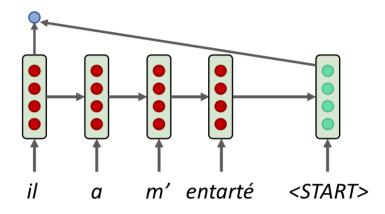
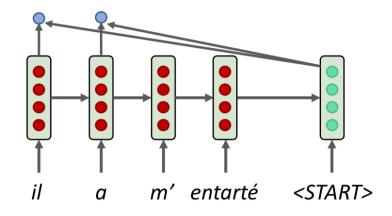
# Deep Learning and Applications

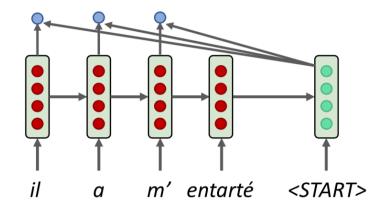
- Compute attention scores given some function  $\alpha$ 
  - Encoder hidden state  $h_1$
  - Decoder hidden state  $s_1$
  - $\rightarrow$  Attention score  $a_{11} = f(h_1, s_1)$



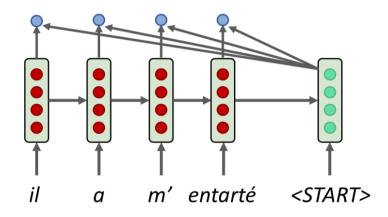
- Compute attention scores given some function  $\alpha$ 
  - Encoder hidden state  $h_2$
  - Decoder hidden state  $s_1$
  - $\rightarrow$  Attention score  $a_{12} = f(h_2, s_1)$



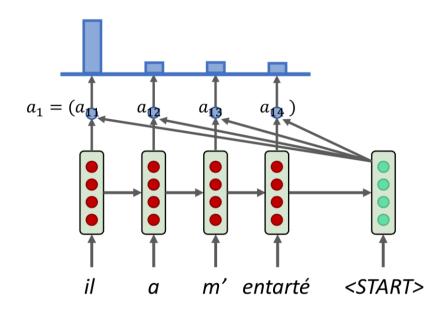
- Compute attention scores given some function  $\alpha$ 
  - Encoder hidden state  $h_3$
  - Decoder hidden state  $s_1$
  - $\rightarrow$  Attention score  $a_{13} = f(h_3, s_1)$



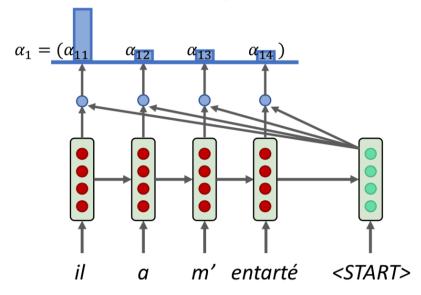
- Compute attention scores given some function  $\alpha$ 
  - Encoder hidden state  $h_4$
  - Decoder hidden state  $s_1$
  - $\rightarrow$  Attention score  $a_{14} = f(h_4, s_1)$

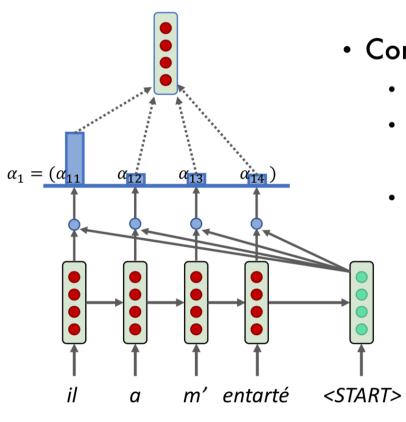


• Convert attention scores into a distribution by softmax.

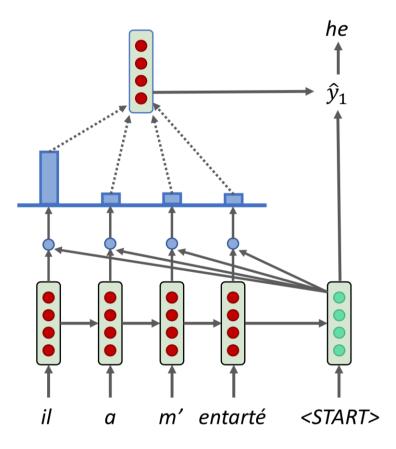


- Convert attention scores into a distribution by softmax.
  - $\alpha_1 = softmax(a_1)$
  - We are mostly focusing on the encoder's 1st hidden state  $h_1$ .



