Midterm 2 Study Guide

The test covers all the material discussed in chapters 6, 7, 8, and sections 9.1-9.3, and homeworks 5 through 8. The following set of questions is meant to help guide your study and is not meant to be exhaustive of all the possibilities.

- 1. Describe what the universal Python program does, and provide code for it.
- 2. Define the language YesOnString and show that it is recognizable (by writing a Python program that recognizes it).
- 3. Write a program that recognizes, but does not decide, the language of genetic strings containing "GAGA". (Can you generalize your proof to *any* decidable language?)
- 4. Give equivalent formulations to the phrase "problem A is (Turing) reducible to problem B".
- 5. Suppose that problem A Turing reduces to problem B. Which of the following are necessarily true?
 - If A is computable then B is computable.
 - If A is undecidable then B is undecidable.
 - If B also reduces to A then A and B must be the same problem.
 - If B reduces to C then A reduces to C.
 - If A reduces to C then B reduces to C.
 - If we have an *oracle* program for deciding A, we can use it to solve problem B.
 - If we have an *oracle* program for deciding B, we can use it to solve problem A.
 - Problem A is solvable.
 - Problem B is solvable.
 - Problem A is no harder to solve than problem B.
- 6. Prove the following reductions, using explicit Python code where needed.
 - HaltsOnEmpty reduces to HaltsOnAllNonempty.
 - HaltsOnAllNonempty reduces to HaltsOnEmpty.
 - HaltsOnEmpty reduces to YesOnString.
 - YesOnString reduces to HaltsOnEmpty.
- 7. Define what it means for a Python program to halt (page 126)
- 8. Define the computational problem Computes F for a given computational problem F.
- 9. True or False:
 - If F is computable then Computes_F is also computable.

- If F is uncomputable then Computes_F is computable.
- If F is computable then Computes_F is uncomputable.
- If F is uncomputable then Computes_F is also uncomputable.
- 10. Give an example of a question about programs that is actually computable.
- 11. Describe how, given a computation tree for a non-deterministic program, we can determine the output of the computation (page 150).
- 12. Given a non-deterministic Turing Machine and an input string, draw the corresponding computation tree and determine the outcome of the computation. (Like figure 8.10 but showing the complete computation history)
- 13. Describe precisely how a non-deterministic Turing Machine differs from a deterministic Turing Machine.
- 14. Let L be an undecidable language. Prove that if L is recognizable then its complement \bar{L} is unrecognizable.
- 15. Classify the following languages according to whether they are: decidable, recognizable but undecidable, corecognizable but undecidable, or neither recognizable nor corecognizable (nasty).
 - YesOnString
 - NotYesOnString
 - containsGAGA
 - HaltsOnEmpty
 - Complement of HaltsOnEmpty
 - Valid Python programs
 - Python programs that do not halt on empty
- 16. Give a precise definition of a deterministic finite automaton (DFA).
- 17. Can a DFA loop on a given input? Explain.
- 18. Give a precise definition of a *non-deterministic finite automaton (NFA)*. What is different about a *strict* NFA?
- 19. Given an NFA, draw an equivalent DFA (like Figure 9.7).
- 20. Provide as many examples as you can of languages that can be decided by an NFA but not by a DFA.