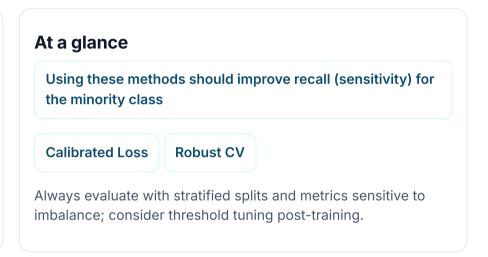
Imbalanced Classification — Practical Methods

A concise overview of four core techniques to handle class imbalance:

- Random Oversampling
- Synthetic Minority Oversampling (SMOTE)
- Random Undersampling
- · Class-Weighted/Loss-Adjusted training.

When to use

- Positive class is rare (e.g., fraud, defects, disease).
- Baseline classifier biased toward majority predictions.
- Metrics like accuracy are misleading; use ROC-AUC/PR-AUC, recall, $F_{\mbox{\scriptsize B}}.$
- $\beta < 1$ gives more emphasis on Precision. $\beta > 1$ gives more emphasis on Recall.



1) Random Oversampling

Duplicate minority samples until class counts are balanced (or closer to balanced).

Simple example

Dataset: 1,000 samples with 50 positive (minority) and 950 negative (majority). Oversample positives by duplicating them \sim 19× to reach \approx 950 positives. Train the model on the augmented dataset.

Pros: Easy; preserves minority distribution; works with any model.

Cons: Risk of overfitting (exact duplicates); no new

information introduced.

Practical notes

- Combine with data augmentation (noise, jitter) for robust models.
- Apply inside cross-validation folds to avoid leakage.
- Useful baseline to compare against SMOTE variants.

2) SMOTE — Synthetic Minority Oversampling Technique

Generate synthetic minority samples by interpolating between a sample and one of its minority nearest neighbors.

Description (with tiny example)

Pick a minority point \mathbf{x}_i . Find its k-nearest minority neighbors. Randomly choose one neighbor \mathbf{x}_z . Draw $\lambda \sim \mathcal{U}(0,1)$ and create:

$$x_{new} = x_i + \lambda (x_z - x_i)$$

Example (1D intuition): if $x_i=2.0$ and neighbor $x_z=5.0$, a sample with $\lambda=0.3$ yields $x_{\rm new}=2+0.3(5-2)=2.9$.

Pros: Reduces overfitting vs pure duplication; smooths decision regions.

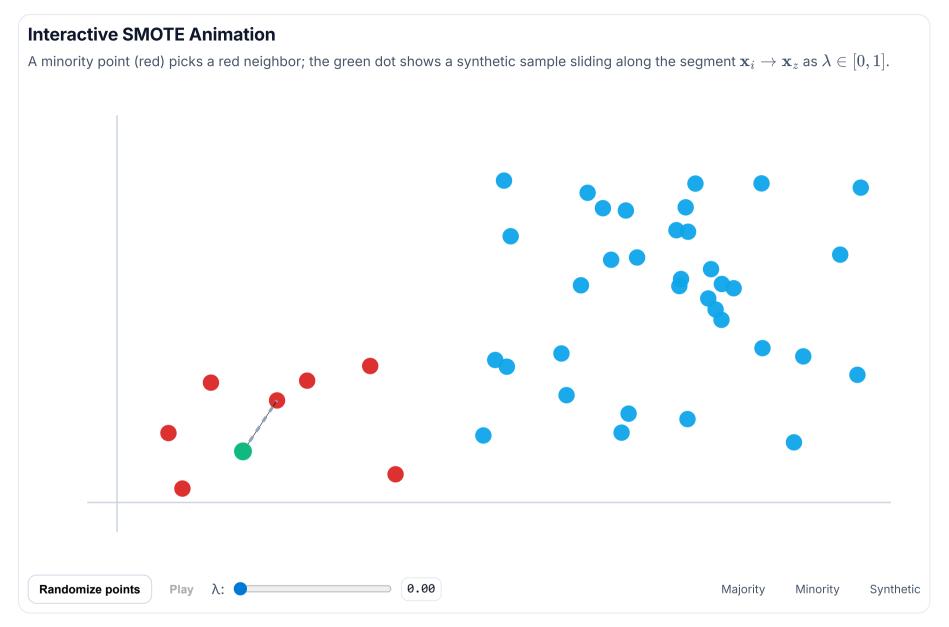
Cons: Can create ambiguous samples near class boundaries; mind feature scaling & categorical features.

