SkePU-3 User Guide

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Chapter 1

SkePU User Guide

Revision history

- 2019-09-25 First Exa2Pro release.
- 2019-11-20 Second Exa2Pro release. Revised installation instructions. Updated SkePU 3 changes.
- 2020-01-29 Third Exa2Pro release. Updated to reflect changes in SkePU API and implementation progress.
- 2020-04-29
 Fourth Exa2Pro release. Updated with new skeleton MapPairsReduce and changes to backend selection process.
- 2020-05-20 Separate document for public SkePU 3 user guide. Refactored changelog into the user guide proper.

1.1 Introduction

This chapter gives a high-level introduction to programming with SkePU. The version of SkePU documented here is a developement release of SkePU 3, a source-breaking update from SkePU 2. SkePU is a skeleton programming framework for multicore and multi-GPU systems with a C++11 interface. It includes data-parallel skeletons such as Map and Reduce generalized to a flexible programming interface. SkePU emphasizes and improves on flexibility, type-safety and syntactic clarity over its predecessor, while retaining efficient parallel algorithms and smart data movement for hgh-performance and energy-efficient computation.

SkePU is structured around a source-to-source translator (precompiler) built on top of Clang libraries, and thus requires the LLVM and Clang source when building the compiler driver.

All user-facing types and functions in the SkePU API are defined in the skepu namespace. Nested namespaces are not part of the API and should be considered implementation-specific. The skepu:: qualifier is implicit for all symbols in this document.

1.2 License

SkePU is distributed as open source and licensed under a modified BSD 4-clause licence. The copyright belongs to the individual contributors.

1.3 Authors and Maintainers

The original SkePU was created by Johan Enmyren and Christoph Kessler [5]. A number of people has contributed to SkePU, including Usman Dastgeer.

The major revision SkePU 2 was designed by August Ernstsson, Lu Li and Christoph Kessler [6]. The major revision towards SkePU 3 was designed by August Ernstsson, Christoph Kessler, Johan Ahlqvist, and Suejb Memeti with input from partners in the EXA2PRO project. [6].

August Ernstsson¹ is the current maintainer of SkePU.

1.3.1 Acknowledgements

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We also acknowledge the National Supercomputer Centre (NSC) and SNIC for providing access to HPC cluster systems used for performance testing (SNIC 2016/5-6).

1.4 Dependencies and Requirements

SkePU is fundamentally structured around C++11 features and thus requires a mature C++11 compiler. It has been tested with relatively recent versions of Clang and GCC, and NVCC version 9.

It also uses the STL, including C++11 additions. It has been tested with libstdc++ and libc++. SkePU does not depend on other libraries.

SkePU requires the LLVM and Clang source when building the source-to-source translator. The translator produces valid C++11, OpenCL and/or CUDA source code and can thus be used on a separate system than the target if necessary ("cross-precompilation").

The StarPU MPI backend requires a recent GCC compiler, an OpenMP library, an MPI library (tested with OpenMPI version 2.1), and StarPU built from the master branch.

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1.5 Example

We will introduce the SkePU syntax with an example.

Listing 1.1: Example SkePU 3 userfunction: A linear congruential generator.

```
#include <iostream>
#include <cmath>
#include <skepu>
// Unary user function
float square(float a)
        return a * a;
}
// Binary user function
float mult(float a, float b)
        return a * b;
// User function template
template < typename T >
T plus(T a, T b)
        return a + b;
}
// Function computing PPMCC
float ppmcc(skepu::Vector<float> &x, skepu::Vector<float> &y)
        // Instance of Reduce skeleton
        auto sum = skepu::Reduce(plus<float>);
        // Instance of MapReduce skeleton
        auto sumSquare = skepu::MapReduce<1>(square, plus<float>);
        // Instance with lambda syntax
        auto dotProduct = skepu::MapReduce<2>(
                 [] (float a, float b) { return a * b; },
                 [] (float a, float b) { return a + b; }
        );
        size_t N = x.size();
        float sumX = sum(x);
        float sumY = sum(y);
        return (N * dotProduct(x, y) - sumX * sumY)
                / sqrt((N * sumSquare(x) - pow(sumX, 2)) * (N * sumSquare(y) - pow(sumY, 2)))
}
int main()
        const size_t size = 100;
        // Vector operands
        skepu::Vector<float> x(size), y(size);
        x.randomize(1, 3);
        y.randomize(2, 4);
        std::cout << "X:_{\sqcup}" << x << "n";
        std::cout << "Y:" << y << "\n";
        float res = ppmcc(x, y);
        std::cout << "res:" << res << "\n";
        return 0;
}
```

1.6 Installation

In Section 1.6.1 we will look at building and installing the clang-based version of SkePU tool. The installation and use process for SkePU is still in a prototype state.

1.6.1 Clang based skepu-tool

There are three steps to do when building skepu-tool from source:

- Getting the source
- Build skepu-tool
- Install skepu-tool

Getting the source

The source code is available at https://github.com/skepu/skepu. The repository uses submodules for it's in source dependencies on other projects. Either use git clone --recursive to clone the submodules at the same time as the SkePU repository, or git submodule update --init to fetch the submodules within an already cloned SkePU repository.

Building skepu-tool

New for skepu-tool is the move from a Makefile to a CMake based build procedure. The CMake scripts requires CMake version 3.13 or later. Best practice is to create an out of source build folder. In the following code snippet, we will use <src>/build. The following commands will build skepu-tool:

```
mkdir build && cd build
cmake -DCMAKE_BUILD_TYPE=Release ..
make
```

A couple of notable build options:

Option name	Default value	Description
SKEPU_ENABLE_TESTING	OFF (Release)	Enables the test suite
	on (Debug)	for skepu-tool.
SKEPU_BUILD_EXAMPLES	OFF (Release)	Enables building skepu
	on (Debug)	examples

For more build options, run cmake -LAH.

