## Schedule

A week-by-week breakdown of the material.

# Week 1 (01/05-01/09)

- Day 1
  - Numbers: Rationals, Reals, Complex<sup>1</sup>
  - Basic proof techniques: Direct<sup>2</sup>
  - Assignment 1<sup>3</sup>
- Day 2
  - Basic proof techniques: Indirect<sup>4</sup>
  - Square root of 2 is irrational<sup>5</sup>
- Day 3
  - Quantifiers<sup>6</sup>
  - Principle of Mathematical Induction<sup>7</sup>
  - Assignment 28
- Day 4
  - Strong induction and Well-Ordering Principle<sup>9</sup>
  - Fibonnaci Numbers<sup>10</sup>

#### Week 2 (01/12-01/16)

- Day 1
  - Divisibility<sup>11</sup>
- Day 2
  - Prime and Composite Numbers<sup>12</sup>

<sup>&</sup>lt;sup>1</sup>notes/numbers\_intro.html

<sup>&</sup>lt;sup>2</sup>notes/proofs\_basic.html

<sup>&</sup>lt;sup>3</sup>assignments/1.html

<sup>&</sup>lt;sup>4</sup>notes/proofs\_basic.html

<sup>&</sup>lt;sup>5</sup>notes/irrationality\_of\_sqrt2.html

<sup>&</sup>lt;sup>6</sup>notes/proofs\_quantifiers.html

<sup>&</sup>lt;sup>7</sup>notes/proofs\_induction.html

<sup>&</sup>lt;sup>8</sup>assignments/2.html

<sup>&</sup>lt;sup>9</sup>notes/proofs induction other.html

<sup>&</sup>lt;sup>10</sup>notes/numbers\_fibonacci.html

<sup>&</sup>lt;sup>11</sup>notes/numbers\_divisibility.html

<sup>&</sup>lt;sup>12</sup>notes/primes\_intro.html

- Assignment 3<sup>13</sup>
- Day 3
  - Patterns in the Primes<sup>14</sup>
  - Common Divisors<sup>15</sup>
- Day 4
  - The Division Theorem<sup>16</sup>

### Week 3 (01/19-01/23)

- Day 1
  - A weird number system<sup>17</sup>
  - The Division Theorem (cont)<sup>18</sup>
  - Assignment 4<sup>19</sup>
- Day 2
  - The Euclidean Algorithm<sup>20</sup>
- Day 3
  - Diophantine Equations<sup>21</sup>
  - Euclidean Division and Diophantine Equations<sup>22</sup>
- Day 4
  - Finding all Solutions<sup>23</sup>
  - Assignment 5<sup>24</sup>

#### Week 4 (01/26-01/30)

- Day 1
  - Finding all Solutions (cont)<sup>25</sup>

<sup>&</sup>lt;sup>13</sup>assignments/3.html

<sup>&</sup>lt;sup>14</sup>notes/primes\_patterns.html

<sup>&</sup>lt;sup>15</sup>notes/numbers gcd.html

<sup>&</sup>lt;sup>16</sup>notes/numbers\_division\_theorem.html

<sup>&</sup>lt;sup>17</sup>notes/weird\_number\_system.html

<sup>&</sup>lt;sup>18</sup>notes/numbers\_division\_theorem.html

<sup>&</sup>lt;sup>19</sup>assignments/4.html

<sup>&</sup>lt;sup>20</sup>notes/numbers euclidean algorithm.html

<sup>&</sup>lt;sup>21</sup>notes/equations\_diophantine\_intro.html

<sup>&</sup>lt;sup>22</sup>notes/equations\_diophantine\_and\_euclidean.html

<sup>&</sup>lt;sup>23</sup>notes/equations\_diophantine\_all\_solutions.html

<sup>&</sup>lt;sup>24</sup>assignments/5.html

<sup>&</sup>lt;sup>25</sup>notes/equations\_diophantine\_all\_solutions.html

- Fundamental Theorem of Arithmetic<sup>26</sup>
- Day 2
  - Consequences of Fundamental Theorem<sup>27</sup>
- Day 3
  - Modular Arithmetic and Congruences<sup>28</sup>
- Day 4
  - Arithmetic with Congruences<sup>29</sup>

### Week 5 (02/02-02/06)

- Day 1
  - Review
- Day 2
  - MIDTERM (Study guide<sup>30</sup>)
- Day 3
  - Chinese Remainder Theorem<sup>31</sup>
  - Assignment 6<sup>32</sup>
- Day 4
  - Congruence Classes as a Number System<sup>33</sup>

# Week 6 (02/09-02/13)

- Day 1
  - Multiplicative Inverses<sup>34</sup>
- Day 2
  - Multiplicative Inverses (cont)<sup>35</sup>
- Day 3

