:}} \\ = \underbrace{\mu_{in}}_{\text{time-invariant}} + B_{i,t} + \underbrace{b_{i,t}}_{\text{location preference shock:}} \\ = \underbrace{\mu_{in}}_{\text{time-invariant}} + B_{i,t} + \underbrace{\mu_{in}}_{\text{location preference shock:}} \\ = \underbrace{\mu_{in}}_{\text{time-invariant}} + B_{i,t} + \underbrace{\mu_{in}}_{\text{location preference shock:}} \\ = \underbrace{\mu_{in}}_{\text{time-invariant}} + B_{i,t} + \underbrace{\mu_{in}}_{\text{location preference shock:}} \\ = \underbrace{\mu_{in}}_{\text{time-invariant}} + B_{i,t} + \underbrace{\mu_{in}}_{\text{location preference shock:}} \\ = \underbrace{\mu_{in}}_{\text{time-invariant}} + \underbrace{\mu_{in}}_{\text{time-invari$$

where  $C_{n,t}$  is the CES demand aggregator

$$C_{n,t} = \left[ \Sigma_{i \in N} \int_0^{M_{i,t}} c_{ni,t}^*(j)^{\frac{\sigma-1}{\sigma}} \mathrm{d}j \right]^{\frac{\sigma}{\sigma-1}}$$

- $c_{ni,t}^*(j)$ : consumption *choice* of variety j from location i in n at time t
- $M_{i,t}$ : endogenously determined measure of varieties supplied by location i (from production)

## Consumers: migration choice

• With algebra and Gumbel properties, we get

$$\max_{i \in N} \left[ \beta E\left(v_{i,t+1}\right) - \mu_{in} + B_{i,t} + b_{i,t} \right] = \nu \log \Sigma_{i \in N} \left( \exp \left[ \beta E\left(v_{i,t+1}\right) - \mu_{in} + B_{i,t} \right] \right)^{\frac{1}{\nu}}$$

and also the share of location n workers that migrate to i at the end of t

$$m_{in,t} = \frac{\left(\exp\left[\beta E\left(v_{i,t+1}\right) - \mu_{in} + B_{i,t}\right]\right)^{\frac{1}{\nu}}}{\sum_{m \in \mathcal{N}} \left(\exp\left[\beta E\left(v_{i,t+1}\right) - \mu_{mn} + B_{m,t}\right]\right)^{\frac{1}{\nu}}}$$

### Consumers: consumption choice

- Think of two stage problem: Each labor unit allocates income  $y_{n,t}$  to  $C_{n,t}$  and  $H_{n,t}$ , then allocate income  $y_{n,t}^C$  within  $C_{n,t}$  to  $c_{ni,t}(j)$ .
- Given the Cobb-Douglas preference over C and H,  $\alpha y_{n,t}$  is spent on C and  $(1-\alpha)y_{n,t}$  is spent on H.
- Within  $C_{n,t}$ , CES functional form implies

$$c_{ni,t}^*(j) = p_{ni,t}(j)^{-\sigma} y_{n,t}^C P_{n,t}^{1-\sigma}$$

where

$$P_{n,t} = \left[ \sum_{i \in N} \int_0^{M_{i,t}} p_{ni,t}(j)^{1-\sigma} \mathrm{d}j \right]^{\frac{1}{1-\sigma}}$$

and  $p_{ni,t}(j)$  is the price of  $c_{ni,t}(j)$ .

- With this setup,  $C_{n,t} = y_{n,t}^C/P_{n,t} = \alpha y_{n,t}/P_{n,t}$ 
  - $ightharpoonup P_{n,t}$  comes from firm's problem given CES demand,
  - $\triangleright$   $y_{n,t}$  next.

