## Schedule

A week-by-week breakdown of the material.

#### Week 1

## Monday

- Introduction
- Writing Mathematics<sup>1</sup>
- Sets, set notation<sup>2</sup>
- Subsets<sup>3</sup>
- Set Operations<sup>4</sup>
- Quiz 0<sup>5</sup> (Due Monday night together with Quiz 1)
- Homework 1 due Tuesday<sup>6</sup>
- Prepare for class presentation:
  - Exercises 1.9, 1.19, 1.34

## **Tuesday**

- Indexed Collections of sets<sup>7</sup>
- Set Partitions<sup>8</sup>
- Cartesian Products<sup>9</sup>
- Quiz 1<sup>10</sup> (Due Monday night together with Quiz 2)
- Homework 2 due Wednesday<sup>11</sup>
- Prepare for class presentation:
  - Exercises 1.41, 1.54

### Wednesday

- Statements<sup>12</sup>
- Negations<sup>13</sup>

<sup>&</sup>lt;sup>1</sup>notes/writing.html

<sup>&</sup>lt;sup>2</sup>notes/sets\_notation.html

<sup>&</sup>lt;sup>3</sup>notes/subsets.html

<sup>&</sup>lt;sup>4</sup>notes/set operations.html

<sup>&</sup>lt;sup>5</sup>https://moodle.hanover.edu/mod/quiz/view.php?id=19351

<sup>&</sup>lt;sup>6</sup>assignments/hw1.html

<sup>&</sup>lt;sup>7</sup>notes/indexed collections.html

<sup>&</sup>lt;sup>8</sup>notes/sets\_partitions.html

<sup>&</sup>lt;sup>9</sup>notes/cartesian products.html

<sup>&</sup>lt;sup>10</sup>https://moodle.hanover.edu/mod/quiz/view.php?id=19389

<sup>&</sup>lt;sup>11</sup>assignments/hw2.html

<sup>&</sup>lt;sup>12</sup>notes/statements.html

<sup>&</sup>lt;sup>13</sup>notes/negation.html

- Disjunction and Conjunction<sup>14</sup>
- Implications<sup>15</sup>
- Quiz 2<sup>16</sup> (Due Tuesday night)
- Homework 3 due Thursday<sup>17</sup>
- Prepare for class presentation:
  - Exercises 2.18, 2.29, 2.32

## Thursday

- Biconditional 18
- Tautologies, Contradictions<sup>19</sup>
- Logical Equivalence<sup>20</sup>
- Fundamental properties of logical equivalence<sup>21</sup>
- Quiz 3<sup>22</sup> (Due Wednesday night)
- Homework 4 due Friday<sup>23</sup>
- Prepare for class presentation:
  - Exercises 2.39, 2.50, 2.53

## **Friday**

• Exam 1

#### Week 2

### **Monday**

- Quantified Statements<sup>24</sup>
- Characterization<sup>25</sup>
- Quiz 4<sup>26</sup> (Due Sunday night)
- Homework 5 due Tuesday<sup>27</sup>

<sup>&</sup>lt;sup>14</sup>notes/disjunction conjunction.html

<sup>&</sup>lt;sup>15</sup>notes/implications.html

<sup>&</sup>lt;sup>16</sup>https://moodle.hanover.edu/mod/quiz/view.php?id=19403

<sup>&</sup>lt;sup>17</sup>assignments/hw3.html

<sup>&</sup>lt;sup>18</sup>notes/biconditional.html

<sup>&</sup>lt;sup>19</sup>notes/tautologies contradictions.html

<sup>&</sup>lt;sup>20</sup>notes/logical equivalence.html

<sup>&</sup>lt;sup>21</sup>notes/logical equiv properties.html

<sup>&</sup>lt;sup>22</sup>https://moodle.hanover.edu/mod/quiz/view.php?id=19429

<sup>&</sup>lt;sup>23</sup>assignments/hw4.html

<sup>&</sup>lt;sup>24</sup>notes/quantified\_statements.html

<sup>&</sup>lt;sup>25</sup>notes/characterization.html

<sup>&</sup>lt;sup>26</sup>https://moodle.hanover.edu/mod/quiz/view.php?id=19644

<sup>&</sup>lt;sup>27</sup>assignments/hw5.html

#### **Tuesday**

- Trivial and Vacuous Proofs<sup>28</sup>
- Direct Proofs<sup>29</sup>
- Proof by Contrapositive<sup>30</sup>
- Prepare for class presentation:
  - Exercises 3.10, 3.18
- Quiz 5<sup>31</sup> (Due Monday night)
- Homework 6 due Wednesday<sup>32</sup>

