

$$(9) \int_C x^2 y \, ds \quad x = \cos t \quad y = \sin t \quad z = t \quad t \in [0, \frac{\pi}{2}]$$

$$\sqrt{\cos^2 t + \sin^2 t + 1^2} = \sqrt{1 + 1} \, dt = \sqrt{2} \, dt = ds$$

$$\int_0^{\frac{\pi}{2}} \cos^2 t + \sin t \sqrt{2} \, dt$$

$$\sqrt{2} \int_0^{\frac{\pi}{2}} \cos^2 t + \sin t \, dt$$

$$v = \cos t \\ dv = -\sin t \, dt \\ -dv = \sin t \, dt$$

$$\sqrt{2} \int_0^1 v^2 \, dv = \sqrt{2} \left(\frac{1}{3} (1-0) \right) = \boxed{\frac{\sqrt{2}}{3}}$$

$$(11) \int_C x e^{yz} \, ds \quad (0,0,0) \quad (1,2,3) \quad r(t) = \langle t, 2t, 3t \rangle \quad t \in [0,1]$$

$$\int_0^1 t e^{6t^2} \sqrt{14} \, dt$$

$$v = 6t^2 \\ dv = 12t \, dt \\ \frac{1}{12} dv = t \, dt$$

$$r'(t) = \langle 1, 2, 3 \rangle \\ |r'(t)| = \sqrt{14} \, dt = ds$$

$$\frac{\sqrt{14}}{12} \int_0^6 e^v \, dv = \boxed{\frac{\sqrt{14}}{12} (e^6 - 1)}$$

$$(13) \int_C x y e^{yz} \, dy \quad x=t \quad y=t^2 \quad z=t^3 \quad t \in [0,1] \\ dy = 2t \, dt$$

$$\int_0^1 t^3 e^{t^5} 2t \, dt = 2 \int_0^1 t^4 e^{t^5} \, dt$$

$$v = t^5 \\ dv = 5t^4 \, dt \\ \frac{2}{5} dv = t^4 \, dt$$

$$= \frac{2}{5} \int_0^1 e^v \, dv \\ = \boxed{\frac{2}{5} (e - 1)}$$