1.7 Usage

The source-to-source translator tool skepu-tool accepts as arguments:

- input file path: -name <filename>,
- output directory: -dir <directory>,
- output file name: <filename> (without file extension),
- any combination of backends to be generated: -cuda -opencl -openmp.

A complete list of supported flags, and further instructions, can be found by running **skepu-tool**-help on the clang based skepu-tool.

Note that code for the sequential backend is always generated.

SkePU programs (source files) are written as if a sequential implementation—without source translation—was targeted. In fact, such an implementation exists and is automatically selected if non-transformed source files are compiled directly. Make sure to #include header skepu, which contains all of the SkePU library².

Please look at the included example programs and Makefiles to get an idea of how everything works in practice.

Include directories

The Clang based skepu-tool uses Clang libraries and will perform an actual parse to be able to properly analyze and transform the source code; still, it is not a fully-featured compiler as you would get with a pre-configured package of, e.g., Clang or GCC. This has consequences when it comes to locating platform and system-specific include directories, as these have to be specified explicitly.

By adding the -- token to the arguments list, you signal that any remaining arguments should be passed directly to the underlying Clang engine. These arguments are formatted as standard Clang arguments. The required arguments are as follows:

- -std=c++11;
- include path to Clang's compiler-specific C++ headers,
 - -I <path_to_skepu>/lib/SkePU/clang-headers, where the path is the root of the Clang sources (typically in the tools directory in the LLVM tree);
- include path to the SkePU source tree: -I <path_to_skepu>/include;
- include path(s) to the C++ standard library, platform-specific;
- additional flags as necessary for the particular application, as if it was being compiled.

Debugging

Standard debuggers can be used with SkePU. Per default, SkePU does not use or require exceptions, and reports internal fatal errors to stderr and terminates. For facilitating debugging, defining the SKEPU_ENABLE_EXCEPTIONS macro will instead cause SkePU to report these errors by throwing exceptions. This should *not* be used for error recovery in release builds, as the internal state of SkePU is not consistent after an error. (The types of errors reported this way are mostly related to GPU management.)

1.7.1 StarPU MPI

To use the StarPU MPI backend, precompile the source with the flags -openmp -starpu-mpi. If only the Map skeleton is used in a program, one can also enable the cuda backend. Do not forget to add the link flags and include flags that is needed to compile StarPU codes.

When using the SkePU StarPU MPI backend, do not forget to make sure the code is safe to execute on multiple ranks at the same time. The skepu::external function can be used to make a region of code safe. Writing to file is one example where multiple nodes cannot execute the same region at the same time.

 $^{^{2}}$ Almost everything in SkePU is templates, so there is no penalty from including skeletons etc., which are not used.

1.7.2 Clang skepu-tool and CMake

The clang skepu-tool offers a CMake function to automatically configure the precompilation step. The syntax is as follows:

```
skepu_add_executable(<name> [EXCLUDE_FROM_ALL]
  [[[CUDA] [OpenCL] [OpenMP]] | [MPI]]
  SKEPUSRC ssrc1 [ssrc2 ...]
  [SRC src1 [src2 ...])
```

The function is a wrapper around add_executable that will generate precompilation targets for the SkePU sources listed as argument. Any include directories added via target_include_directory or target_link_library will propagate to the precompilation targets as well. The MPI backend option to skepu add executable implies OpenMP.

To be able to use the function, add find_package(SkePU) to the CMakeLists.txt file. If SkePU is not installed in a path that CMake is aware of, one adds the argument HINTS <skepu_prefix> to find_package.

1.8 Limitations

The following section details limitations as of 2020-05-20.

1.8.1 SkePU general

Known issues with the SkePU headers:

- MapOverlap (all) code generation is disabled for OpenCL (Section 1.10.5).
- MapOverlap (3D, 4D) code generation is disabled for CUDA (Section 1.10.5).
- MapPairsReduce code generation is disabled for CUDA and OpenCL (Section 1.10.7).
- Multi-valued return (Section 1.11.1) is not implemented for MapOverlap.
- Multi-valued return is disabled for CUDA and OpenCL.
- Scan is missing OpenMP backend selection parameters (thread count, scheduling mode).

1.8.2 StarPU-MPI skeleton backends

The StarPU MPI backend is not very well tested yet. The following list are known issues:

- The containers are not be fully compatible with the normal version of SkePU.
- The skeleton Call is missing.
- Only the Map, MapPairs, and Reduce skeletons has support for CUDA and applications that use other skeletons cannot have CUDA and StarPU-MPI enabled at the same time.

1.8.3 Clang SkePU tool

In addition, not all combinations of skeleton features are implemented/tested for this release.

1.9 Definitions

Please read through this section once to familiarize yourself with the terms used in this document. It can then be used as a reference, as the terms defined here are typeset in *italics* at first mention in each section.

- **Skeleton** A computation structure on *containers*, e.g. map or reduce. The skeletons in SkePU 2 are all data-parallel, i.e., the computation graph is directed by the structure of container parameters and not dependent on the value of individual elements in a container.
- **Container** An object of some SkePU container class, i.e., vector or matrix. Homogenous; contains objects of a single *scalar* type. In this document, the term container refers exclusively to SkePU containers (as opposed to, e.g., raw data pointers or STL vectors).
- Scalar The type of elements in a *container*. May be a fundamental type such as float, double or int or a compound struct type satisfying certain rules. (Note that the compound types are still referred to as scalar types when in containers.)
- **User function** An operation performed repeatedly (perhaps in parallel) in a *skeleton instance*. A user function in SkePU should not contain side effects, with the exeption of writing to *random access arguments*.
- **Skeleton instance** An object of some skeleton type instantiated with one or more user functions. May include state such as
 - backend specification,
 - execution plan, and
 - skeleton-specific parameters such as the starting value for a reduction.
- **Skeleton invocation** The process of applying a *skeleton instace* to a set of parameters. Performs some computation as specified by the instance's *skeleton* type and *user function*.
- **Output argument** For the *skeletons* which return a *container*, this container is passed as the first argument in a *skeleton invocation*. If the skeleton instead returns a *scalar*, no argument is passed and the value is instead the evaluated value of the invocation expression (i.e., the return value).
- **Element-wise parameter/argument** A container argument to a skeleton instace, elements of which, during skeleton invocation, is passed to the corresponding user function parameter as a scalar value. Iterators into containers can also be used for these parameters, with
- Random access parameter/argument A container argument to a skeleton instace, which, during skeleton invocation, is passed to the corresponding user function parameter and av.
- Uniform parameter/argument A scalar argument to a skeleton invocation, passed unaltered to each user function call.
- Backend The compute units and/or programming interface to use when executing a skeleton
- **Backend specification** An object of type BackendSpec. Encodes a backend (e.g., OpenMP) along with backend-specific parameters for execution (e.g., number of threads) for use by a skeleton instance. Overrides execution plans when selecting backends.
- **Tuning** The process of training a *skeleton instance* on differently sized input data to determine the optimal *backend* in each case.