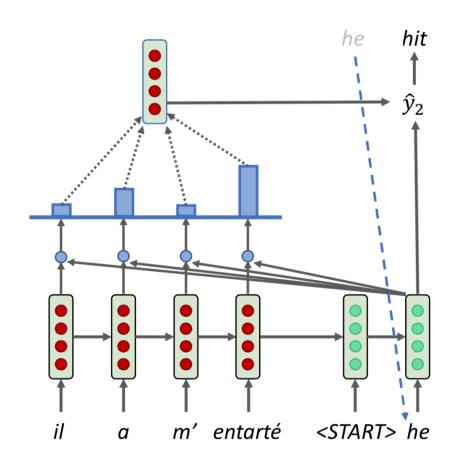


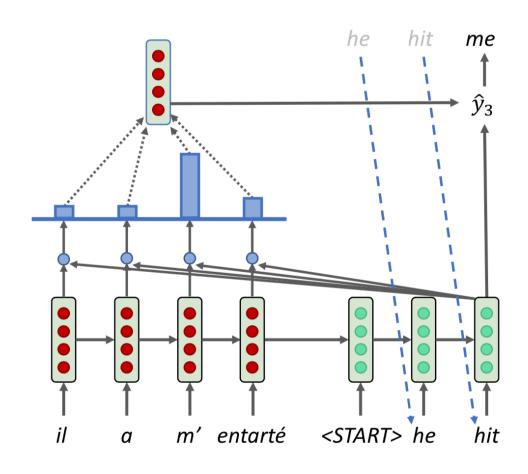
- Compute the attention output  $z_1$ .
  - Weighted sum of hidden states.
  - $z_1 = \sum_{t=1}^4 \alpha_{1t} h_t$
  - Attention output contains information of every hidden state proportionally to attention distribution  $\alpha$ .

