

$$⑦ \quad x = \sqrt{t^2+3} \quad y = \ln(t^2+3) \quad z = t \quad (2, \ln 4, 1) \quad t=1$$

$$r(t) = \langle \sqrt{t^2+3}, \ln(t^2+3), t \rangle$$

$$r'(t) = \left\langle \frac{t}{\sqrt{t^2+3}}, \frac{2t}{t^2+3}, 1 \right\rangle$$

$$r'(1) = \left\langle \frac{1}{2}, \frac{1}{2}, 1 \right\rangle$$

$$r = r_0 + t r'(1) = \langle 2, \ln 4, 1 \rangle + t \left\langle \frac{1}{2}, \frac{1}{2}, 1 \right\rangle$$

$$r = \left\langle 2 + \frac{1}{2}t, \ln 4 + \frac{1}{2}t, 1+t \right\rangle$$

$$\boxed{x = 2 + \frac{1}{2}t \quad y = \ln 4 + \frac{1}{2}t \quad z = 1+t}$$

$$⑧ \quad r(t) = \langle t^2, \ln t, t \ln t \rangle \quad (1, 0, 0) \quad \ln(t) = 0 \quad t = e^0 = 1$$

$$r'(t) = \left\langle 2t, \frac{1}{t}, 1 + \ln t \right\rangle$$

$$r'(1) = \langle 2, 1, 1 \rangle$$

$$|r'(t)| = \sqrt{4t^2 + \frac{1}{t^2} + (1 + \ln t)^2}$$

$$|r'(1)| = \sqrt{4 + 1 + 1} = \sqrt{6}$$

$$r''(t) = \left\langle 2, -\frac{1}{t^2}, \frac{1}{t} \right\rangle$$

$$r''(1) = \langle 2, -1, 1 \rangle$$

$$r'(1) \times r''(1) = \begin{vmatrix} i & j & k \\ 2 & 1 & 1 \\ 2 & -1 & 1 \end{vmatrix} = \begin{vmatrix} 1 & 1 \\ -1 & 1 \end{vmatrix} i - \begin{vmatrix} 2 & 1 \\ 2 & 1 \end{vmatrix} j + \begin{vmatrix} 2 & 1 \\ 2 & -1 \end{vmatrix} k = \langle 2, 0, -4 \rangle$$

$$|\langle 2, 0, -4 \rangle| = \sqrt{4 + 16} = \sqrt{20}$$

$$k(1) = \frac{\sqrt{20}}{(\sqrt{6})^3} = \frac{2\sqrt{5}}{6\sqrt{6}} = \frac{\sqrt{5}}{3\sqrt{6}} = k(1)$$