

# Decrease-by-constant-factor algorithms

- Read 4.4, pages 150-155
  - Study the **BinarySearch** algorithm in detail.
    - \* Explain the meaning of the variables  $l$ ,  $r$  and  $m$ .
    - \* Explain the assignments to  $l$  and  $r$  inside the inner if.
    - \* How would we modify the algorithm, if the array was sorted in the reverse order (from largest to smallest)?
  - What is the best-case running time for the binary search algorithm? When does it occur?
  - What is the worst-case running time for the binary search algorithm? Develop it by building a recurrence relation.
  - Explain how the **Russian Peasant Multiplication** algorithm works.
    - \* Demonstrate its use if for  $n = 45$  and  $m = 126$ .
    - \* The algorithm could start by possibly switching the roles of  $n$  and  $m$ . Does the choice of which of the two numbers is  $n$  and which is  $m$  affect the running time of the algorithm?
    - \* Write pseudocode for the RPM algorithm using a recursive approach. What about a non-recursive solution?
  - Read up on the Josephus problem.
    - \* Manually work out what would happen in the case where  $n = 8$  and  $n = 9$ .
    - \* Make sure to understand the two recurrence relations that determine the relation between the person's position before and after a round of eliminatoins.
    - \* Exercise 4.4.15:
      - Directly compute  $J(n)$  for each  $n$  from 1 to 15 by following the game rules.
      - Explain why  $J(n) = 1$  for every power of 2.
      - Verify that the 1-bit cyclic shift of  $n$  does result in  $J(n)$  for those cases you just computed.
      - Prove that the 1-bit cyclic shift operation obeys the same recurrence relations that  $J(n)$  does, with the same start values when  $n = 1, 2$ .