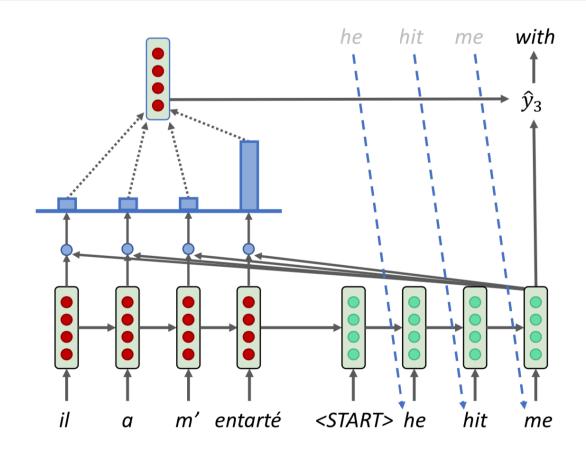


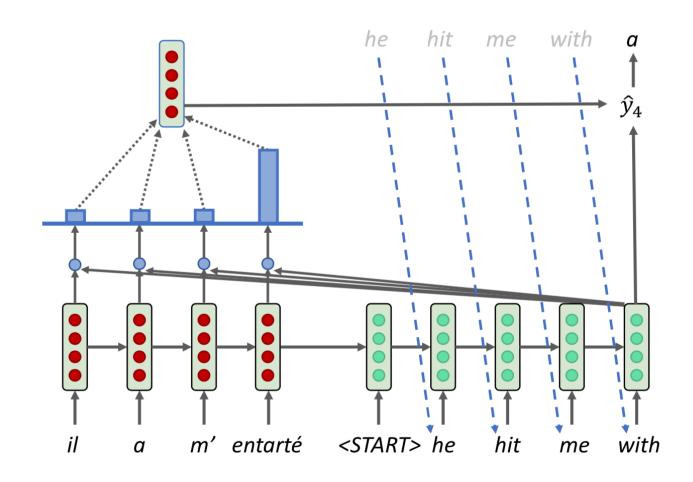
#### Concatenate then generate

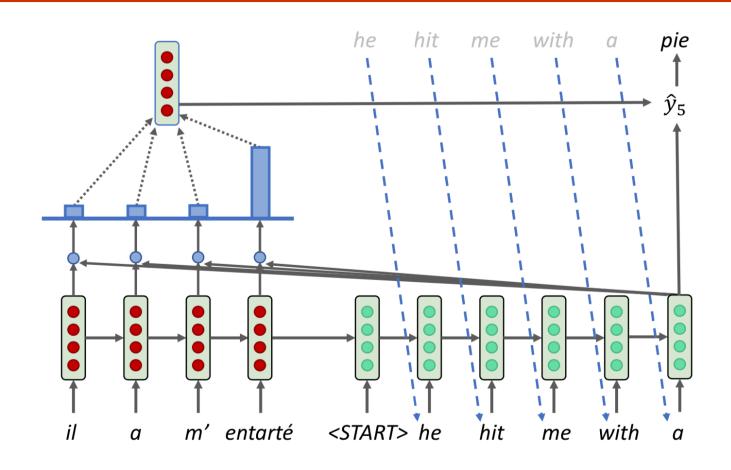
- $[z_t; s_t] \in \mathbb{R}^{2d}$
- $\hat{y}_t = softmax(g([z_t; s_t]))$

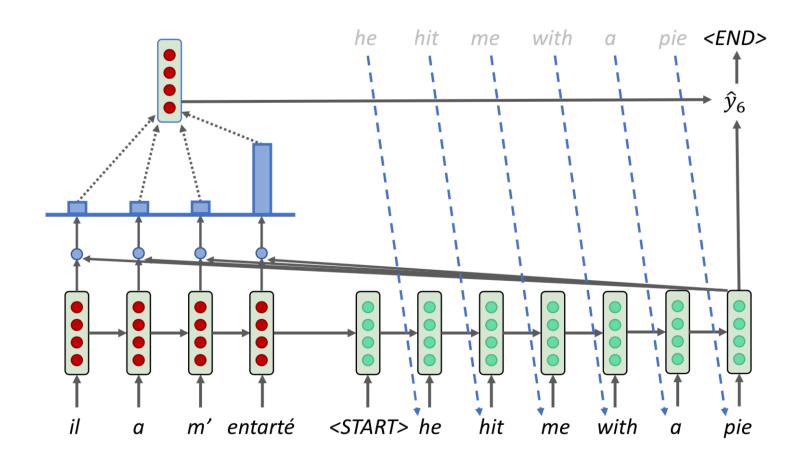












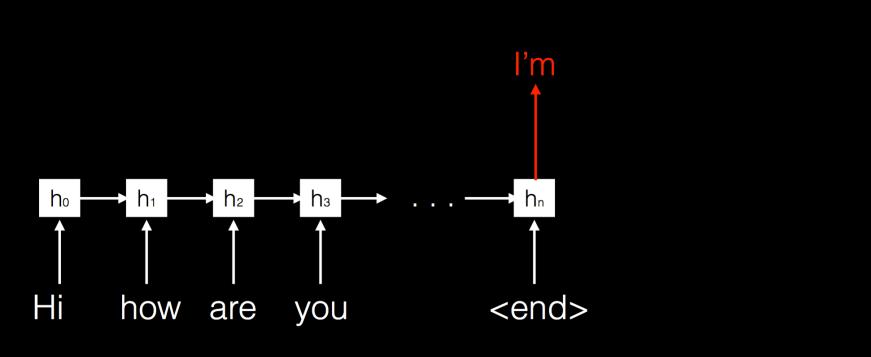
- For each time t,
  - Decoder hidden state  $s_t \in \mathbb{R}^d$ .
  - For every encoder hidden state  $h_1, \dots, h_T$ ,

- For each time t,
  - Decoder hidden state  $s_t \in \mathbb{R}^d$ .
  - For every encoder hidden state  $h_1, \dots, h_T$ ,
    - Compute attention scores  $a_t = (a_{t1}, ..., a_{tT})$  where  $a_{tu} = f(h_u, s_t)$ .

