

# Divide and Conquer Algorithms: Mergesort

- Read 5.1
  - What is the main idea of the divide-and-conquer technique? How does it differ from the decrease-and-conquer approach?
  - What is the general form of the recurrence relation for divide-and-conquer algorithms? What do the parameters  $a$ ,  $b$  and  $f(n)$  represent?
  - What does the **master theorem** say about a function  $T(n)$  that satisfies the general recurrence relation?
    - \* The three cases of the master theorem are written in terms of comparing  $a$  and  $b^d$ . Write them instead in terms of comparing  $\log_b a$  and  $d$ .
  - If a recursive algorithm needs to solve 3 subproblems of half the size, and it takes a constant time ( $\Theta(1)$ ) to put together the final answer, then what does the master theorem tell us about the runtime  $T(n)$  of this algorithm?
  - Describe how the MergeSort algorithm sorts an array.
    - \* Is MergeSort stable? Is it in-place?
    - \* What does the Merge subprocess do? What do the indices  $i$ ,  $j$ ,  $k$  represent?
    - \* Do we need to use the index  $k$  for the Merge process, or can we compute the needed value from  $i$  and  $j$ ?
    - \* Explain the meaning of the “copy” phase of the Merge algorithm.
    - \* Use the MergeSort algorithm to sort the characters in the word EXAMPLE.
  - Determine the runtime of MergeSort:
    - \* Start with a recurrence relation for the runtime  $C(n)$  of MergeSort, in terms of the runtime  $C_{\text{merge}}(n)$  of the Merge process.
    - \* Determine the runtime of the (non-recursive) Merge process.
    - \* Use the master theorem to determine the runtime  $C(n)$  of MergeSort.