

Schedule

A week-by-week breakdown of the material.

Week 1 (01/05-01/09)

- Day 1
 - Numbers: Rationals, Reals, Complex¹
 - Basic proof techniques: Direct²
 - Assignment 1³
- Day 2
 - Basic proof techniques: Indirect⁴
 - Square root of 2 is irrational⁵
- Day 3
 - Quantifiers⁶
 - Assignment 2⁷
- Day 4
 - Principle of Mathematical Induction⁸

Week 2 (01/12-01/16)

- Day 1
 - Strong induction⁹
 - Well Ordering Principle¹⁰
- Day 2
 - Fibonacci Numbers¹¹
- Day 3
 - Divisibility¹²

¹[notes/numbers_intro.html](#)

²[notes/proofs_basic.html](#)

³[assignments/1.html](#)

⁴[notes/proofs_basic.html](#)

⁵[notes/irrationality_of_sqrt2.html](#)

⁶[notes/proofs_quantifiers.html](#)

⁷[assignments/2.html](#)

⁸[notes/proofs_induction.html](#)

⁹[notes/proofs_strong_induction.html](#)

¹⁰[notes/proofs_well_ordering.html](#)

¹¹[notes/numbers_fibonacci.html](#)

¹²[notes/numbers_divisibility.html](#)

- Prime and Composite Numbers¹³
- Day 4
 - Prime Factorization: Existence¹⁴

Week 3 (01/19-01/23)

- Day 1
 - Infinitude of Primes¹⁵
 - The Prime Number Theorem¹⁶
- Day 2
 - Common Divisors¹⁷
- Day 3
 - The Division Theorem¹⁸
- Day 4
 - Euclidean Division Algorithm¹⁹

Week 4 (01/26-01/30)

- Day 1
 - GCD via Euclidean Algorithm²⁰
- Day 2
 - Diophantine Equations²¹
- Day 3
 - Euclidean Division and Diophantine Equations²²
- Day 4
 - Other Diophantine Equations²³
 - Diophantine Equations: Finding all solutions²⁴

¹³[notes/primes_intro.html](#)

¹⁴[notes/primes_factorization_existence.html](#)

¹⁵[notes/primes_infinitude.html](#)

¹⁶[notes/primes_theorem.html](#)

¹⁷[notes/numbers_gcd.html](#)

¹⁸[notes/numbers_division_theorem.html](#)

¹⁹[notes/numbers_euclidean.html](#)

²⁰[notes/numbers_gcd_compute.html](#)

²¹[notes/equations_diophantine_intro.html](#)

²²[notes/equations_diophantine_and_euclidean.html](#)

²³[notes/equations_diophantine_other.html](#)

²⁴[notes/equations_diophantine_all_solutions.html](#)

Week 5 (02/02-02/06)

- Day 1
 - Fundamental Theorem of Arithmetic²⁵
 - Finding all Divisors²⁶
- Day 2
 - MIDTERM
- Day 3
 - Modular Arithmetic and Congruences²⁷
- Day 4
 - Arithmetic with Congruences²⁸
 - Divisibility Tests²⁹

Week 6 (02/09-02/13)

- Day 1
 - Chinese Remainder Theorem³⁰
- Day 2
 - Congruence Classes as a Number System³¹
- Day 3
 - \mathbb{Z}_n as a Ring³²
- Day 4
 - Multiplicative Inverses³³
 - Multiplicative Cancellation³⁴

²⁵[notes/numbers_fundamental_theorem.html](#)

²⁶[notes/numbers_all_divisors.html](#)

²⁷[notes/congruence_intro.html](#)

²⁸[notes/congruence_arithmetic.html](#)

²⁹[notes/numbers_divisibility_tests.html](#)

³⁰[notes/congruence_chinese_remainder.html](#)

³¹[notes/congruence_system.html](#)

³²[notes/congruence_ring.html](#)

³³[notes/congruence_multiplicative_inverses.html](#)

³⁴[notes/congruence_multiplicative_cancellation.html](#)

Week 7 (02/16-02/20)

- Day 1
 - Wilson's Theorem³⁵
- Day 2
 - Basics of Encryption³⁶
- Day 3
 - Encryption via Multiplication³⁷
- Day 4
 - Fermat's Little Theorem³⁸

Week 8 (02/23-02/27)

BREAK

Week 9 (03/02-03/06)

- Day 1
 - Reduced Residues and Euler's ϕ ³⁹
- Day 2
 - Euler's Theorem⁴⁰
- Day 3
 - Fast exponentiation⁴¹
- Day 4
 - Encryption via Exponentiation⁴²

³⁵[notes/congruence_wilsons.html](#)

³⁶[notes/encryption_basic.html](#)

³⁷[notes/encryption_mult.html](#)

³⁸[notes/congruence_fermats.html](#)

³⁹[notes/residues_basics.html](#)

⁴⁰[notes/residues_eulers_theorem.html](#)

⁴¹[notes/residues_exponentiation.html](#)

⁴²[notes/encryption_exp.html](#)

Week 10 (03/09-03/13)

- Day 1
 - Public Keys and RSA⁴³
- Day 2
 - Order of Elements in \mathbb{Z}_n ⁴⁴
- Day 3
 - Polynomials over \mathbb{Z}_n ⁴⁵
- Day 4
 - Primitive Roots⁴⁶

Week 11 (03/16-03/20)

- Day 1
 - Primitive Root Theorem⁴⁷
- Day 2
 - MIDTERM
 - Applications of Primitive Roots: Diffie-Hellman protocol⁴⁸
- Day 3
 - Congruential Random Number Generators⁴⁹
- Day 4

Week 12 (03/23-03/27)

- Day 1
 - Quadratic Residues⁵⁰
- Day 2
 - The Legendre Symbol⁵¹

⁴³[notes/encryption_rsa.html](#)

⁴⁴[notes/residues_order.html](#)

⁴⁵[notes/residues_polynomials.html](#)

⁴⁶[notes/residues_primitive_roots.html](#)

⁴⁷[notes/residues_primitive_root_theorem.html](#)

⁴⁸[notes/encryption_diffie_hellman.html](#)

⁴⁹[notes/numbers_random.html](#)

⁵⁰[notes/residues_quadratic.html](#)

⁵¹[notes/residues_legendre.html](#)

- Day 3
 - Euler’s Identity⁵²
- Day 4
 - Properties of Legendre symbol⁵³

Week 13 (03/30-04/03)

- Day 1
 - Law of Quadratic Reciprocity⁵⁴
- Day 2
 - Gauss’s Lemma⁵⁵
- Day 3
 - []
- Day 4

Week 14 (04/06-04/10)

- Day 1
- Day 2
- Day 3
- Day 4

⁵²[notes/residues_eulers_identity.html](#)

⁵³[notes/residues_legendre_properties.html](#)

⁵⁴[notes/residues_reciprocity.html](#)

⁵⁵[notes/residues_gauss_lemma.html](#)