Execution plan Generated during tuning and stored in a skeleton instance. Helps select the proper backend for a certain input size.

Source-to-source translator / precompiler (skepu-tool) Clang-based tool which transforms SkePU programs for parallel execution. Accepts C++11 code as input and produces C++11/CUDA/OpenCL/OpenMP code as output. Built by user from Clang sources, patched with SkePU-provided extensions.

Host compiler User-provided C++11/CUDA compiler which performs the final build of a SkePU program, producing an executable. Can also be used on raw (non-precompiled) SkePU source for a sequential executable.

1.10 Skeletons

SkePU (3) encompasses currently eight different skeletons:

- Map,
- Reduce,
- MapReduce,
- Scan,
- MapOverlap,
- MapPairs,
- MapPairsReduce, and
- Call.

Each skeleton except for Call encodes a computational pattern which is efficiently parallelized. In general, the skeletons are differentiated enough to make selection obvious for each use case. However, there is some overlap; for example, MapReduce is an efficient combination of Map and Reduce in sequence. This makes Reduce a special case of MapReduce.

Most of the skeletons are very flexible in how they can be used. All but Reduce and Scan are variadic, and some have different behaviours for one- and two-dimensional computations.

Skeletons in SkePU are instantated by calling factory functions named after the skeletons, returning a ready-to-use skeleton *instance*. The type of this instance is implementation-defined and can only be declared as auto. This has the consequence of an instance not being possible to declare before definition, passed as function arguments, etc., which is important to consider when architecting applications based on SkePU³.

SkePU guarantees, however, that a skeleton instance supports a basic set of operations (a "concept" in C++ parlance).

instance(args...) Invokes the instance with the arguments. Specific rules for the argument list applies to each skeleton.

instance.tune() Performs tuning on the instance.

instance.setBackend(backendspec) Sets a backend specification to be used by the instance and overrides the automatic choice.

³We are considering different solutions to work around this restriction, please contact the SkePU maintainers if this is important for you.

Listing 1.2: Example usage of the Map skeleton.

```
float sum(float a, float b)
{
    return a + b;
}

Vector<float> vector_sum(Vector<float> &v1, Vector<float> &v2)
{
    auto vsum = Map<2>(sum);
    Vector<float> result(v1.size());
    return vsum(result, v1, v2);
}

11 }
```

instance.resetBackend() Clears a backend specification set by setBackend.

instance.setExecPlan(plan) Sets the execution plan manually. The plan should be heapallocated, and ownership of it is immediately transferred to the instance and cannot be dereferenced by the caller anymore.

1.10.1 Map

The fundamental property of Map is that it represents a set of computations without dependencies. The amount of such computations matches the size of the *element-wise* container arguments in the *application* of a Map *instance*. Each such computation is a call to (application of) the user function associated with the Map instance, with the element-wise parameters taken from a certain position in the inputs. The return value of the user function is directed to the matching position in the output container.

Map can additionally accept any number of random access container arguments and uniform scalar arguments.

When *invoking* a Map skeleton, the output container (required) is passed as the first argument, followed by element-wise containers all of a size and format which matches the output container. After this comes all random-access container arguments in a group, and then all uniform scalars. The user function signature matches this grouping, but without a parameter for the output (this is the return value) and the element-wise parameters being scalar types instead. The return value is the output container, by reference.

An example can be found in Listing 1.2

OpenMP Scheduling Modes

The OpenMP backend in SkePU 3 has changed. It is now possible to control the scheduling mode, as the implementation uses the runtime option for OpenMP loop scheduling. The options are static scheduling (default), dynamic scheduling, guided dynamic scheduling or letting the OpenMP runtime decide.

```
skepu::BackendSpec spec{...};

// OpenMP
spec.setBackend(skepu::Backend::Type::OpenMP);
spec.setSchedulingMode(skepu::Backend::Scheduling::Static);
spec.setSchedulingMode(skepu::Backend::Scheduling::Dynamic);
spec.setSchedulingMode(skepu::Backend::Scheduling::Guided);
spec.setSchedulingMode(skepu::Backend::Scheduling::Auto);
spec.setCPUChunkSize(/*int*/);

// CUDA + OpenCL
spec.setBackend(skepu::Backend::Type::CUDA);
spec.setBackend(skepu::Backend::Type::OpenCL);
```

Listing 1.3: Example usage of the Reduce skeleton.

```
float min_f(float a, float b)
{
    return (a < b) ? a : b;
}

float min_element(Vector<float> &v)
{
    auto min_calc = Reduce(min_f);
    return min_calc(v);
}
```

```
spec.setDevices(<int>); // number of GPUs
spec.setGPUThreads(/*int*/);
spec.setGPUBlocks(/*int*/);

// Hybrid
spec.setBackend(skepu::Backend::Type::Hybrid);
spec.setCPUPartitionRatio(/*float*/); // CPU fraction, range [0, 1]
```

1.10.2 Reduce

Reduce performs a standard reduction. Two modes are available: 1D reduction on vectors or matrices and 2D reduction on matrices only. An instance of the former type accepts a vector or a matrix, producing a scalar respectively a vector, while the latter only works on matrices. For matrix reductions, the primary direction can be controlled with a parameter on the instance.

