

Next-Generation Technologies Assignment 5- Diffie-Hellman

Problem 1 output and code:

```
Primitive X
"C:\Users\skeha\AppData\Local\Programs\Eclipse Adoptium\jdk-17.0
Smallest primitive root of 13 is 2

Process finished with exit code 0
```

```
Keys
"C:\Users\skeha\AppData\Local\Programs\E
The value of P:23
The value of G:9
The private key a for Alice:4
The private key b for Bob:3
Secret key for the Alice is:9
Secret key for the Bob is:9
```

Keys class:

```
class Keys{

private static long power(long a, long b, long p)
{
    if (b == 1)
        return a;
    else
        return (((long)Math.pow(a, b)) % p);
}

// Driver code
public static void main(String[] args)
{
    long P, G, x, a, y, b, ga, gb;

    // Both the persons will be agreed upon the
    // public keys G and P

    // A prime number P is taken
    P = 13;
    System.out.println("The value of P:" + P);

    // A primitive root for P, G is taken
    G = 6;
    System.out.println("The value of G:" + G);

    // Alice will choose the private key a
    // a is the chosen private key
    a = 5;
    System.out.println("The private key a for Alice:" + a);
```

```

// Gets the generated key
x = power(G, a, P);

// Bob will choose the private key b
// b is the chosen private key
b = 2;
System.out.println("The private key b for Bob:" + b);

// Gets the generated key
y = power(G, b, P);

// Generating the secret key after the exchange
// of keys
ga = power(y, a, P); // Secret key for Alice
gb = power(x, b, P); // Secret key for Bob

System.out.println("Secret key for the Alice is:" + ga);
System.out.println("Secret key for the Bob is:" + gb);
}
}

```

Primitive class:

```

import java.util.*;

class Primitive
{
    // Returns true if n is prime
    static boolean isPrime(int n)
    {
        // Corner cases
        if (n <= 1)
        {
            return false;
        }
        if (n <= 3)
        {
            return true;
        }

        // This is verified so that the below loop can skip the middle five
        // numbers.
        if (n % 2 == 0 || n % 3 == 0)
        {
            return false;
        }

        for (int i = 5; i * i <= n; i = i + 6)
        {
            if (n % i == 0 || n % (i + 2) == 0)
            {
                return false;
            }
        }

        return true;
    }
}

```

```

static int power(int x, int y, int p)
{
    int res = 1;    // Initialize result

    x = x % p; // Update x if it is more than or equal to p

    while (y > 0)
    {
        // If y is odd, multiply x with result
        if (y % 2 == 1)
        {
            res = (res * x) % p;
        }

        // y must be even now
        y = y >> 1; // y = y/2
        x = (x * x) % p;
    }
    return res;
}

// function to store prime factors of a number
static void findPrimefactors(HashSet<Integer> s, int n)
{
    // Print the number of 2s that divide n
    while (n % 2 == 0)
    {
        s.add(2);
        n = n / 2;
    }

    // n must be odd at this point. So we can skip one element
    for (int i = 3; i <= Math.sqrt(n); i = i + 2)
    {
        // While i divides n, print i and divide n
        while (n % i == 0)
        {
            s.add(i);
            n = n / i;
        }
    }

    // This condition is to handle the case when n is a prime number
    // greater than 2
    if (n > 2)
    {
        s.add(n);
    }
}

// Function to find smallest primitive root of n
static int findPrimitive(int n)
{
    HashSet<Integer> s = new HashSet<Integer>();

    // Check if n is prime or not
    if (isPrime(n) == false)
    {

```

```

        return -1;
    }

    // Find value of Euler Totient function of n
    // Since n is a prime number, the value of Euler
    // Totient function is n-1 as there are n-1
    // relatively prime numbers.
    int eul = n - 1;

    // Find prime factors of eul and store in a set
    findPrimefactors(s, eul);

    // Check for every number from 2 to eul
    for (int r = 2; r <= eul; r++)
    {
        // Iterate through all prime factors of eul.
        // and check if we found a power with value 1
        boolean flag = false;
        for (Integer a : s)
        {
            // Check if  $r^{(eul)/\text{primefactors}} \bmod n$ 
            // is 1 or not
            if (power(r, eul / (a), n) == 1)
            {
                flag = true;
                break;
            }
        }

        // If there was no power with value 1.
        if (flag == false)
        {
            return r;
        }
    }

    // If no primitive root found
    return -1;
}

// Driver code
public static void main(String[] args)
{
    int n = 13;
    System.out.println(" Smallest primitive root of " + n
        + " is " + findPrimitive(n));
}
}

```

Problem 2 output and code:

```
"C:\Users\skeha\AppData\Local\Programs\Eclipse Adoptium\jdk-17
The value of P: 13
The value of G: 6

The private key a for Alice: 997
The private key b for Bob: 554

Mallory selected private number for Alice: 72
Mallory selected private number for Bob: 134

Secret key for the Alice is: 7
Secret key for the Bob is: 7

Secret key for Mallory for Alice is: 5
Secret key for Mallory for Bob is: 9

Alice computed (S1): 3
Mallory computed key for Alice (S1): 3

Bob computed (S2): 4
Mallory computed key for Bob (S2): 4

Process finished with exit code 0
```

```
class Mitm {
    private static long power(long a, long b, long p) {
        if (b == 1)
            return a;
        else
            return (((long) Math.pow(a, b)) % p);
    }

    public static void main(String[] args) {
        long P, G, x, a, y, b, z, c, w, d, ga, gb, gc, gd, S1, S2;

        // A prime number P is taken
        P = 13;
        System.out.println("The value of P: " + P);

        // A primitive root for P, G is taken
        G = 6;
        System.out.println("The value of G: " + G + "\n");
    }
}
```

```

        // Alice will choose the private key a
        // a is the chosen private key
        a = 5;
        System.out.println("The private key a for Alice(a): " + a);

        // Gets the generated key
        x = power(G, a, P);

        // Bob will choose the private key b
        // b is the chosen private key
        b = 2;
        System.out.println("The private key b for Bob(b): " + b + "\n");

        // Gets the generated key
        y = power(G, b, P);

        // Mallory will choose two random numbers (c)
        c = 72;
        System.out.println("Mallory selected private number for Alice(c): "
+ c);

        // Gets the generated key
        z = power(G, c, P);

        // Mallory will choose two random numbers (d)
        d = 134;
        System.out.println("Mallory selected private number for Bob(d): " +
d + "\n");

        // Gets the generated key
        w = power(G, d, P);

        ga = power(y, a, P); // Secret key for Alice
        gb = power(x, b, P); // Secret key for Bob
        gc = power(w, c, P); // Secret key from mallory for Alice
        gd = power(z, d, P); // Secret key from mallory for Bob

        S1 = power(G, d, a)%P; // Alice
        S2 = power(G, c, b)%P; // Bob

        System.out.println("Secret key for Alice is(ga): " + ga);
        System.out.println("Secret key for Bob is(gb): " + gb + "\n");
        System.out.println("Eve published value for Alice (gc): " + gc);
        System.out.println("Eve published value for Bob (gd): " + gd +
"\n");

        System.out.println("Alice computed (S1): " + S1);
        System.out.println("Mallory computed key for Alice (S1): " + S1 +
"\n");

        System.out.println("Bob computed (S2): " + S2);
        System.out.println("Mallory computed key for Bob (S2): " + S2);

    }
}

```