

## Psychology of Thinking

- "I am thinking how to do the home assignment"
- "I think there is no lecture today. No one has turned up in class"
- "I am thinking about which phone would be best for me"

## Psychology of Thinking

- Problem Solving
- Reasoning
- Decision Making (and Judgement)

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# Thinking

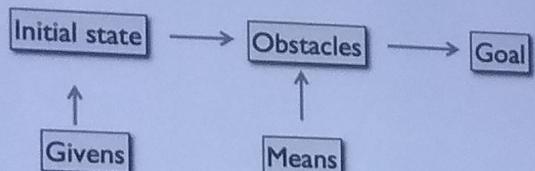
- Cognitive rearrangement or manipulation of *external* (environment) and *internal* (memory) information
- Types of thinking
  - *Unfocused vs Focused*
- Information used in thinking are often called symbols
- Most symbols used in thinking are in the form of language

## Problem Solving

- **Problem:** A gap / barrier / obstacle that interferes with the direct path between initial or current state and the goal
- **Problem Solving difficulty:**
  - **Simple:** paying online
  - **Complex:** investing in stocks
- **Parts of a problem:**
  - **Initial State, Obstacles, Goals**
  - **Givens, Means (steps)**

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## Parts of a problem



- Initial State and Givens:
  - Objects, conditions, and constraints that affect how the problem is approached and solved
  - Explicit (materials) vs Implicit (Experience)
- Obstacles:
  - No recall of previous information
  - No clear path
  - No domain knowledge
  - Limited cognitive capacity
- Means: Operations
  - Cognitive: LTM, attention, working memory
  - Physical: location, weight
- Goal
  - end-state
  - what is desired

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## Parts of a problem

• Obstacles

• Goal

Means

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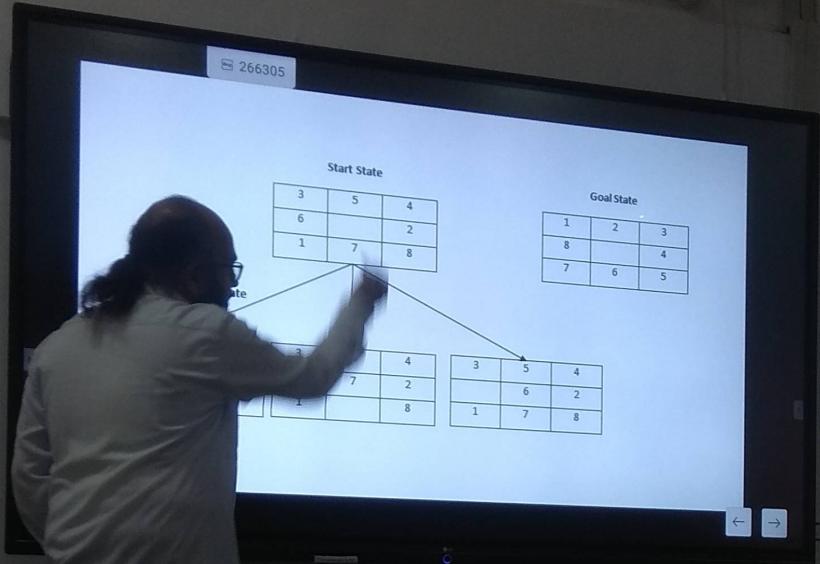
## How Humans Solve Problems

- Problem Space
- Representation
- Memories

- **Problem-solving** is moving from initial state to goal state
- **Problem Space:**
  - All possible things that can be done whether the problem is solved or not solved
  - A set of all states that an agent can achieve

## Problem Space Analysis

- Problem-solving is finding the correct path through the problem space
- Problem Space:
  - Problem State
  - Problem Operators
- Problem solving operators generate a space of possible states through which the problem solver must search to find a path to the goal



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Inter

3	
6	
1	



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## Problem-Solving Operators

- Operator: Action that will transform the problem state to another problem state
- Acquisition of Operators
  - Discovery (*figuring out yourself*)
  - Instruction
  - Modeling examples

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**TABLE 8.1** Instruction for Pyramid Problems

**(a) Direct Specification**

N\$M is a pyramid expression for designating repeated addition where each term in the sum is one less than the previous.  
N, the base, is the first term in the sum.  
M, the height, is the number of terms you add to the base.