The reduction is allowed to be implemented in a tree pattern, so the user function(s) should be associative.

instance.setReduceMode(mode) Sets the reduce mode for matrix reductions. The accepted values
 are ReduceMode::RowWise (default) or ReduceMode::ColWise.

instance.setStartValue(value) Sets the start value for reductions. Defaults to a default-constructed object, which is 0 for built-in numeric types.

An example can be found in Listing 1.3

Revisions to Reduce Skeleton

The Reduce skeleton and the reduce step of MapReduce is seeing some changes in SkePU 3.

Reduce modes will be revised to not always trigger data rearrangement such as transposition (sublinear extra memory complexity).

A define is available to enable the old behavoir up to a set container size,

```
-DSKEPU REDUCE2DCOL TRANSPOSE SIZE MAX [n].
```

The revisions to MapReduce skeleton includes the availablilty of an additional reduce mode: not only reduction over the entire container span, but also reduction over the innmost dimension (row-wise for matrices).

1.10.3 MapReduce

MapReduce is a combination of Map and Reduce in sequence and offers the most features of both, for example, only 1D reductions are supported.

An instance is created from two user functions, one for mapping and one for reducing. The reduce function should be associative.

Listing 1.4: Example usage of the MapReduce skeleton.

```
float add(float a, float b)
{
    return a + b;
}

float mult(float a, float b)
{
    return a * b;
}

float dot_product(Vector<float> &v1, Vector<float> &v2)
{
    auto dotprod = MapReduce<2>(mult, add);
    return dotprod(v1, v2);
}
```

Listing 1.5: Example usage of the Scan skeleton.

```
float max_f(float a, float b)
{
    return (a > b) ? a : b;
}

Vector<float> partial_max(Vector<float> &v)
{
    auto premax = Scan(max_f);
    Vector<float> result(v.size());
    return premax(result, v);
}
```

instance.setStartValue(value) Sets the start value for reduction. Defaults to a default-constructed object, which is 0 for built-in numeric types.

An example can be found in Listing 1.4

1.10.4 Scan

Scan performs a generalized prefix sum operation, either inclusive or exclusive.

When *invoking* a Scan skeleton, the output container is passed as the first argument, followed by a single input container of equal size to the first argument. The return value is the output container, by reference.

instance.setStartValue(value) Sets the start value for exclusive scan. Defaults to a default-constructed object, which is 0 for built-in numeric types.

An example can be found in Listing 1.5

1.10.5 MapOverlap

MapOverlap is a stencil operation. It is similar to Map, but instead of a single element, a region of elements is available in the user function. The region is passed as a pointer, so manual pointer arithmetic is required to access the data. The pointer points to the center element.

A MapOverlap can either be one-dimensional, working on vectors or matrices (separable computations only) or two-dimensional for matrices. The type is set per-instance and deduced from the user function.

The parameter list for a user function to MapOverlap is important. It always starts with an int, which is the overlap radius in the x-direction. 2D MapOverlap also has another int, which will bind to the y-direction overlap radius. The presence of this parameter is used to deduce that an instance is for 2D. A size_t parameter follows, this is the stride. The next parameter is a pointer to of the contained type, pointing to the center of the overlap region. Random-access container and uniform scalar arguments follow just as in Map and MapReduce.

instance.setOverlap(radius) Sets the overlap radius for all available dimensions.

instance.setOverlap(x_radius , y_radius) For 2D MapOverlap only. Sets the overlap for x and y directions.

instance.getOverlap() Returns the overlap radius: a single value for 1D MapOverlap, a std::pair (x, y) for 2D MapOverlap.

instance.setEdgeMode(mode) Sets the mode to use for out-of-bounds accesses in the overlap region. Allowed values are Edge::Pad for a user-supplied constant value, Edge::Cyclic for cyclic access, or Edge::Duplicate (default) which duplicates the closest element.

instance.setOverlapMode(mode) For 1D MapOverlap: Sets the mode to use for operations on matrices. Allowed values are Overlap::RowWise (default), Overlap::ColWise, Overlap::RowColWise, or Overlap::ColRowWise. The latter two are for separable 2D operations, implemented as two passes of 1D MapOverlap.

instance.setPad(pad) Sets the value to use for out-of-bounds accesses in the overlap region when
 using Edge::Pad overlap mode. Defaults to a default-constructed object, which is 0 for built-in
 numeric types.

Major Revision to MapOverlap Skeleton

To improve upon the usability of MapOverlap, and also to better generalize the syntax to higher-dimensionality smart contaniners (see the addition of tensors in SkePU 3), the interface of MapOverlap user functions has changed.

Before, the signature of a MapOverlap user function was very deliberate with explicit parameters for overlap size, and the smart container data was passed by a raw pointer. This also meant that the addressing into the overlap region was left to the user, and this could be quite tricky to get right.

In SkePU 3, this is now changed by the addition of a new set of smart container proxy classes. Similar to existing Vec, Mat, and the new MatRow (see Section 1.15.3), the RegionND (where N = 1, 2, 3, 4) classes are proxy classes representing an overlap region from a smart container of dimensionality N.

The region object contains members for accessing the overlap size, region.on where n = i, j, k, l. A region object allows element access by using paranthesis notation, with one argument for each dimension. **Note:** the element at position (0, ..., 0) is the center element, and the notation allows

Below are some examples of how to use the new user function syntax. Note that the parameter list after the Section parameter is flexible like before, with any number of random-access and uniform arguments allowed.

access in the range [-overlap, +overlap] (inclusive) for each dimension.

```
float over_1d(skepu::Region1D<float> r, int scale)
{
    return (r(-2)*4 + r(-1)*2 + r(0) + r(1)*2 + r(2)*4) / scale;
}
```

1.10.6 MapPairs

SkePU 3 adds an additional top-level skeleton, **MapPairs**. This skeleton applies a cartesian product-style pattern from *two* Vector<T> sets (note that the templated type may differ across these vectors).

