## Midterm 2 Study Guide

## Chapters covered: 5-7

- 1. Definition of Cut Vertex (section 5.1). Examples.
- 2. Theorem 5.1, Corollary 5.2, Theorem 5.3.
- 3. Corollary 5.4. Proof of Theorem 5.5
- 4. Nonseparable graphs (section 5.2). Theorem 5.7.
- 5. Blocks. Be able to explain the equivalence relation of theorem 5.8 (why it is equivalence) and what its equivalence classes are. Corollary 5.9 (no proof).
- 6. Give examples of blocks of order 2, 3, 5 in a graph.
- 7. Definitions of vertex-cuts, minimum vertex-cuts, vertex-connectivity, edge-cuts, minimum edge-cuts, edge-connectivity (section 5.3).
- 8. Proof of Theorem 5.10, Theorem 5.11
- 9. Eulerian trails/circuits/graphs (section 6.1). Examples of graphs with and without such trails/circuits.
- 10. Proof of Theorem 6.1.
- 11. Corollary 6.2
- 12. Hamiltonian paths/cycles/graphs (section 6.2). Examples of graphs with and without such paths/cycles.
- 13. Proof of Theorem 6.4.
- 14. Theorem 6.5 and its consequences. Theorem 6.6.
- 15. Directed graphs and related definitions (section 7.1). Theorem 7.1
- 16. Weakly connected vs strongly connected. Directed distance.
- 17. Theorems 7.3, 7.4, 7.5.
- 18. Tournaments (section 7.2). Transitive tournaments. Theorem 7.6.
- 19. Proof of Theorem 7.7
- 20. Proof of Theorem 7.8
- 21. Proof of Theorem 7.9
- 22. Theorem 7.10

## Practice problems:

- 5.1, 5.3, 5.9, 5.12, 5.16, 5.18, 5.21, 5.25
- 6.4, 6.5, 6.6, 6.11, 6.12, 6.13, 6.16
- 7.3, 7.4, 7.8, 7.12