n: the number of dimensions in space (n = 2).

m: the order of the curve passing through a space.

N: the number of bits in a derived-key, N = nm.

i: the number of the iteration of the algorithm, $i \in [1, m]$.

byte: a word containing n bits.

 $\omega^{\mathbf{i}}$: A byte of n bits where

$$\omega^{i} = \omega^{i-1} \oplus \bar{\tau}^{i-1}, \omega^{1} = 0 \ 0 \ \cdots \ 0 \ 0.$$

 $\alpha^{\mathbf{i}}$: A byte of n bits where

$$\alpha^i = \omega^i \oplus \bar{\sigma}^i.$$

 $\mathbf{a_j}$: a coordinate in dimension j of the point, (a_1, a_2, \dots, a_n) whose *derived-key* is r. A coordinate is also expressed as a real number in the range [0, 1). $\alpha_i^{\mathbf{i}}$: a binary digit in a coordinate a_j , such that

$$\alpha_i = a_i^i \cdots \alpha_n^i = a_n^i$$
.

principal position: the last, or least significant, bit position, j, in ρ^i such that $\rho^i_j \neq \rho^i_n$. If all bits in ρ^i are equal, the principal position is the nth, or least significant. The most significant bit position is considered to occupy position 1. **parity**: the number of bits in a byte which are set to 1 modulo 2.

 J_i : An integer between 1 and n equal to the subscript of the principal position of ρ^i .

 $\bar{\sigma}^{\mathbf{i}}$: A byte of n bits where

$$\bar{\sigma}^i = \alpha^i \oplus \omega^i, \bar{\sigma}^1 = \alpha^1$$

There is no shift in $\bar{\sigma}^1$.

 $\sigma^{\mathbf{i}}$: A byte of n bits, such that

$$(J_1-1)+(J_2-1)+\cdots+(J_{i-1}-1)$$

 ρ^i represents the ith byte of n bits in r, such that

$$\rho_1^i = \rho_1^i, \rho_2^i = \sigma_2^i \oplus \sigma_1^i, \cdots, \rho_n^i = \sigma_n^i \oplus \sigma_{n-1}^i.$$

 τ^{i} : A byte of n bits obtained by complementing σ^{i} in the nth position and then, if and only if the resulting byte is of odd parity, complementing in the principal position. Hence, τ^{i} is always of even parity. Note that the parity of σ^{i} is given by the bit ρ^{i}_{n} and that a mask for performing the second complementation may be set up in the same process which calculates J_{i} . An algorithm for finding τ^{i} follows:

- 1. if $\rho^i < 3$ then
- 2. $\tau^i := 0$
- 3. else

- 4. if $\rho^i \% 2 == 0$ then
- 5. $\tau^i := (\rho^i 1) \oplus (\rho^i 1)/2$
- 6. else
- 7. $\tau^i := (\rho^i 2) \oplus (\rho^i 2)/2$
- 8. end if
- 9. end if

 $\bar{\tau}^i$: A byte of n bits obtained by shifting τ^i in exactly the same way as σ^i is derived from $\bar{\sigma}^i$.

derived from $\bar{\sigma}^i$. $\bar{\tau}^i$: A byte of n bits obtained by shifting τ^i in exactly the same way as σ^i is derived from $\bar{\sigma}^i$.