Each cartesian combination of vector set indicies generates one userfunction invocation, the result of which is an element in a Matrix. As in Map, there is an optional Index2D parameter in the user function signature to access this index.

Each vector set may contain an arbitrary number of vector containers, similar to the variadicity of Map. All of the vectors in a set are expected to be of the same size.

MapPairs is only defined for Vector-Matrix application, there is no analog for Matrix-Tensor4 at this point.

Below is a simple example of MapPairs in use.

```
int uf(int a, int b) { return a * b }

void test1(size_t Vsize, size_t Hsize, skepu::BackendSpec spec)
{
    auto pairs = skepu::MapPairs(uf);
    pairs.setBackend(spec);

    skepu::Vector<int> v1(Vsize, 3), h1(Hsize, 7);
    skepu::Matrix<int> res(Vsize, Hsize);
    pairs(res, v1, h1);
}
```

Advanced and more flexible use of MapPairs can be carried out similarly to other SkePU skeletons. For instance, it retains flexibility of Map with regards to variadicity (4-way variadic compared to Map being 3-way):

• Elementwise-V args

- Elementwise-H args
- Random-access args
- Uniform args

A more involved skeleton instance might look like this: auto pairs = skepu::MapPairs<3, 2>(uf2); Note that the skeleton is templated in number of containers for each set ("vertical" and "horizontal" dimensions). A compatible user function can be seen below:

1.10.7 MapPairsReduce

SkePU 3 also adds MapPairsReduce, analogous to MapReduce for MapPairs.

Just like MapReduce, the skeleton is initialized with two user functions: one matching the format of a MapPairs user function, and one meeting the restrictions of a Reduce user function.

MapPairsReduce supports arity <0,0> and up. If the arity is 0 in a dimension, it will determine the size of the intermediate Matrix by the values given in a call to setDefaultSize(<Hsize>, <Vsize>) member function beforehand.

The intermediate Matrix is not guaranteed to be stored in memory at any point.

MapPairsReduce supports two reduce modes, both reduce-to-vector: row-wise and col-wise. See the code example below.

```
int uf(int a, int b)
{
        return a * b;
}
int sum(int lhs, int rhs)
{
        return lhs + rhs;
}
{
        auto mpr = skepu::MapPairsReduce(uf, sum);
        skepu::Vector<int> v1(Vsize), h1(Hsize);
        skepu::Vector<int> resV(Vsize), resH(Hsize);

        mpr.setReduceMode(skepu::ReduceMode::ColWise);
        mpr(resH, v1, h1);

        mpr.setReduceMode(skepu::ReduceMode::RowWise);
        pairs(resV, v1, h1);
}
```

1.10.8 Call

Call is special in that it does not provide any pre-defined structure for computation. It is a way to extend SkePU for computations which does not fit into any skeleton, while still utilizing features such as smart containers and tuning. As such, Call provides a minimal interface.

1.11 Multi-Valued Return from Skeletons and User Functions

1.11.1 Multi-valued Return in User Functions

SkePU 3 introduces tuple-like return functionality for cases where a single skeleton instance requires multiple (element-wise) output containers. This way, multiple return values can be computed by the same user function, operating on the inputs in one sequence, potentially improving data locality compared to two separate skeleton invocations after each other. Though the values are returned in a tuple-like manner, the output containers are completely separate objects. This distinguishes this new feature from the existing use of custom structs as (inputs or) return values, as those are stored in array-of-records format.

To use this feature, specify the return type in the user function signature as skepu::multiple<[basic_type, ...]>, i.e., analogous to std::tuple. Then at the site of the return statement, construct this compound object by skepu::ret([expression, ...]).

Below is an example of a user function utilizing this:

```
skepu::multiple < int, float >
multi_f(skepu::Index1D index, int a, int b, skepu::Vec < float > c, int d)
{
    return skepu::ret(a * b, (float)a / b);
}
```

The skeleton instance declaration and invocation follows the syntax of oridinary Map, but instead of supplying one output container as the first argument, specify several of the correct types and order.

```
skepu::Vector<int> v1(size), v2(size), r1(size);
skepu::Vector<float> e(1);
auto multi = skepu::Map<2>(multi_f);
multi(r1, r2, v1, v2, e, 10);
```

Multi-valued return statements are available in the Map skeleton.

1.12 Multi-Variant User Functions

A new feature in SkePU 3 is the possibility to specify alternative, usually platform-specific, user functions beyond the platform-independent one [8]. This establishes a second level of selection, i.e. nested selection / nested composition. In other words, by adding *multi-variant user functions* to multi-backend skeletons (which are just special predefined multi-variant components) we obtain nested multi-variant components.

There are multiple scenarios where a user function with a singular definition can be too restrictive for the purposes of performance: use cases include algorithms with different trade-offs in time complexity versus memory complexity, instruction set architecture differences such as native double or half precision floating point arithmetics, the existence of SIMD vector instructions, or other hardware-accelerated implementations of common computations. Since these attributes are constrained on the underlying platform, the software-defined code variants must somehow be declared compatible only with the appropriate hardware configurations. For this we employ C++ attributes and the use of XPDL to model the target platform.