Mathematical description

Given minority set $\mathcal{X}_{\min} = \{\mathbf{x}_1, \dots, \mathbf{x}_m\}$, choose $\mathbf{x}_i \in \mathcal{X}_{\min}$, pick neighbor $\mathbf{x}_z \in \mathsf{NN}_k(\mathbf{x}_i) \cap \mathcal{X}_{\min}$, and sample

$$\mathbf{x}_{
m new} \ = \ \mathbf{x}_i \ + \ \lambda ig(\mathbf{x}_z - \mathbf{x}_iig), \qquad \lambda \sim \mathcal{U}(0,1).$$

Repeat until desired oversampling ratio is met. Use distances after proper normalization; categorical features require specialized variants (e.g., SMOTE-NC).



3) Random Undersampling

Remove a subset of majority samples to reduce imbalance (and training time).

Simple example

Dataset: 100 positive (minority) vs 9,900 negative (majority). Randomly discard ~9,800 majority samples to reach ~100 vs 100. Train on the reduced set.

Pros: Faster training; simplifies decision boundary; useful

when majority is very redundant.

Cons: Risk of discarding informative majority cases; higher

variance if too aggressive.

Practical notes

- Prefer stratified undersampling or informed heuristics (e.g., keep "hard negatives").
- Combine with cost-sensitive loss instead of extreme undersampling.
- Always apply inside CV folds to avoid leakage.

4) Class Weights / Loss Function Adjustment

Modify the loss so that mistakes on the minority class cost more than those on the majority class.

Binary cross-entropy with class weights

Let $y_i \in \{0,1\}$, prediction $p_i = \Pr(y_i = 1 \mid \mathbf{x}_i)$, and weights w_1 (for positives) and w_0 (for negatives). The weighted loss is

$$\mathcal{L}_{ ext{wBCE}} = -rac{1}{N} \sum_{i=1}^N \Big(w_1 \, y_i \log p_i \; + \; w_0 \, (1-y_i) \log (1-p_i) \Big).$$

Common choice (inverse frequency): for class $c \in \{0,1\}$ with count n_c , total n, and C=2 classes,

$$w_c = rac{n}{C \, n_c}.$$

Larger w_1 increases the gradient for positive errors, improving recall but potentially reducing precision. Tune threshold after training.

Margin-based models (SVM, etc.)

For a linear SVM with hinge loss, class-specific penalty C_c scales the slack term:

$$\min_{\mathbf{w},b,oldsymbol{\xi}} \;\; rac{1}{2} \|\mathbf{w}\|^2 \; + \; \sum_{i=1}^N C_{y_i} \, \xi_i \quad ext{s.t.} \quad y_i \, (\mathbf{w}^ op \mathbf{x}_i + b) \geq 1 - \xi_i, \; \xi_i \geq 0.$$

Setting $C_1 > C_0$ makes positive-class violations more costly.

Simple example

Dataset: 200 positives, 4,800 negatives ($n=5{,}000$). Using $w_c=rac{n}{Cn_c}$ with C=2:

- $egin{array}{ll} ullet & w_1 = rac{5000}{2 \cdot 200} = 12.5 \ ullet & w_0 = rac{5000}{2 \cdot 4800} pprox 0.5208 \end{array}$

These weights push the optimizer to focus more on minority errors.

Quick Comparison & Tips

Method comparison

- Random Oversampling: Baseline; risk of overfitting; consider light noise.
- **SMOTE:** Better generalization; take care near class boundaries; scale features.
- Random Undersampling: Faster; may lose signal; pair with cost-sensitive loss.
- Class Weights: Model-native; no data duplication; pair with threshold tuning.

Evaluation checklist

- Use *stratified* CV and maintain time order for temporal data.
- Prefer PR-AUC and recall @ target precision for rare positives.
- Tune decision threshold on a validation set aligned to business costs.
- Guard against leakage: perform resampling inside each CV fold.

Class Weight parameters of popular classification models

Model	Parameter	Options	Default
LogisticRegression	class_weight	None, "balanced", dict	None
DecisionTreeClassifier	class_weight	None, "balanced", dict	None
RandomForestClassifier	class_weight	None, "balanced", "balanced_subsample", dict	None
XGBClassifier	scale_pos_weight	Positive float (e.g., n _{neg} /n _{pos})	1

Meaning of "balanced" and "balanced_subsample"

For class c with n_c samples in a dataset of total size n and C classes:

$$w_c = rac{n}{C \cdot n_c}$$

- "balanced": The weights w_c are computed using the whole training set once, then applied globally.
- "balanced_subsample": For ensembles (e.g. Random Forests), the same formula is applied but on each bootstrap sample drawn for a tree, so n and n_c are computed *per-subsample*.