

$$\textcircled{21} \quad y = x^2 \quad z = 0 \quad y + z = 1$$

$$y \in [x^2, 1] \quad z \in [0, 1-y] \quad 1 = x^2$$

$$x = \pm 1 \quad x \in [-1, 1]$$

$$D = \{(x, y, z) \mid x \in [-1, 1] \wedge y \in [x^2, 1] \wedge z \in [0, 1-y]\}$$

$$V = \int_{-1}^1 \int_{x^2}^1 \int_0^{1-y} dz dy dx = \int_{-1}^1 \int_{x^2}^1 (1-y) dy dx = \int_{-1}^1 \left[ y - \frac{1}{2} y^2 \right]_{x^2}^1 dx$$

$$= \int_{-1}^1 \left( 1 - \frac{1}{2} - x^2 + \frac{1}{2} x^4 \right) dx = \int_{-1}^1 \left( \frac{1}{2} - x^2 + \frac{1}{2} x^4 \right) dx = 2 \left[ \frac{x}{2} - \frac{1}{3} x^3 + \frac{x^5}{10} \right]_0^1$$

$$= 2 \left[ \frac{1}{2} - \frac{1}{3} + \frac{1}{10} \right] = 2 \left[ \frac{1}{6} + \frac{1}{10} \right] = 2 \left[ \frac{16}{60} \right] = \frac{16}{30} = \boxed{\frac{8}{15}}$$

$$\textcircled{25} \quad \iiint_B \cos(xyz) dV \quad B = \{(x, y, z) \mid x \in [0, 1] \wedge y \in [0, 1] \wedge z \in [0, 1]\}$$

$$\Delta V = \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{8} \quad \frac{1}{4}, \frac{3}{4}$$

$$V = \frac{1}{8} \left[ f\left(\frac{1}{4}, \frac{1}{4}, \frac{1}{4}\right) + f\left(\frac{1}{4}, \frac{1}{4}, \frac{3}{4}\right) + f\left(\frac{1}{4}, \frac{3}{4}, \frac{1}{4}\right) + f\left(\frac{1}{4}, \frac{3}{4}, \frac{3}{4}\right) + \right.$$

$$\left. f\left(\frac{3}{4}, \frac{1}{4}, \frac{1}{4}\right) + f\left(\frac{3}{4}, \frac{1}{4}, \frac{3}{4}\right) + f\left(\frac{3}{4}, \frac{3}{4}, \frac{1}{4}\right) + f\left(\frac{3}{4}, \frac{3}{4}, \frac{3}{4}\right) \right]$$

$$= \frac{1}{8} \left[ f\left(\frac{1}{4}, \frac{1}{4}, \frac{1}{4}\right) + 3 f\left(\frac{1}{4}, \frac{1}{4}, \frac{3}{4}\right) + 3 f\left(\frac{3}{4}, \frac{3}{4}, \frac{1}{4}\right) + f\left(\frac{3}{4}, \frac{3}{4}, \frac{3}{4}\right) \right]$$

$$= \frac{1}{8} \left[ \cos\left(\frac{1}{64}\right) + 3 \cos\left(\frac{3}{64}\right) + 3 \cos\left(\frac{9}{64}\right) + \cos\left(\frac{27}{64}\right) \right]$$

$$\approx \boxed{0.985}$$