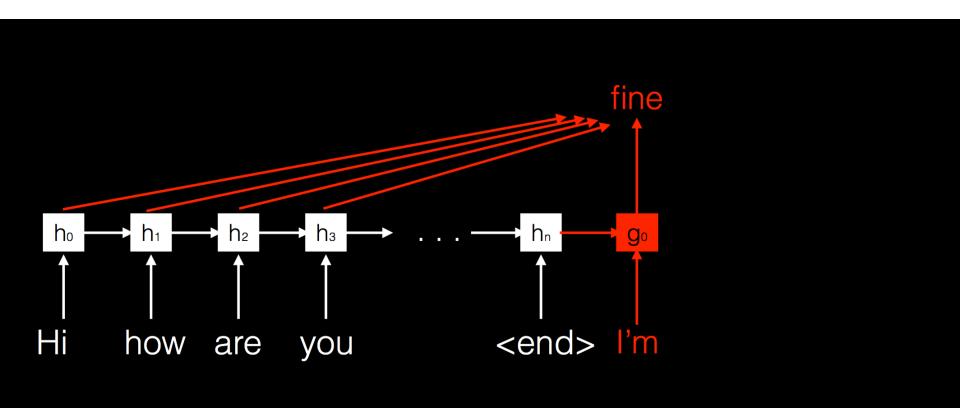
- For each time t,
  - Decoder hidden state  $s_t \in \mathbb{R}^d$ .
  - For every encoder hidden state  $h_1, \dots, h_T$ ,
    - Compute attention scores  $a_t = (a_{t1}, ..., a_{tT})$  where  $a_{tu} = f(h_u, s_t)$ .
    - Convert  $a_t$  to attention distribution  $\alpha_t = (\alpha_{t1}, ..., \alpha_{tT}) = softmax(a_t)$ .
    - Get the weighted encoder state  $z_t = \sum_{u=1}^{T} \alpha_{tu} h_u$
    - Vertically concatenate the states:  $[z_t; s_t] \in \mathbb{R}^{2d}$
    - Predict an output (as a distribution):  $\hat{y}_t = softmax(g([z_t; s_t]))$

- Basic dot-product attention:  $\alpha_{tu} = f(h_u, s_t) = s_t^T h_u$ 
  - Assume  $\dim(s_t) = \dim(h_u)$ .
  - Nothing to learn for f
- Multiplicative attention:  $\alpha_{tu} = f(h_u, s_t, ) = s_t^T W h_u$ 
  - Say  $d_1 = \dim(h_u)$ ,  $d_2 = \dim(s_t)$ .
  - Then we should learn  $W \in \mathbb{R}^{d_2 \times d_1}$  from the training data.
- Additive attention:  $a_{tu} = f(h_u, s_t) = v^T \tanh(W_h h_u + W_s s_t)$ .
  - Say  $d_3 = \dim(v)$ , which will be a new user hyper-parameter.
  - Then we should learn  $W_h \in \mathbb{R}^{d_3 \times d_1}$ ,  $W_s \in \mathbb{R}^{d_3 \times d_2}$ , and  $v \in \mathbb{R}^{d_3}$ .

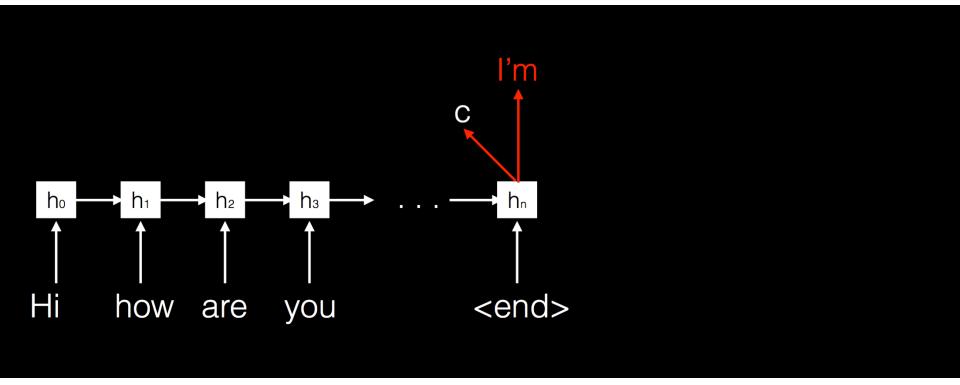
- Third version: Attention Mechanism
- Ideally output could consider 'attention' to parts of history



