

7) b.) $\text{div } F = \frac{\partial P}{\partial x} + \frac{\partial Q}{\partial y} + \frac{\partial R}{\partial z} = \boxed{e^x \sin y + e^y \sin z + e^z \sin x}$

9) a) $F = \langle P, Q, R \rangle \quad \text{div } F = \frac{\partial P}{\partial x} + \frac{\partial Q}{\partial y}$

$\frac{\partial P}{\partial x} = 0$ since x components of each vector is 0

$\frac{\partial Q}{\partial y}$ is negative since the y components of each vector is decreasing in length as $y \rightarrow \infty$.

Therefore $\text{div } F = 0 - \frac{\partial Q}{\partial y} = -\frac{\partial Q}{\partial y}$ Divergence is negative

b) $\text{curl } F = \langle 0, 0, \left(\frac{\partial Q}{\partial x} - \frac{\partial P}{\partial y} \right) \rangle =$

$\frac{\partial Q}{\partial x} = 0$ as x components = 0 $\frac{\partial P}{\partial y} = 0$ since x components are 0.

$\text{curl } F = \langle 0, 0, 0 - 0 \rangle = \langle 0, 0, 0 \rangle = \boxed{0}$

11) a) $F = \langle P, Q, R \rangle \quad \text{div } F = \frac{\partial P}{\partial x} + \frac{\partial Q}{\partial y}$

$\frac{\partial P}{\partial x} = 0$ as x components have same length as $x \rightarrow \infty$.

$\frac{\partial Q}{\partial y} = 0$ since y components of the vectors are 0.

$\text{div } F = 0 + 0 = \boxed{0}$