

$$(27) \quad 2x + y + z = 4$$

$$z = 4 - 2x - y$$

$$x=2 \quad (2, 0, 0)$$

$$y=4 \quad (0, 4, 0)$$

$$z=0, \quad y=4-2x$$

$$D = \{(x, y) \mid x \in [0, 2] \wedge y \in [0, 4-2x]\}$$

$$\int_0^2 \int_0^{4-2x} (4-2x-y) \, dy \, dx = \int_0^2 \left[4y - 2xy - \frac{1}{2}y^2 \right]_0^{4-2x} dx$$

$$= \int_0^2 \left(4(4-2x) - 2x(4-2x) - \frac{1}{2}(4-2x)^2 \right) dx = \int_0^2 (2x^2 - 8x + 8) dx$$

$$= \frac{2}{3}(2^3) - 4(2)^2 + 8(2) = \frac{2(8)}{3} = \boxed{\frac{16}{3}}$$

$$(31) \quad x^2 + y^2 = 1 \quad y = z \quad x=0 \quad z=0$$

$$y = \sqrt{1-x^2}$$

$$D = \{(x, y) \mid x \in [0, 1] \wedge y \in [0, \sqrt{1-x^2}]\}$$

$$\text{if } y=0 \quad x^2=1 \\ x=\pm 1 \\ x=1$$

$$\int_0^1 \int_0^{\sqrt{1-x^2}} y \, dy \, dx = \int_0^1 \left[\frac{1}{2}y^2 \right]_0^{\sqrt{1-x^2}} dx = \int_0^1 \left(\frac{1}{2} - \frac{1}{2}x^2 \right) dx$$

$$= \left[\frac{1}{2}x - \frac{1}{6}x^3 \right]_0^1 = \frac{1}{2} - \frac{1}{6} = \boxed{\frac{1}{3}}$$