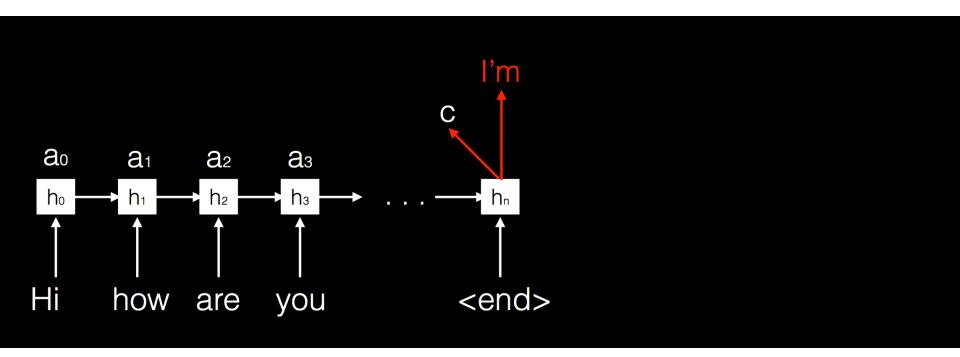
Could look at every state in the past



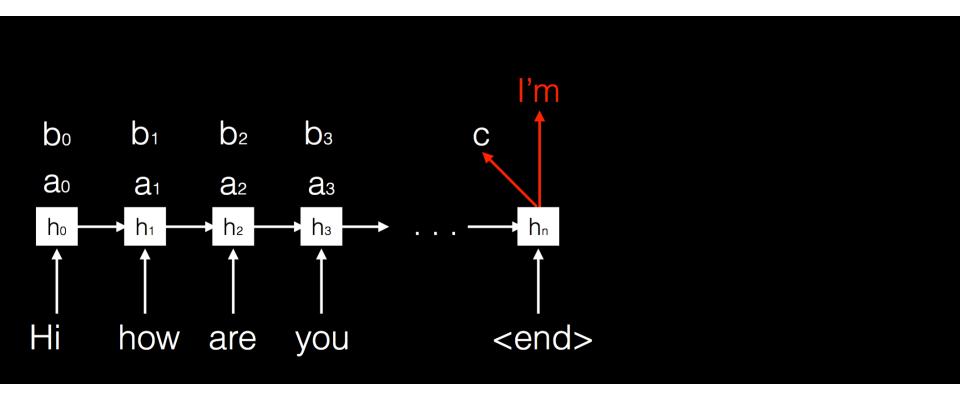
 So instead of returning a word, output the current state



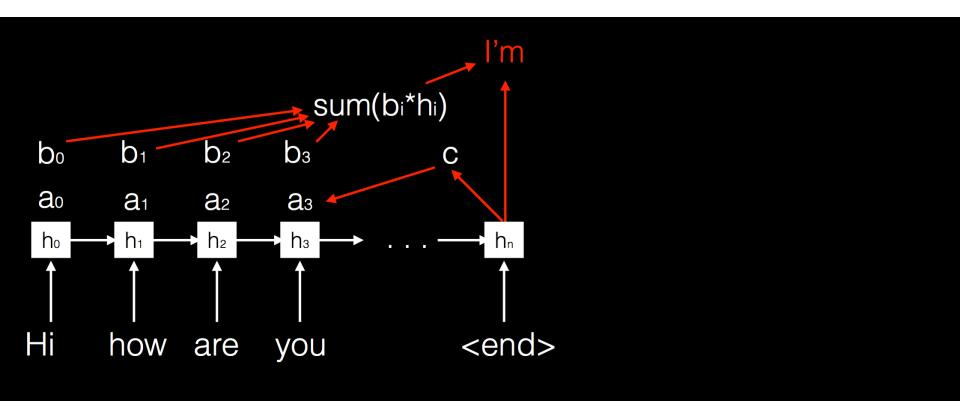
Take inner products with previous states



Take inner products with previous states

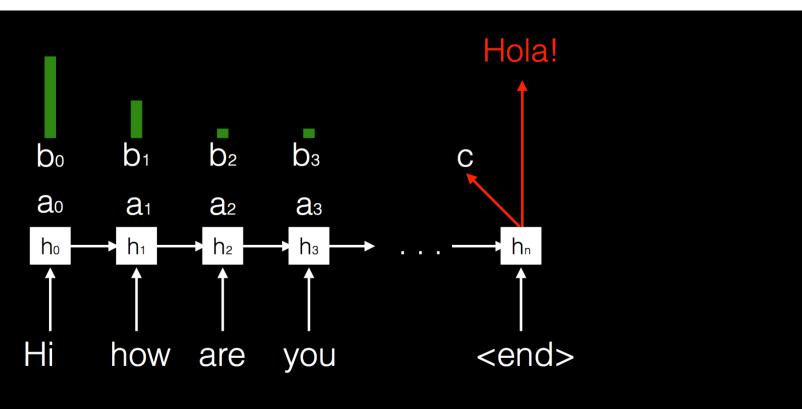


Pass through a neural net layer to predict final word



## Example III (Extension): Same with Translation!

 Same principle also applies for translation. The first prediction learns to focus on certain part of the input



 The second prediction learns to focus on certain part of the input