#### Consumers: Income

- Workers get income from two sources: wages  $w_{n,t}$  and lump sum transfers of land rental income, which is transferred lump sum to workers.
- Total income at n, t is given by

$$y_{n,t}L_{n,t} = w_{n,t}L_{n,t} + (1-\alpha)y_{n,t}L_{n,t} \implies y_{n,t} = w_{n,t}/\alpha$$

• Also, given  $H_{n,t}$  and  $y_{n,t}$ , land market clearing pins down  $r_{n,t}$ :

$$(1-\alpha)y_{n,t}L_{n,t}=r_{n,t}H_{n,t}$$

## Consumers: Expected Indirect utility

Putting all the pieces together, we get expected indirect utility in location n at time t:

$$V_{n,t} = \alpha \log \left(\frac{w_{n,t}}{\alpha}\right) - \alpha \log P_{n,t} + (1-\alpha) \log \left(\frac{H_{n,t}}{(1-\alpha)L_{n,t}}\right) + \nu \log \Sigma_{i \in N} \left(\exp \left[\beta V_{i,t+1} - \mu_{in} + B_{i,t}\right]\right)^{\frac{1}{\nu}}$$

- ullet Benefit of transportation infrastructure:  $V_{n,t}\downarrow$  in  $P_{n,t} o P_{n,t}\uparrow d_{ni}$  (production)
- Congestion:  $V_{n,t} \uparrow \text{ in } \frac{H_{n,t}}{L_{n,t}}$

## Production: prices

- Two endogenous objects:  $p_{ni,t}(j)$  and  $M_{i,t} \rightarrow P_{n,t}$
- Producing  $x_{i,t}(j)$  quantity of variety j at location i needs requires labor

$$I_{i,t}(j) = F + \frac{x_{i,t}(j)}{A_{i,t}}$$

• Given iceberg costs for transporting from i to n,  $d_{ni,t}$  and CES demand functions above, each firm j sets same price

$$p_{ni,t} = \left(\frac{\sigma}{\sigma - 1}\right) \frac{d_{ni,t} w_{i,t}}{A_{it}}$$

## Production: $M_{i,t}$

ullet With this, zero profit condition implies labor demand for variety j

$$I_{i,t}(j) = \sigma F$$

Labor market clearing in n, t

$$\underbrace{\int_{0}^{M_{i,t}} I_{i,t}(j)}_{\text{labor demand}} = M_{i,t} \sigma F = \underbrace{L_{i,t}}_{\text{labor supply}}$$

- Agglomeration economies via CES demand: More varieties at cheaper prices
  - ▶  $M_{n,t}$  proportional to  $L_{n,t}$ , and
  - ▶ locally produced variety is cheaper  $p_{ni}(j) \uparrow$  in  $d_{ni}$

#### Bilateral trade

Gravity: Value of bilateral trade flows from i to n

$$X_{ni,t} = \alpha \left( X_{n,t} P_{n,t}^{\sigma-1} \right) M_{i,t} p_{ni,t}^{1-\sigma}$$

• Share of n's expenditure on goods from i

$$\pi_{ni,t} = \frac{X_{ni,t}}{\sum_{k \in N} X_{nk,t}} = \frac{M_{i,t} p_{ni,t}^{1-\sigma}}{\sum_{k \in N} M_{k,t} p_{nk,t}^{1-\sigma}}$$

• Trade balance: Total income at location i is equal to the total expenditure on goods produced in location i

$$w_{i,t}L_{i,t} = \sum_{n \in N} \pi_{ni} X_{n,t}$$

#### Bilateral trade

• Under symmetric trade costs, trade balance is a set of two static conditions

$$w_{i,t}L_{i,t} = L_{i,t} \left(\frac{w_{i,t}}{A_{i,t}}\right)^{1-\sigma} MA_{i,t}$$

$$MA_{i,t} = \sum_{n \in N} \frac{d_{ni,t}^{1-\sigma} X_{n,t}}{MA_{n,t}} = \sum_{n \in N} \frac{d_{ni,t}^{1-\sigma} w_{n,t} L_{n,t}}{MA_{n,t}}$$

- $MA_{i,t}$  useful for testing the model.
- International trade: Add RoW to the set of locations.
  - ▶ Treat exports  $E_t$  are exogenous.
  - Model implies that only data on total exports and bilateral international trade costs is needed.

