

$$(21) \quad 4x^2 - 4y^2 - z^2 = 4$$

$$4y^2 = 4 + 4y^2 + z^2$$

$$x^2 = 1 + y^2 + \frac{z^2}{4}$$

Since part of hyperboloid is in front of yz plane

\Rightarrow

$$x = \sqrt{1 + y^2 + \frac{z^2}{4}}$$

$$y = y \quad z = z$$

$$(25) \quad x^2 + y^2 + z^2 = 36 \quad z = 0 \quad z = 3\sqrt{3}$$

Through spherical coordinates $x = \rho \sin \phi \cos \theta$ $y = \rho \sin \phi \sin \theta$ $z = \rho \cos \phi$

$$\rho^2 = 36 \quad \rho = 6$$

$$x = 6 \sin \phi \cos \theta \quad y = 6 \sin \phi \sin \theta \quad z = 6 \cos \phi$$

$$6 \cos \phi = 0$$

$$\cos \phi = 0$$

$$\phi = \frac{\pi}{2}$$

$$6 \cos \phi = 3\sqrt{3}$$

$$\cos \phi = \frac{\sqrt{3}}{2}$$

$$\phi = \frac{\pi}{6}$$

$$\phi \in \left[\frac{\pi}{6}, \frac{\pi}{2} \right]$$

$$\theta \in [0, 2\pi]$$

$$(33) \quad x = u + v \quad y = 3u^2 \quad z = u - v \quad (2, 3, 0) \quad \vec{u} = \vec{v} = 1$$

$$r_u = \langle 1, 6u, 1 \rangle \quad r_v = \langle 1, 0, -1 \rangle \quad r_u \times r_v = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 6u & 1 \\ 1 & 0 & -1 \end{vmatrix} = \begin{vmatrix} 6u & 1 \\ 0 & 1 \end{vmatrix} - \begin{vmatrix} 1 & 1 \\ 1 & -1 \end{vmatrix} \hat{k} = \langle 6u, 2, -6u \rangle$$

Since $u=1$ normal vector is $\langle -6, 2, -6 \rangle$
equation of plane!

$$(x-2)(-6) + (y-3)(2) + (z)(-6) = 0$$

$$-6x + 12 + 2y - 6 - 6z = 0$$

$$= -6x - 6 - 6z = 0$$

$$\Rightarrow \boxed{3x - y + 3z = 3}$$