

$$(15) F(x,y,z) = \langle z \cos y, xz \sin y, x \cos y \rangle$$

$$\text{curl } F = \langle (-\cancel{x} \sin y - x \sin y), (\cancel{z} \cos y - \cos y), (z \sin y + z \sin y) \rangle$$

$$= \langle -2x \sin y, 0, 2z \sin y \rangle \neq \langle 0, 0, 0 \rangle \quad \boxed{\text{Not conservative}}$$

$$(17) F(x,y,z) = \langle e^{yz}, xz e^{yz}, xy e^{yz} \rangle \quad \text{curl } F = \left( \frac{\partial R}{\partial y} - \frac{\partial Q}{\partial z} \right) \mathbf{i} + \left( \frac{\partial P}{\partial z} - \frac{\partial R}{\partial x} \right) \mathbf{j} + \left( \frac{\partial Q}{\partial x} - \frac{\partial P}{\partial y} \right) \mathbf{k}$$

$$\text{curl } F = \langle (x e^{yz} + x z e^{yz}) - (x e^{yz} + x z e^{yz}), (y e^{yz} - y e^{yz}), (z e^{yz} - z e^{yz}) \rangle$$

$$= \langle 0, 0, 0 \rangle = 0 \quad \therefore \text{Conservative}$$

$$f_x = e^{yz} \quad f_y = xz e^{yz} \quad f_z = xy e^{yz}$$

$$f(x,y,z) = x e^{yz} + g(y,z) \quad \frac{\partial f}{\partial y} = xz e^{yz}$$

$$f(x,y,z) = x e^{yz} + g(xy)$$

$$g'(xy) = 0$$

$$g'(y,z) = 0$$

$$F = \int xz e^{yz} dy$$

$$v = xz \quad dv = z dy$$

$$\frac{1}{z} dv = dy$$

$$f(x,y,z) = x e^{yz} + g(x,z)$$

$$g'(x,z) = 0$$

$$g(y,z) = g(x,z) = g(xy) = C$$

$$\boxed{\text{Conservative vector field. } f(x,y,z) = x e^{yz} + C}$$