Below is a simple SkePU program performing element-wise vector addition:

Listing 1.6: Example: Simple vector addition using Map, with a generic user function.

```
float add(float a, float b) { return a + b; }
int main( int argc, char *argv[] )
{
```

```
const size_t size = N; // multiple of 8
auto vector_sum = skepu::Map<2>(add);
skepu::Vector<float> v1(size), v2(size), res(size);
vector_sum( res, v1, v2 );
}
```

A variant for the user function add, here specialized for systems that support AVX vector instructions, can be defined as follows:

Listing 1.7: Example (cont.): Source code for an alternative user function variant.

```
[[skepu::vectorize(8)]]
void add( float* c, const float *a, const float *b )
{
   __m256 av = _mm256_load_ps(a);
   __m256 bv = _mm256_load_ps(b);
   __m256 cv = _mm256_add_ps(av, bv);
   _mm256_store_ps(c, cv); // return by pointer
}
```

This is placed in a separate file. The presence of this user function variant is made known to SkePU through the use of a manifest file, using the syntax below. A list of variants include the name of the variant, which is also the name of the subdirectory that contains the source code, as well as a compile-time predicate (typically an XPDL query [10]) that determines if the variant is eligible for inclusion by the source-to-source compiler.

Listing 1.8: Example (cont.): Manifest file for user function variant.

```
skepu::VariantList {
    skepu::Variant (
    "add_avx" ,
    skepu::Requires (
    xpdl::includes<xpdl::cpu_1::isa_extensions, xpdl_avx>::value ),
    skepu::Backend::Type::CPU
)
};
```

An XPDL [10] platform description (see Listing 1.9) is then supplied to the SkePU source-to-source compiler and, depending on the attributes in the model, user function variants are either included or removed from the resulting program.

Listing 1.9: Example (cont.): XPDL platform model containing AVX instruction set availability.

```
<?xml version="1.0" encoding="UTF-8"?>
<xpdl:model xmlns:xpdl="http://www.xpdl.com/xpdl_cpu"</pre>
            xmlns:xsi="http://www.w3.org/2001/XMLSchema-instance"
            xsi:schemaLocation="http://www.xpdl.com/xpdl_cpu.xsd">
 <xpdl:component type="cpu" />
 <xpdl:cpu name="Intel_Xeon_Gold_6130"</pre>
           num_of_cores="16'
           num_of_threads="32"
           isa_extensions="avx_avx2">
  <xpdl:group prefix="core_group" quantity="16">
   <xpdl:core frequency="2.1" unit="GHz" />
  <xpdl:cache name="L1" size="32" unit="KiB" set="16" />
  <xpdl:cache name="L2" size="1" unit="MiB" set="16" />
  </xpdl:group>
  <xpdl:cache name="L3" size="22" unit="MiB" set="1" />
  <xpdl:power_model type="power_model_Gold_6130" />
 </xpdl:cpu>
</xpdl:model>
```

See Figure 1.1 for an illustration of the workflow and which source and definition files are required. A SkePU application compiled directly by a C++ compiler ignores any variants, as the feature is purely additive and any variants are defined externally from the main source files.

We refer to our ParCo'19 paper [8], EXA2PRO Deliverable D2.3 or the EXA2PRO Programming Guide for further details.

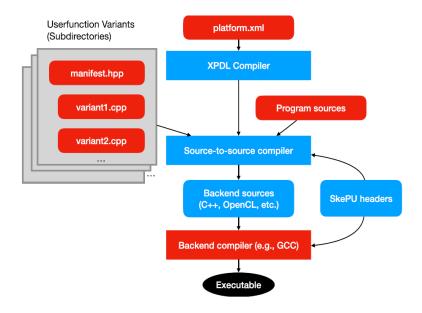


Figure 1.1: Workflow for using multi-variant user functions.

1.13 Manual Backend Selection and Default Settings

1.13.1 Backend Specification API Changes

SkePU 3 changes the backend selection mechanism, in both API and implementation. Especially the OpenMP parameters are expanded with new scheduling mechanisms.

Global Backend Specification

In SkePU 3 it is now possible to set a global backend specification. This specification will be used by default for all skeleton instances. Overriding can be done on an instance basis using a member function, see example.

```
skepu::BackendSpec spec{/*string or SkePU::Backend::Type enum*/};
skepu::setGlobalBackendSpec(spec);
skepu::restoreDefaultGlobalBackendSpec();
skel.setBackend(other_spec); // now overrides global specification
```

1.14 Tuning of Skeleton Instances

A skeleton instance can be tuned for backend selection by going though a process of training on different input sizes of the *element-wise* arguments. This process is automated, but since there is significant overhead (during the tuning process, not afterwards) it has to be started manually. An instance is tuned by calling <code>instance.tune()</code>. Note that this is an experimental feature with limitations. Only the size of element-wise arguments can be used as the tuner's problem size, which is not applicable to all types of computations possible with SkePU.

Tuning creates an internal execution plan which is used as a look-up table during *skeleton invo*cation. It is also possible to construct such a plan manually, and assign it to

1.15 Smart Containers

The smart containers available in SkePU are Vector and Matrix. Using these is mostly transparent, as they will optimize memory management and data movement dynamically between CPU and GPUs.

There is also manual interface for data movement: container.updateHost() will force download of up-to-date data from the GPUs, and container.invalidateDeviceData() forces a re-upload for the next skeleton invocation on a GPU.

Element access on the CPU can be done either with operator[index], which includes overhead for checking remove copies, or operator(index) which provides direct, no-overhead access.

When smart containers are used as *element-wise parameters* to user functions, it is important to note that separate types are used, Vec and Mat. These proxy types do not provide the full smart container functionality and are used with a C-style interface. Elements are retrieved using container.data[index] member, and size, rows, and cols are members and not member functions. By default, the arguments are read/writeable and will encur copy operations both up and down from GPUs; by adding const qualifier, the copy-down is emliminated. Similarly, a [[skepu::out]] attribute will turn them into output parameters.

1.15.1 Smart Container Set

The SkePU container set is extended with tensors, which are higher-dimensionality containers. In SkePU 3 there are tensors of three and four dimensions, complementing the existing 1D "vector" and 2D "matrix". Smart container dimensionality in SkePU 3 is therefore static, though their sizes in each dimension is dynamic.

