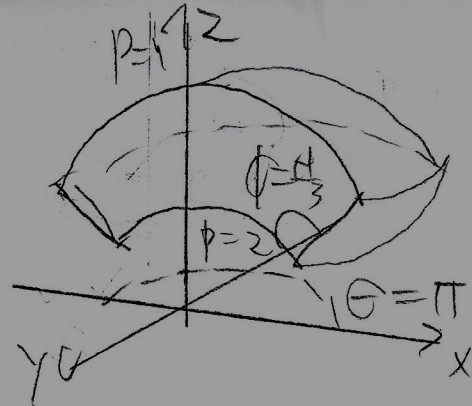


$$(13) \quad \rho \in [2, 4] \quad \phi \in [0, \frac{\pi}{3}] \quad \theta \in [0, \pi]$$



$$(15) \quad z = \sqrt{x^2 + y^2} \quad x^2 + y^2 + z^2 = z$$

$$x^2 + y^2 + z^2 = z$$

$$\rho^2 \sin^2 \phi + \rho^2 \cos^2 \phi = \rho \cos \phi$$

$$\rho^2 = \rho \cos \phi$$

$$\rho = \cos \phi$$

$$\rho = \frac{\sqrt{2}}{2}$$

$$z = \sqrt{x^2 + y^2}$$

$$\rho \cos \phi = \sqrt{\rho^2 \sin^2 \phi} (1)$$

$$\rho \cos \phi = \rho \sin \phi$$

$$1 = \tan \phi$$

$$\phi = \frac{\pi}{4}$$

$$\boxed{\phi \in [0, \frac{\pi}{4}] \quad \rho \in [0, \cos \phi]}$$

$$(17) \quad \int_0^{\frac{\pi}{6}} \int_0^{\frac{\pi}{2}} \int_0^3 \rho^2 \sin \phi \, d\rho \, d\theta \, d\phi = \int_0^{\frac{\pi}{6}} \sin \phi \, d\phi \int_0^{\frac{\pi}{2}} d\theta \int_0^3 \rho^2 \, d\rho$$

$$= \left(-\cos \phi \right) \Big|_0^{\frac{\pi}{6}} \left(\frac{\pi}{2} \right) \left(\frac{27}{3} - 0 \right) = \frac{9\pi}{2} \left(1 - \cos\left(\frac{\pi}{6}\right) \right) = \frac{9\pi}{2} \left(1 - \frac{\sqrt{3}}{2} \right)$$

$$= \boxed{\frac{9\pi}{4} (2 - \sqrt{3})}$$

$$\phi \in [0, \frac{\pi}{6}] \quad \theta \in [0, \frac{\pi}{2}] \quad \rho \in [0, 3]$$