## Sequential equilibrium

Given  $\{d_{in,t}, \mu_{in}, A_{n,t}, B_{n,t}, H_{n,t}, E_t\}$ , a sequential equilibrium is a set of labor allocations  $\{L_{n,t}\}$ , wages  $\{w_{n,t}\}$ , migration shares  $\{m_{ni,t}\}$ , market access terms  $\{MA_{n,t}\}$  and expected lifetime utilties  $\{V_{n,t}\}$  that solve

- Trade equilibrium: previous slide
- Consumer's problem: Expected indirect utility satisfies the  $V_{n,t}$  recursion
- Migration shares

$$m_{in,t} = \frac{\left(\exp\left[\beta V_{i,t+1} - \mu_{in} + B_{i,t}\right]\right)^{\frac{1}{\nu}}}{\sum_{m \in \mathcal{N}} \left(\exp\left[\beta V_{m,t+1} - \mu_{mn} + B_{m,t}\right]\right)^{\frac{1}{\nu}}}$$

• Law of motion of  $L_{n,t}$ 

$$L_{n,t+1} = \sum_{i \in N} m_{ni,t} L_{i,t}$$

## Testing the model

• Taking logs and first-differencing

$$w_{i,t}L_{i,t} = L_{i,t} \left(\frac{w_{i,t}}{A_{i,t}}\right)^{1-\sigma} MA_{i,t}$$

implies

$$\triangle \log w_i = \left(\frac{\sigma - 1}{\sigma}\right) \triangle \log A_i + \left(\frac{1}{\sigma}\right) \triangle \log MA_i$$

• Measuring MA: Use data on  $\{d_{ni,t}w_{n,t}L_{n,t}\}$  for t=2000 and t=2010, and solve

$$MA_{i,t} = \sum_{n \in N} \frac{d_{ni,t}^{1-\sigma} w_{n,t} L_{n,t}}{MA_{n,t}}$$

and compute  $\triangle \log MA_i = \log MA_{i,2010} - \log MA_{i,2000}$ .

• Compare coefficient on  $\triangle \log MA_i$  to  $\frac{1}{\sigma}$ .

## Testing the model

$$\triangle \log w_i = \left(\frac{\sigma - 1}{\sigma}\right) \triangle \log A_i + \left(\frac{1}{\sigma}\right) \triangle \log MA_i$$

- Endogeneity:  $\triangle \log A_i$  is unobserved
  - ▶ Productivity trends correlated with △MA controls and region FE
  - ► Transportation improvements correlated with district-level unobservables
  - ▶ Spatial correlation between  $\triangle w_n$  or  $\triangle L_n \rightarrow$  spurious correlation between  $\triangle \log w_i$  and  $\triangle \log MA_i$
- Use IV based announcement of a highway project to be built along the route of the historic Ho Chi Minh Trail from 2000.
- Exclusion: Trail constructed as logistical supply route for soldiers from 1969-1973
  - ▶ Add controls for district geography, US bombing and district characteristics.
- Calibrated  $\frac{1}{\sigma} = \frac{1}{7}$  lies within the 95% CI of coefficient.

#### Data and Calibration

- 541 spatial units (districts) geographic, demographic and economic data for 2010, and some for 2000.
- $d_{ni}$  measured as lowest cost route between any two district centroids (more details)
- Road construction costs from engineering
- $\alpha$ ,  $\beta$ ,  $\sigma$ ,  $\nu$  (migration elasticity) from external sources.
- Calibrate  $MA_{i,2010}$  as above and use trade balance to get  $A_{i,2010}$ .
- Set assumptions about future inundation gradual inundation of land below 1m over 100 years.
  - ▶  $H_{n,t}$  gradually goes down by fraction of area of district n below 1m.
  - $ightharpoonup d_{ni}$  gradually goes up for all road stretches below 1m.