The interface for these containers are virtually indentical to those of the other containers, differing in the obvious ways of naming and element access detailed below. They are defined as follows:

```
template < typename T > Tensor3 { ... };
template < typename T > Tensor4 { ... };
```

Instances of these tensor types are created with one constructor argument for each dimension. Optionally an additional argument of type T specifices the default value of all elements in the container.

```
skepu::Tensor3<float> t3(dim1, dim2, dim3);
skepu::Tensor4<float> t4(dim1, dim2, dim3, dim4);
```

Compare with existing containers:

```
skepu::Vector<float> v(dim1);
skepu::Matrix<float> m(dim1, dim2);
```

The Index object set in SkePU, useable in e.g. user function signatures, is extended with these structs:

```
struct Index3D { size_t i, j, k; };
struct Index4D { size_t i, j, k, 1; };
```

This complements the existing structs. Note that the naming convention is different for matrix indices for compatibility reasons.

```
struct Index1D { size_t i; };
struct Index2D { size_t row, col; }; // note!
```

Tensor Usage

Tensor3<T> and Tensor4<T> are useable in a way analogous to Matrix<T> in most cases.

Map Over the full domain without regard to dimensionality Optional argument Index3D for Tensor3<T> and Index4D for Tensor4<T> ufs

Reduce Over full domain or over inmost dimension.

MapReduce See Map. For the reduce step, over full domain or the innmost dimension.

Scan Over full domain.

MapOverlap Overlap radius limited to 1 in each dim (default) Larger overlap dependent on backend support.

Call See Map

1.15.2 Smart Container Element Access

SkePU 3 deprecates the angle bracket []-notation for smart container element read/write access outside user functions. This is part of a simplification of the coherency systems for manual element access from the host (CPU) side.

The user should flush the whole container instead before doing single-element accesses of user function data, see Section 1.15.2.

Instead of angle brackets, the parantheses ()-notation is extended to higher dimensionality. This syntax accepts one index argument for each dimension of the underlying container. The indicies count must equal container dimensionality, otherwise there is a compile-time error.

Formally, the syntax is container(i,[j, [k, [1]]]) [= value];

This change means that there's no interface for 1D indexing of higher-dimensionality containers.

There is no longer a coherency-satisfying single-element access mechanism in SkePU smart containers except inside user function proxy objects (Vec<T>, Mat<T>, etc). However, for correctness debugging purposes, there is a macro to enable explicit flush of a container upon access,

-DSKEPU_ALWAYS_UPDATE_HOST_ON_CPU_ELEMENT_ACCESS [0,1],

but note that this has serious performance implications.

Memory Coherency

flush interface revised from feedback from partners flush with options

enum class FlushMode Default, Dealloc ;

FlushMode::Default is implicit if no other value given.

Container member function flush as well as variadic free template function flush

Member function: dynamic flush mode, can be selected at runtime

Free function: flush mode is static constant, known to the compiler (and precompiler)

```
skepu::Vector<int> v1(n), v2(n);
skepu::Matrix<int> m1(n, n), m2(n, n);

v1.flush(); // FlushMode::Default
m1.flush(); // FlushMode::Default
skepu::flush(v2, m2); // FlushMode::Default

v1.flush(skepu::FlushMode::Dealloc);
m1.flush(skepu::FlushMode::Dealloc);
skepu::flush<skepu::FlushMode::Dealloc);</pre>
```

There is no #pragma for flush declarations in SkePU, but the flush (member) functions are compiler-known symbols to the precompiler, as are smart container classes, so the presence or absence of flush operations in SkePU source code is subject to static analysis and optimization.

1.15.3 Matrix-row User Function Proxy Containers

SkePU has since version 2 allowed for flexible parameter lists for user functions, including so-called random-access containers in addition to the for skeleton programming standard element-wise mapped containers. While this allows for powerful expressivity, very little about the access patterns of these random-access containers are known to SkePU, and performance may thus not always be ideal.

One common pattern when using Matrix as a random-access container argument is that each user function invocation is only interested in one row of the matrix. This pattern is seen in matrix-vector multiplication and similar multi-reduction-style computations. To improve SkePU performance in these cases, SkePU 3 introduces a new proxy container object, MatRow<T>. Bridging the gap between element-wise mapped and random-access container arguments, this proxy type when used in a Map skeleton instance that maps over vectors (i.e., the result container(s) of the skeleton are Vector), makes available one single row of the argument matrix container to the user function.

Note: it is required that the matrix container has at least as many rows as the result vector has elements.

Example. Matrix-vector multiplication using MatRow<T> may be implemented as follows:

```
template < typename T>
T arr(const skepu::MatRow < T> mr, const skepu::Vec < T> v)
{
        T res = 0;
        for (size_t i = 0; i < v.size; ++i)
            res += mr.data[i] * v.data[i];
        return res;
}</pre>
```

Compared to the closest corresponding SkePU 2 implementation below (still valid in SkePU 3), the code is more succinct and there is more information about the access pattern available to SkePU.

```
template < typename T>
T arr(skepu::Index1D row, const skepu::Mat<T> m, const skepu::Vec<T> v)
{
        T res = 0;
        for (size_t i = 0; i < v.size; ++i)
            res += m.data[row.i * m.cols + i] * v.data[i];
        return res;
}</pre>
```

There is no change in syntax of skeleton instantiation or skeleton invocation needed for this feature to apply.

Matrix-row user function proxy containers are available in user functions for Map, MapReduce, and MapOverlap skeleton instances that satisfy the above requirements.

1.16 Using Custom Types

It is possible to use custom types in SkePU containers or inside user functions. These types should be C-style structs for compatibility with OpenCL. **Note**: It is not guaranteed that a struct has the same data layout in OpenCL as on the CPU. SkePU does not perform any translation between layouts, so it is the responsibility of the user to ensure that the layout matches.

