

33)  $x^2 + y^2 = 4$   $x \geq 0$  density  $= k = p(x, y)$

$$x = 2 \cos t \quad y = 2 \sin t \quad t \in \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$$

$$\bar{x} = \frac{1}{m} \int_C x p(x, y) ds \quad \bar{y} = \frac{1}{m} \int_C y p(x, y) ds$$

$$m = \int_C p(x, y) ds = \int_C k ds \quad m = k \int_C ds \xrightarrow{\frac{2\pi(2)}{(2)} = 2\pi} m = 2\pi k$$

$$\bar{x} = \frac{k}{m} \int_C x ds \quad ds = \sqrt{4 \sin^2 t + 4 \cos^2 t} = 2 dt$$

$$\bar{x} = \frac{k}{m} \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 2 \cos t dt = \frac{4k}{m} \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \cos t dt = \frac{4k}{m} (\sin t) \Big|_{-\frac{\pi}{2}}^{\frac{\pi}{2}} = \frac{8k}{m}$$

$$\frac{8k}{2\pi k} = \frac{4}{\pi}$$

$$\bar{y} = \frac{k}{m} \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 4 \sin t dt = \frac{4k}{m} \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin t dt = \frac{4k}{m} (-\cos t) \Big|_{-\frac{\pi}{2}}^{\frac{\pi}{2}} = 0$$

mass of wire:  $m = 2\pi k$

center of mass of wire:  $\left(\frac{4}{\pi}, 0\right)$