

$$\textcircled{7} \quad \iiint_E x^2 dV \quad x^2 + y^2 = 1 \quad z = 0 \quad z^2 = 4x^2 + 4y^2$$

$$r^2 = 1 \quad z^2 = 4r^2$$

$$r = 1 \quad z = 2r$$

$$\theta \in [0, 2\pi] \quad 0 = 4r^2 \quad z \in [0, 2r]$$

$$r = 0 \quad r \in [0, 1]$$

$$E = \{(r, \theta, z) \mid \theta \in [0, 2\pi] \wedge r \in [0, 1] \wedge z \in [0, 2r]\}$$

$$\int_0^{2\pi} \int_0^1 \int_0^{2r} r^3 \cos^2 \theta \, dz \, dr \, d\theta$$

$$= \int_0^{2\pi} \cos^2 \theta \, d\theta \int_0^1 \left[r^3 z \right]_0^{2r} dr = \int_0^{2\pi} \left[\frac{1}{2} + \frac{1}{2} \cos 2\theta \right] d\theta \int_0^1 2r^4 dr$$

$$= \int_0^{2\pi} \left[\frac{1}{2} + \frac{1}{2} \cos 2\theta \right] d\theta \left[\frac{2}{5} r^5 \right]_0^1 = \frac{2}{5} \int_0^{2\pi} \left[\frac{1}{2} + \frac{1}{2} \cos 2\theta \right] d\theta$$

$$= \frac{2}{5} \left[\frac{\theta}{2} + \frac{\sin 2\theta}{4} \right]_0^{2\pi} = \frac{2}{5} [\pi + 0 - 0 - 0] = \boxed{\frac{2\pi}{5}}$$