#### Wednesday

- Proof by cases<sup>33</sup>
- Direct and Contrapositive proofs for divisibility<sup>34</sup>
- Direct and Contrapositive proofs for congruence<sup>35</sup>
- Prepare for class presentation:
  - Exercises 3.28, 4.16
- Quiz 6<sup>36</sup> (Due Tuesday night)
- Homework 7 due Thursday<sup>37</sup>

## Thursday

- Direct and Contrapositive proofs for real numbers<sup>38</sup>
- Proofs involving sets<sup>39</sup>
- Properties of set operations, cartesian products<sup>40</sup>
- Prepare for class presentation:
  - Exercises 4.34, 4.38, 4.44, 4.58, 4.62, 4.64
- Quiz 7<sup>41</sup> (Due Wednesday night)
- Homework 8 due Friday<sup>42</sup>

<sup>&</sup>lt;sup>28</sup>notes/trivial vacuous proofs.html

<sup>&</sup>lt;sup>29</sup>notes/direct proofs.html

<sup>&</sup>lt;sup>30</sup>notes/contrapositive.html

<sup>&</sup>lt;sup>31</sup>https://moodle.hanover.edu/mod/quiz/view.php?id=19782

<sup>&</sup>lt;sup>32</sup>assignments/hw6.html

<sup>&</sup>lt;sup>33</sup>notes/proofs\_cases.html

<sup>&</sup>lt;sup>34</sup>notes/proofs\_divisibility.html

<sup>&</sup>lt;sup>35</sup>notes/proofs\_congruence.html

<sup>&</sup>lt;sup>36</sup>https://moodle.hanover.edu/mod/quiz/view.php?id=19786

<sup>&</sup>lt;sup>37</sup>assignments/hw7.html

<sup>&</sup>lt;sup>38</sup>notes/proofs\_reals.html

<sup>&</sup>lt;sup>39</sup>notes/proofs\_sets.html

<sup>&</sup>lt;sup>40</sup>notes/set\_properties.html

<sup>41</sup> https://moodle.hanover.edu/mod/quiz/view.php?id=19787

<sup>&</sup>lt;sup>42</sup>assignments/hw8.html

## **Friday**

- Catching up
- Exam 2

#### Week 3

## **Monday**

- Proofs by counterexample<sup>43</sup>
- Proofs by contradiction<sup>44</sup>
- Existence proofs<sup>45</sup>
- Prepare for class presentation:
  - Exercises 5.6, 5.18
- Quiz 8<sup>46</sup> (Due Sunday night)
- Homework 9 due Tuesday<sup>47</sup>

## **Tuesday**

- Principle of Mathematical Induction<sup>48</sup>
- General Principle of Mathematical Induction<sup>49</sup>
- Proofs by Minimum Counterexample<sup>50</sup>
- Prepare for class presentation:
  - Exercises 6.8, 6.18
- Quiz 9<sup>51</sup> (Due Monday night)
- Homework 10 due Wednesday<sup>52</sup>

## Wednesday

- Strong Principle of Mathematical Induction
- Conjectures
- Introduction to Relations
- Quiz 10 (Due Tuesday night)

<sup>&</sup>lt;sup>43</sup>notes/proofs\_counterexample.html

<sup>&</sup>lt;sup>44</sup>notes/proofs\_contradiction.html

<sup>&</sup>lt;sup>45</sup>notes/proofs\_existence.html

<sup>46</sup>https://moodle.hanover.edu/mod/quiz/view.php?id=19997

<sup>&</sup>lt;sup>47</sup>assignments/hw9.html

<sup>&</sup>lt;sup>48</sup>notes/mathematical induction.html

<sup>&</sup>lt;sup>49</sup>notes/general induction.html

<sup>&</sup>lt;sup>50</sup>notes/proofs\_minimum\_counterexample.html

<sup>&</sup>lt;sup>51</sup>https://moodle.hanover.edu/mod/quiz/view.php?id=20014

<sup>&</sup>lt;sup>52</sup>assignments/hw10.html

## **Thursday**

- Properties of Relations
- Equivalence Relations
- Quiz 11 (Due Wednesday night)

## **Friday**

- Catchup
- Exam 3

#### Week 4

### **Monday**

- Equivalence Classes
- Congruences as an equivalence
- Quiz 12 (Due Sunday night)

### **Tuesday**

- Arithmetic on Integers modulo n
- Definition of functions
- Quiz 13 (Due Monday night)

## Wednesday

- One-to-one and onto functions
- Bijective functions, Inverse function
- Image and inverse image of sets under functions/relations. Properties
- Quiz 14 (Due Tuesday night)

## Thursday

- Numerically Equivalent sets
- Denumerable sets
- Quiz 15 (Due Wednesday night)

# Friday

- Uncountable sets
- Comparing cardinalities
- Schroder-Bernstein theorem
- Wrap-up
- Exam 4