<sup>&</sup>lt;sup>26</sup>notes/numbers fundamental theorem.html

<sup>&</sup>lt;sup>27</sup>notes/numbers\_fta\_consequences.html

<sup>&</sup>lt;sup>28</sup>notes/congruence\_intro.html

<sup>&</sup>lt;sup>29</sup>notes/congruence\_arithmetic.html

<sup>&</sup>lt;sup>30</sup>studyGuide1.html

<sup>&</sup>lt;sup>31</sup>notes/congruence\_chinese\_remainder.html

<sup>&</sup>lt;sup>32</sup>assignments/6.html

<sup>&</sup>lt;sup>33</sup>notes/congruence\_system.html

<sup>&</sup>lt;sup>34</sup>notes/congruence\_multiplicative\_inverses.html

<sup>&</sup>lt;sup>35</sup>notes/congruence\_multiplicative\_inverses.html

- Basics of Encryption<sup>36</sup>
- Encryption via Multiplication<sup>37</sup>
- Day 4
  - Fermat's Little Theorem<sup>38</sup>
  - Assignment 7<sup>39</sup>

#### Week 7 (02/16-02/20)

- Day 1
- Day 2
  - Reduced Residues and phi<sup>40</sup>
- Day 3
  - Reduced Residues and phi (cont)<sup>41</sup>
- Day 4
  - Reduced Residues and phi (cont)<sup>42</sup>

#### Week 8 (02/23-02/27)

**BREAK** 

## Week 9 (03/02-03/06)

- Day 1
  - Euler's Theorem<sup>43</sup>
  - Assignment 8<sup>44</sup>
- Day 2
  - Encryption via Exponentiation<sup>45</sup>
- Day 3

<sup>&</sup>lt;sup>36</sup>notes/encryption\_basic.html

<sup>&</sup>lt;sup>37</sup>notes/encryption\_mult.html

<sup>&</sup>lt;sup>38</sup>notes/congruence\_fermats.html

<sup>&</sup>lt;sup>39</sup>assignments/7.html

<sup>&</sup>lt;sup>40</sup>notes/residues\_basic.html

<sup>&</sup>lt;sup>41</sup>notes/residues\_basic.html

<sup>&</sup>lt;sup>42</sup>notes/residues basic.html

<sup>&</sup>lt;sup>43</sup>notes/residues\_eulers\_theorem.html

<sup>&</sup>lt;sup>44</sup>assignments/8.html

<sup>&</sup>lt;sup>45</sup>notes/encryption\_exponentiation.html

- Snow Day
- Day 4
  - Public Key Cryprography and RSA<sup>46</sup>

## Week 10 (03/09-03/13)

- Day 1
  - Public Key Cryprography and RSA (cont)<sup>47</sup>
- Day 2
  - Public Key Cryprography and RSA (cont)<sup>48</sup>
- Day 3
  - Order of Elements in Zn<sup>49</sup>
- Day 4
  - Order of Elements in Zn (cont)<sup>50</sup>

## Week 11 (03/16-03/20)

- Day 1
  - Review
- Day 2
  - MIDTERM (Study guide<sup>51</sup>)
- Day 3
  - Polynomials over Zn<sup>52</sup>
- Day 4
  - Primitive Roots<sup>53</sup>

<sup>&</sup>lt;sup>46</sup>notes/encryption\_rsa.html

<sup>&</sup>lt;sup>47</sup>notes/encryption\_rsa.html

<sup>&</sup>lt;sup>48</sup>notes/encryption\_rsa.html

<sup>&</sup>lt;sup>49</sup>notes/residues order.html

<sup>&</sup>lt;sup>50</sup>notes/residues\_order.html

 $<sup>^{51}</sup>$ studyGuide2.html

<sup>&</sup>lt;sup>52</sup>notes/residues\_polynomials.html

<sup>&</sup>lt;sup>53</sup>notes/residues\_primitive\_roots.html

#### Week 12 (03/23-03/27)

- Day 1
  - Primitive Roots (cont)<sup>54</sup>
- Day 2
  - Applications of Primitive Roots: Diffie-Hellman protocol<sup>55</sup>
  - Assignment 9<sup>56</sup>
- Day 3
  - Quadratic Residues<sup>57</sup>
- Day 4
  - Quadratic Residues (cont)<sup>58</sup>

#### Week 13 (03/30-04/03)

- Day 1
  - Everything below is work in progress.
  - Law of Quadratic Reciprocity<sup>59</sup>
- Day 2
  - Gauss's Lemma<sup>60</sup>
- Day 3
- Day 4

# Week 14 (04/06-04/10)

- Day 1
- Day 2
- Day 3
- Day 4

<sup>&</sup>lt;sup>54</sup>notes/residues\_primitive\_roots.html

<sup>&</sup>lt;sup>55</sup>notes/encryption\_diffie\_hellman.html

<sup>&</sup>lt;sup>56</sup>assignments/9.html

<sup>&</sup>lt;sup>57</sup>notes/residues\_quadratic.html

<sup>&</sup>lt;sup>58</sup>notes/residues\_quadratic.html

<sup>&</sup>lt;sup>59</sup>notes/residues\_reciprocity.html

<sup>60</sup> notes/residues\_gauss\_lemma.html