Excitation
$$u(t) = u_1(t) + u_2(t) + u_3(t)$$

$$G(s) = \frac{\beta_1 s^2 + \beta_2 s + \beta_3}{s^2 + \beta_4 s + \beta_5}$$

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$$Output$$

$$y(t)$$

$$Identification$$

$$P(k) = P(k-1) - \frac{P(k-1)\phi(k)\phi^{\tau}(k)P(k-1)}{1+\phi^{\tau}(k)P(k-1)\phi(k)}$$

$$e(k) = z(k) - \phi^{\tau}(k)\hat{\theta}(k-1)$$

$$\theta(k) = \hat{\theta}(k-1) + P(k)\phi(k)e(k)$$

$$T_S \text{ is sampling time, } P(0) = P_0 = P_0^{\tau} > 0,$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ -y(k-1) - y(k-1) - y(k-1) \end{bmatrix}, \theta = \begin{bmatrix} \theta_1 \\ \theta_2 \\ \theta_3 \\ -\alpha_3 \\ -\alpha_4 \\ -\alpha_5 \end{bmatrix}$$

$$Discretized plant model in state space:$$

$$x(k+1) = A_d x(k) + B_d u(k),$$

$$y(k+1) = C_d x(k) + B_d u(k),$$

$$y(k+1) = C_d x(k) + D_d u(k),$$

$$y$$

 $\beta_3 = C_{1,1}(B_{2,1}A_{1,2} - B_{1,1}A_{2,2}) + C_{1,2}(B_{1,1}A_{2,1} - B_{2,1}A_{1,1}) + D_{1,1}(A_{1,1}A_{2,2} - A_{1,2}A_{2,1}),$

 $\beta_1 = D_{1,1}, \beta_2 = C_{1,1}B_{1,1} + C_{1,2}B_{2,1} - D_{1,1}(A_{1,1} + A_{2,2}),$

 $\beta_4 = -(A_{1.1} + A_{2.2}), \text{ and } \beta_5 = A_{1.1}A_{2.2} - A_{1.2}A_{2.1}$