1.17 Calling Library Functions; Whitelisting

Sometimes, it can be beneficial to call built-in/library functions from inside user functions. By default, SkePU assumes that all called functions are to be processed by the precompiler, which will prevent using library functions, because SkePU does not know in general whether these are available on every accelerator type supported and functionally equivalent to their CPU counterparts.

To avoid this issue, use the -fnames argument of the SkePU precompiler. This flag tells SkePU to ignore any function with this symbol name (all possible overloads), and it is up to the user to ensure that the compiler and linker for each backend can find suitable functions to call.

This feature is useful for whitelisting mathematical functions or printf debugging, but is best used very carefully, especially if accelerator backends are enabled. See the example usage below, as part of the skepu-tool invocation. Multiple function names are separated by whitespace.

```
skepu-tool -fnames "sinucos"
```

1.18 SkePU 3 Changelog

This section goes through all the syntactical and behavioral changes from SkePU 2 to SkePU 3.

In particular, the skeleton set has changed in SkePU 3, with the addition of the all-new MapPairs and MapPairsReduce skeletons, important extensions to the capabilities of the standard Map skeleton, and an interface change to improve usability of the MapOverlap skeleton.

The smart container set has also seen an extension in SkePU 3, the framework now has higher-dimensionality *tensors* in Tensor3 and Tensor4. The coherency model of smart containers has also seen an update.

1.18.1 Namespace Change

The namespace for SkePU is changed in SkePU 3. Historically, the skepu:: namespace was used by the initial SkePU release ("SkePU 1"), and since SkePU 2 was a major source-breaking change from SkePU 1, the decision was made to switch over the namespace as a way to communicate the source incompatibilities.

Today, there is to our knowledge little or no application code in active use which depends on SkePU 1. The decision was therefore made to switch back to the version-agnostic skepu: namespace for new releases of SkePU, starting with SkePU 3. This has the additional benefit of communicating that SkePU 3 also is a source-breaking transition from SkePU 2, although this time the scope of the changes is much smaller and transitioning between SkePU 2 to 3 is expected to be much simpler.

The intention is to keep this namespace for future versions of SkePU, and future source-breaking changes will be communicated in other ways.

The above namespace applies to skeletons and smart containers alike, as well as suporting constructs such as enums, backend specifications, container proxy objects, and index structs. In short, every C++ symbol in the library is affected. The exeption is C++11 attributes, whose names are forced to be namespaced but these namespaces are distinct from the standard C++ namespace definitions. This was introducted to SkePU in version 2 and have always been skepu::, (e.g. [[skepu::out]] and will remain as such.

In addition to the namespace change the default include header (the main entry point to the SkePU header library) has been changed. #include <skepu2.hpp> is replaced by #include <skepu> which aside from dropping the version now also mirrors the standard library with the absence of a file extension. (Note that the include directive may be different depending on the directory setup.)

1.18.2 Other Changes Summary

The following major changes, described in more detail above, have been applied in the transition from SkePU-2 to SkePU-3 (as of May 2020):

- New skeletons MapPairs, MapPairsReduce;
- Revised interface for MapOverlap and Reduce;

- New container types Tensor3, Tensor4 and new container proxy types MatRow, Ten3, Ten4;
- Deprecation of any STL-inherited dynamic features of the SkePU containers as a clarification that they are to be used as static objects;
- Multi-valued return from skeletons and user functions;
- Multi-variant user functions;
- Dynamic scheduling option for all skeletons except Scan and Call;
- New memory consistency model for smart containers: weak consistency;
- New MPI backend (available for some skeletons at this time), along with a new construct (interface still pending) to frame external I/O operations.

Several of these design changes are the result of feedback from application partners in the running H2020 FETHPC project EXA2PRO.

Moreover, the public distribution of SkePU has moved to github.com/skepu/skepu and the SkePU web page has moved from Linköping University to skepu.github.io.

The SkePU license has been changed from GPLv3 for SkePU-2 to a less restrictive modified 4-clause BSD license for SkePU-3.

1.19 More Information about SkePU

For further information about SkePU we refer to our publications.

SkePU 1 was introduced in 2010 and is presented in Enmyren and Kessler [5].

The integration of SkePU and StarPU to provide data-driven dynamic scheduling of asynchronous skeleton calls was presented by Dastgeer et al. [3].

The second generation of a back-end selection tuning framework for SkePU was developed by Dastgeer et al. [4]. Dastgeer also further developed the smart data-containers (Vector, Matrix) in [2]. Selection tuning and smart containers are still contained in today's SkePU implementation.

SkePU 1 supports sequential and multithreaded CPU execution as well as single- and multi-GPU execution in OpenMP and CUDA backends. These backends are, in modified form, still part of today's SkePU implementation. Experimental back-ends for SkePU 1 had also been developed for plain MPI [12] and Movidius Myriad 2 [16], but were not mature enough to be included in the public distribution and were finally abandoned at the transition to SkePU-2.

Case studies on SkePU 1 include the porting of the EDGE flow simulation code [15], which revealed a number of weaknesses in the SkePU 1 API and finally led to the design of SkePU 2.

SkePU 2 was introduced in 2016. It involved the complete redesign of the SkePU programming interface based on C++11, and is described in Ernstsson et al. [9].

The generalization of smart containers for lazy execution of skeletons to provide global run-time optimizations such as tiling and kernel fusion across data-flow graphs of containers and skeletons was presented by Ernstsson and Kessler [7].

A new hybrid CPU-GPU back-end for SkePU 2 was proposed by Öhberg et al. [13] and is included in today's implementation.

The concept of multi-variant user functions and their implementation (included in SkePU-3) is presented in Ernstsson and Kessler [8].

Panagiotou et al. [14] present a case study of using SkePU in a brain modeling application, including first scaling results for the new SkePU 3 cluster backend based on StarPU-MPI [1], which is included in the distribution.

A SkePU tutorial, including most of the new SkePU 3 features, can be found on the SkePU web page [11].

A paper presenting SkePU 3 in its entirety is currently in preparation.

Chapter 2

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