## Solving the model

- We don't observe  $\{\mu_{in}\}$  or  $\{B_{n,t}\}$  (even in initial period).
- Solve the model in relative time differences Caliendo et. al. (2019).
  - ▶ Closed form expressions for  $Y_{n,t} = [\exp(V_{n,t+1} V_{n,t})]^{\frac{1}{\nu}}$  and ratio of migration shares.
  - ▶ time-invariant  $\{\mu_{in}\}$  cancel out, also  $B_n$
  - ▶ In general, we don't need to know the levels of some of the fundamentals
- Solution method has two requirements:
  - Need to know initial conditions and paths for model fundamentals  $\{d_{in,t}\}$ ,  $\{A_{n,t}\}$ ,  $\{H_{n,t}\}$  and  $\{E_t\}$  and agents have perfect foresight.
  - Sequential equilibrium converges to a stationary equilibrium i.e. all endogenous objects are constant in the long run.

## Solving the model

#### Simulation-based solution method

- Fix T (when path becomes stationary) and  $\{d_{in,t}, A_{n,t}, H_{n,t}, E_t\}_{t=0}^T$ .
- Guess a path of  $Y_{n,t}$  such that  $Y_{n,T} = 1$ .
- Given  $m_{in,-1}$ , solve for path of  $\{m_{in}\}$ , and use this to infer path of  $\{L_{nt}\}$ .
- Solve the static equilibrium conditions for  $MA_{nt}$  each period and get  $w_{nt}$ .
- Use these to calculate  $Y_{n,t}^{new}$ , which serves as the updated guess until convergence.

#### Counterfactuals

• The paper derives a closed form expression for expected lifetime utility

$$W_{n,t} = \sum_{s=t}^{\infty} \beta^{s-t} \log \left( \frac{\frac{w_{n,s}}{\alpha} \exp(B_{n,s})}{P_{n,s}^{\alpha} \left( \frac{(1-\alpha)L_{n,s}}{H_{n,s}} \right)^{1-\alpha} m_{nn,s}^{\nu}} \right) = \sum_{s=t}^{\infty} \beta^{s-t} \log \left( \Omega_{n,s} \right)$$

• Denoting a counterfactual scenario by  $\hat{\ }$ , time t compensating variation in consumption  $\delta_{n,t}$  satisfies

$$\hat{\mathcal{W}}_{n,t} = \sum_{s=t}^{\infty} \beta^{s-t} \log \left( \delta_{n,t} \hat{\Omega}_{n,s} \right)$$

which gives a measure of change in welfare

$$\triangle \mathsf{Welfare}_{n,t} = \log\left(\delta_{n,t}\right) = (1-eta) \Sigma_{s=t}^{\infty} eta^{s-1} \log\left(\hat{\Omega}_{n,s}/\Omega_{n,s}\right)$$

- Each counterfactual scenario comprises a different set of model fundamentals  $\{\hat{d}_{in,t}, \hat{A}_{n,t}, \hat{H}_{n,t}, \hat{E}_t\}_{t=0}^T$ .
- The all scenarios assume fixed  $A_{n,t} = A_{n,2010}$  and  $B_{n,t} = B_n$ , which drop out in relative time differences.

#### Counterfactuals

- Ex-post evaluation of roads built from 2000-2010 average welfare 1.47% higher with future inundation, 2.49% higher without.
- Ex-ante evaluations of infrastructure projects with same total cost as the ones realized
  - non-targeted: connect all districts, maximize market potential (distance weighted market size)
  - ▶ targeted: maximize market potential outside sub-1m zone, sub-5m zone.
- Important findings
  - upgrades that maximize market potential outside sub1-m zone give 72% welfare improvements.
  - even the non-targeted projects do not favor coastal areas!
  - ▶ without sea-level rise 72% reduced to 48% still substantial!
- Robustness with changes in  $A_{n,t}$  and  $B_{n,t}$ , and more...