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**TABLE 8.1** Instruction for Pyramid Problems

**(a) Direct Specification**

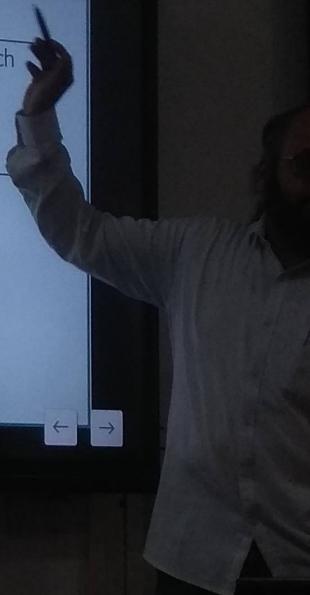
$N\$M$  is a pyramid expression for designating repeated addition where each term in the sum is one less than the previous.  
N, the base, is the first term in the sum.  
M, the height, is the number of terms you add to the base.

**(b) Just an Example**

$7\$3$  is an example of a pyramid expression.

$$7\$3 = 7 + 6 + \underbrace{5 + 4} = 22$$

↑                    ↓  
7 is the            3 is the  
base                height



## Search Strategies

- Algorithms
  - Guaranteed solution if steps are followed
- Heuristics
  - General rules and guidelines
  - Better (quicker) search
  - Role of memory

# Algorithms

- **Nature of algorithm**
  - Guaranteed solution if steps are followed
  - Eg. Maths formula / cooking recipe
- **Exhaustive search**
  - Checking every possible solution
  - Efficiency depends on size of problem space

## Heuristics

- **Nature of Heuristics**
  - A cognitive short-cut that relies on previous knowledge (memory)
  - Does not guarantee a solution
- **Involves utilization of general knowledge.**
  - E.g. Where would you look for if you lost your keys

## Operator Selection Criteria

- **Backup avoidance**
  - *Not going back to previous state*
- **Difference Reduction**
  - *Choosing non-repeating operator that most reduces the difference between current state and goal state*
- **Means-End Analysis**
  - *Breaking problem into smaller/simpler problems*

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## Operator Selection Criteria

- Backup avoidance
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## Hill Climbing

- Makes use of difference reduction
- Each step takes the current state and moves it closer to the end state
- Depends on similarity of the upcoming state to the goal state
- Not applicable for all problems – e.g. Local minima/maxima

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Peak

A hill climbing robot can  
not advance beyond this  
local maximum



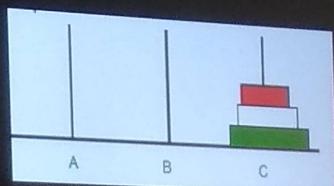
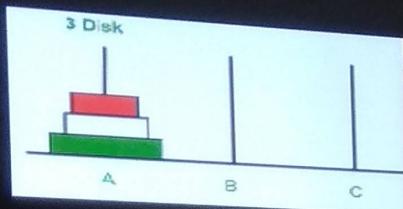
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## Means End Analysis

- Involves reduction of problem space
- Breaking down an ill-defined problem into several smaller well-defined problems
- Unlike difference reduction, it does not abandon an operator if it cannot be used immediately
- It focuses on enabling blocked operators (means)

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### Tower of Hanoi Problem



- Only one disc can be moved at a time
- larger disc must never be on top of the smaller disc



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On one side of a river are three hobbits and three orcs. They have a boat on their side that is capable of carrying two creatures at a time across the river. The goal is to transport all six creatures across to the other side of the river. At no point on either side of the river can orcs outnumber hobbits (or the orcs would eat the outnumbered hobbits). The problem, then, is to find a method of transporting all six creatures across the river without the hobbits ever being outnumbered.



## Impediments to Problem Solving

- Improper Representation
- Functional Fixedness
- Set Effects

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## Improper Representation

- Problems are often represented that don't allow application of appropriate operators

What is the acceleration (increase in speed each second) of a train, if its speed increases uniformly from 15 m/s at the beginning of the 1st second, to 45 m/s at the end of the 12th second?



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Juanita went to work as a teller in a bank at a salary of \$12,400 per year and received constant yearly increases, coming up with a \$16,000 salary during her 13th year of work. What was her yearly salary increase?



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## Functional Fixedness

- Tendency to see objects as serving conventional problem-solving functions and thus failing to see possible novel functions.

## Set Effects

- Einstellung Effect: Negative effect of previous experience on solving new problem

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**TABLE 8.3** Luchins's Water Jug Problems Used to Illustrate the Set Effect

<b>Problem</b>	<b>Capacity (cups)</b>			<b>Desired Quantity</b>
	<b>Jug A</b>	<b>Jug B</b>	<b>Jug C</b>	
1	21	127	3	100
2	14	163	25	99
3	18	43	10	5
4	9	42	6	21
5	20	59	4	31
6	23	49	3	20
7	15	39	3	18
8	28	76	3	25
9	18	48	4	22
10	14	36	8	6