Classes of Graphs

Reading

- Read 1.3, pages 19-24
 - What graph do we call a **path**? How is it denoted?
 - * What relation must there be between the order and the size in a path graph?
 - * Is a graph that has this order-size relation necessarily a path graph? What about if it is a connected graph?
 - * How many paths are there in the path graph of order n?
 - What graph do we call a **circle**? How is it denoted?
 - * What relation must there be between the order and the size in a cycle graph?
 - * Is a graph that has this order-size relation necessarily a cycle graph? What about if it is a connected graph?
 - What graph do we call **complete**? How is it denoted?
 - * What relation must there be between the order and the size in a complete graph?
 - * Is a graph that has this order-size relation necessarily a complete graph?
 - What is the **complement** of a graph? How is it denoted?
 - * How many edges does the complement of a graph have?
 - * Prove theorem 1.11: If G is a disconnected graph, then \bar{G} is connected.
 - * If G is a connected graph, is it necessary that \bar{G} be disconnected?
 - st If $ar{G}$ is connected, is it necessary that G be disconnected?
 - What graph do we call bipartite? What graph do we call complete bipartite?
 - * How many complete bipartite subgraphs does the complete graph on 5 vertices have? Can you extend this to *n* vertices?
 - \ast Prove or disprove: Every path graph of order at least 2 is bipartite.
 - * When can a cycle graph be bipartite? Prove your answer.
 - * Prove theorem 1.12: a nontrivial graph is bipartite if and only if it contains no odd cycles.
 - Two ways to construct new graphs from two existing graphs are the **join** and the **cartesian product**. Explain what those are and demonstrate for C_3 combined with C_3 .
 - * The join of two empty graphs has another name. What is that name?
 - Define the *n*-cube graphs Q_n , and draw the graphs for $n \leq 4$.
 - Practice problems: 1.24, 1.25, 1.27, 1.28

- Read 1.4, pages 26-28
 - How does a **multigraph** differ from a "normal" graph?
 - How does a **pseudograph** differ from a multigraph and from a "normal" graph?
 - What is a digraph, and how does it differ from a "normal" graph?
 - * When is such a graph called **oriented**?
 - * We can define many of the terms from graphs to this context. For instance define what a **walk**, **path**, a **cycle** would mean in a *digraph*, and what **geodesic arcs** would mean, and what the **diameter** would be.